



Preface

Content

Interactive design aids in accordance to US codes ACI 318-11, AISC 14th edition and ASCE-7-10

Guidelines of use

After installing a free trial or demo version the interactive templates will be available free of charge. The only requirement is a registration at www.VCmaster.com.

The examples provided have been created using VCmaster. All annotated and illustrated design aids can be used as a basis to create own templates. In order to do this a full version of VCmaster is necessary.

All templates are linked to various databases by TAB()- or SEL() functions. For instructional purposes these links are displayed in this document, but can also be hidden when printing.

What is VCmaster?

VCmaster is a software application for technical documentation specifically designed for engineers. The unique software concept integrates all structural design and CAD software. Universal interfaces guarantee easy data transfer, so that the output of all programs can be transposed.

Beside its functions for documentation, VCmaster offers an intuitive concept enabling engineers to carry out calculations. The input of mathematic formulas can be executed in natural notation directly in the document itself. The software significantly supports the reuse of structural calculations and documents. VCmaster simplifies modifications and adjustments and automates standard tasks. Collaboration with work-groups or with other offices and clients is uncomplicated as well. As a result, processing time and costs can be considerably reduced.

System Requirements

VCmaster 2017 or newer

Development and Copyrights

VCmaster has been developed in Germany

VCmaster is a registered trademark

All templates are made in the U.S.A.

© Veit Christoph GmbH 1995-2018

www.VCmaster.com



Contents

Chapter 1: Concrete Design	4
Corbel Design	4
Precast Spandrel Beam for Combined Shear and Torsion	7
Beam Ledge Design	11
Rectangular Section with Tension Reinforcement	14
Rectangular Section with Compression Reinforcement	16
Shear Reinforcement for Section Subject to Q & N	19
Shear Reinforcement for Section Subject to Q & T	22
Deflection of Shored Composite Section	24
Flexural Design of Flanged Section	28
Cracking Moment Strength for Prestressed Sections	31
Flexural Strength of Prestressed Member	32
Tension Controlled Limit for Prestressed Flexural Member	34
Prestress Losses	36
Punching Shear Reinforcement on Slab	39
One Way Joist	41
Two-Way Slab Analyzed by the Direct Design Method	47
Development Length of Bars in Tension	50
Group of Headed Studs in Tension Near an Edge	52
Shear Strength of Slab at Column Support	54
Simple Span Deep Beam by Strut-and-Tie Model	56
Continuous Deep Beam by Strut-and-Tie Model	60
Transfer of Horizontal Force at Base of Column	65
Bearing Wall by Empirical Method	67
Shear Design of Wall	70
Shear Friction	73
Single Adhesive Anchor in Tension	75
Single Headed Anchor Bolt in Tension	77
Single Headed Anchor Bolt in Shear Near an Edge	79
Deflection of Simple Beam	81
Shear Reinforcement for Section Subject to Q & M	84
Shear Reinforcement at Opening	87
Horizontal Shear for Composite Slab and Precast Beam	90

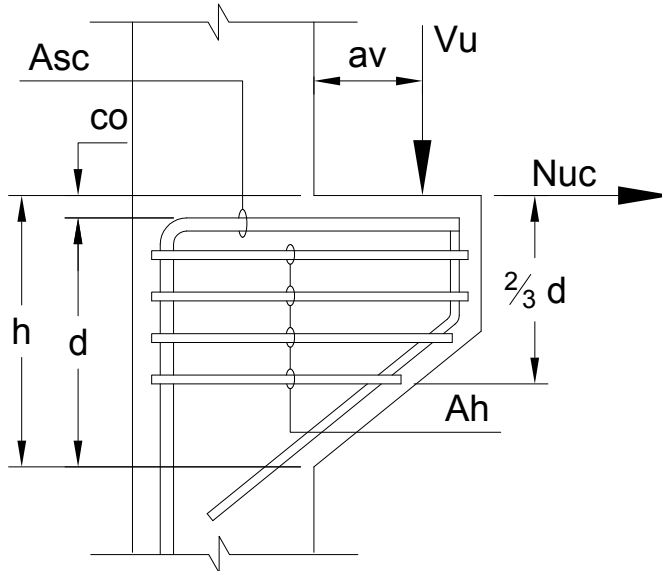


Chapter 2: Foundation Design	92
Reinforcement of Shallow Foundation	92
Depth of Shallow Foundation	95
Depth for Pile Cap	98
Slab on Grade	101
Chapter 3: Steel Design	102
W-Shapes in Strong Axis Bending, Braced at Some Points	102
W-Shape in Strong Axis Bending, Continuously Braced	106
W-Shape in Minor Axis Bending	109
W-Shape Subjected to Tension Force and Bending Moments	112
W-Shapes in Axial Compression	117
WT-Shapes in Axial Compression	120
Built-Up W-Shapes with Slender Elements	124
W-Shapes Subjected to Compression and Bending	128
W-Shape Subjected to P and M including the Second Order Effect	134
HSS-Shape in Strong Axis Bending	140
W-Shape Subjected to Tension Force in a Bolted Connection	143
WT-Shape Subjected to Tension Force in Welded Connections	146
Interior Panel of Built-Up Girder with Transverse Stiffeners	149
End Panel of Built-Up Girder with Transverse Stiffeners	151
Composite Beam Subjected to Bending	153
Chapter 4: Connection Design	159
Base Plate Subjected to Concentric Loading	159
Base Plate Subjected to Small Eccentricity	161
Base Plate Subjected to Large Eccentricity	164
Shear Lug	167
Fillet Weld Subjected to Longitudinal Shear Force	169
Bolts in Bearing Type Connection Subjected to T & V	171
Slip Critical Connection with Short-Slotted Holes	173
Chapter 5: Design Loads	175
Wind load for Solid Freestanding Walls & Signs	175
Snow Loads for Flat Roof	178
Snow Loads for Sloped Roof	179
Seismic Base Shear	180



Chapter 1: Concrete Design

Design of Corbel as per ACI 318-11 Chapter 11



System

Corbel Width, b =		14.0 in
Corbel Height, h =		12.0 in
Concrete Cover, co =		1.0 in
Corbel Depth, d =	$h - co = 12.0 - 1.0$	= 11.0 in
Distance from Column Face to Vertical Load, a_v =		3.0 in

Load

Ultimate Vertical Load, V_u =	88.8 kips
Ultimate Horizontal Load, N_{uc} =	32.0 kips

Material Properties

Concrete Strength, f'_c =	5000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), $\mu = 1.4 * \lambda$	= 1.40



Check Vertical Load Capacity

$$\begin{aligned} V_{n1} &= 0.2 * f_c * b * d / 1000 &= 154.0 \text{ Kips} \\ V_{n2} &= (480 + 0.08 * f_c) * b * d / 1000 &= 135.5 \text{ Kips} \\ V_{n3} &= 1600 * b * d / 1000 &= 246.4 \text{ Kips} \\ \text{Nominal Vertical Capacity (According to Cl.11.8.3.2.1 of ACI318),} \\ \Phi V_n &= \Phi * \text{MIN}(V_{n1}; V_{n2}; V_{n3}) &= 101.6 \text{ Kips} \\ \text{Vertical Load Capacity=} &= \text{IF}(V_u > \Phi V_n; \text{"Not Pass"}; \text{"Pass"}) &= \text{Pass} \end{aligned}$$

Determine Shear Friction Reinforcement (A_{vf})

Required Area of Reinforcement for Shear Friction (According to Cl.11.6.4.1 of ACI318),

$$A_{vf} = V_u \times 1000 / (\Phi \times f_y \times \mu) = 1.41 \text{ in}^2$$

Determine Direct Tension Reinforcement (A_n)

Minimum Horizontal Force on Corbel, $Nuc_min = 0.2 \times V_u = 17.8 \text{ Kips}$

Horizontal Force on Corbel, $Nuc_act = \text{MAX}(Nuc; Nuc_min) = 32.0 \text{ kips}$

Required Area of Reinforcement for Direct Tension (According to Cl.11.8.3.1 of ACI318),

$$A_n = Nuc_act \times 1000 / ((\Phi) * f_y) = 0.71 \text{ in}^2$$

Determine Flexural Reinforcement (A_f)

$$M_u = V_u * a_v + Nuc_act * (h - d) = 298.4 \text{ kip} \cdot \text{in}$$

Required Area of Reinforcement for Flexural (According to Cl.11.8.3.3 of ACI318),

$$A_f = M_u \times 1000 / (\Phi \times f_y \times 0.9 \times d) = 0.67 \text{ in}^2$$

Determine Primary Tension Reinforcement (A_{sc})

Required Area of Reinforcement for Primary Tension (According to Cl.11.8.3.5 of ACI318),

$$A_{sc} = \text{MAX}((2/3 * A_{vf}) + A_n; A_f + A_n) = 1.65 \text{ in}^2$$

Minimum Area of Reinforcement for Primary Tension (According to Cl.11.8.5 of ACI318),

$$A_{sc_min} = 0.04 * f_c / f_y * b * d = 0.51 \text{ in}^2$$
$$A_{sc_Req} = \text{MAX}(A_{sc}; A_{sc_min}) = 1.65 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.9}$$
$$\text{Provided Area of Bar Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 1.00 \text{ in}^2$$

Number of Provided Bars, $n = 2$

$$\text{Provided Area of Reinforcement, } A_{sc_Prov} = n * A_{sb} = 2.00 \text{ in}^2$$
$$\text{Check Validity=} = \text{IF}(A_{sc_Prov} \geq A_{sc_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$



Chapter 1: Concrete Design

Corbel Design

ACI 318

Page: 6

Determine Horizontal Reinforcement (A_h)

Required Area of Reinforcement for Horizontal Shear (According to Cl.11.8.4 of ACI318),

$$A_{h_Req} = 0.5 * (A_{sc_Prov} - A_n) = 0.65 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.3}$$

$$\text{Provided Area of Bar Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; A_{sb}; \text{Bar}=\text{Bar}) = 0.11 \text{ in}^2$$

$$\text{Number of Provided Bars, } n = 6$$

$$\text{Provided Area of Reinforcement, } A_{h_Prov} = n * A_{sb} = 0.66 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{h_Prov} \geq A_{h_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Distribute in two-thirds of Effective Corbel Depth adjacent to A_{sc}

Design Summary

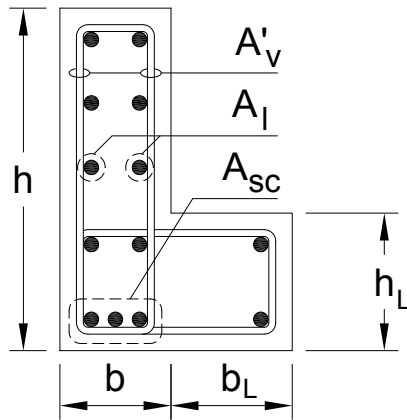
$$\text{Area of Reinforcement for Primary Tension } A_{sc} = A_{sc_Prov} = 2.00 \text{ in}^2$$

$$\text{Area of Reinforcement for Horizontal Shear, } A_h = A_{h_Prov} = 0.66 \text{ in}^2$$

Distribute in two-thirds of Effective Corbel Depth adjacent to A_{sc}



Design Precast Spandrel Beam for Combined Shear and Torsion as per ACI 318-11 Chapter 11



System

Width of Beam, b =	16.0 in
Height of Beam, h =	48.0 in
Width of Beam Ledge, b_L =	8.0 in
Height of Beam Ledge, h_L =	16.0 in
Concrete Cover, co =	2.50 in
Concrete Cover to Center of Stirrup, co' =	1.50 in
Effective Depth of Beam, $d = h - co$	= 45.50 in

Load

Ultimate Bending Moment, M_u =	1316.0 kip*ft
Ultimate Torsional Moment, T_u =	108.6 kip*ft
Ultimate Shear Force, V_u =	127.2 kips

Material Properties

Concrete Strength, f'_c =	5000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Yield Strength of Stirrups Reinforcement, f_{yt} =	60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ_s =	0.75
Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ_t =	0.90
Modification Factor for Lightweight Concrete, λ =	1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), $\mu = 1.4 * \lambda$	= 1.40



Determine Concrete Cracking Torque

Area Enclosed by Outside Perimeter of Spandrel Beam Including the Ledge,

$$A_{cp} = b * h + b_L * h_L = 896 \text{ in}^2$$

Outside Perimeter of Spandrel Beam Including the Ledge,

$$P_{cp} = 2 * (b + b_L + h) = 144 \text{ in}$$

$$\text{Concrete Cracking Torque, } T_{cr} = 4 * \lambda * \sqrt{f'_c} * \frac{A_{cp}^2}{P_{cp}} / 12000 = 131.4 \text{ kip*ft}$$

$$\text{Torsional Moment should be: IF}(T_u < \Phi_s * T_{cr} / 4; \text{"Neglected"; "Checked"}) = \text{Checked}$$

Calculation of Torsion Reinforcement

Area Enclosed by Centerline of The Outermost Closed Transverse Torsional Reinforcement (According to Cl.11.5.3.6 of ACI318),

$$A_{oh} = (h - 2 * co') * (b - 2 * co') + (b_L) * (h_L - 2 * co') = 689.0 \text{ in}^2$$

$$A_o = 0.85 * A_{oh} = 585.6 \text{ in}^2$$

Angle of Compression Diagonal Struts (According to 11.5.3.6 of ACI318),

$$\Theta = 45^\circ$$

Required Area for Torsion Shear per Stirrups Spacing (According to Eq. 11-20, 21 of ACI318),

$$A'_{vt} = \frac{T_u * 12000}{2 * \Phi_s * A_o * f_{yt} * (1 / \tan(\Theta))} = 0.025 \text{ in}^2 \text{ per in}$$

Calculation of Shear Reinforcement

Nominal Shear Strength Provided by Concrete (According to Eq.11-3 of ACI318),

$$V_c = 2 * \lambda * \sqrt{f'_c} * \frac{b * d}{1000} = 102.95 \text{ kips}$$

Nominal Shear Strength Provided by Reinforcement (According to Eq.11-2 of ACI318),

$$V_s = V_u / \Phi_s - V_c = 66.65 \text{ kips}$$

Required Area for Direct Shear per Stirrups Spacing (According to Eq. 11-1, 2 of ACI318),

$$A'_{vs} = \frac{V_s * 1000}{f_{yt} * d} = 0.024 \text{ in}^2 \text{ per in}$$



Calculation of Combined Shear and Torsion Reinforcement

Total Required Area for Torsion & Shear per Stirrups Spacing (According to Cl.11.5.3.8 of ACI318),

$$A'_v = \frac{A'_{vt} + A'_{vs}}{2} = 0.037 \text{ in}^2 \text{ per in per leg}$$

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.4

Provided Reinforcement, A_{sb} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.20 in²

Required Stirrups Spacing, s_{Req} = A_{sb}/A'_v = 5.41 in

Provided Stirrups Spacing, s_{Prov} = 5.00 in

Check Validity= IF($s_{Prov} \leq s_{Req}$; "Valid"; "Invalid") = Valid

Perimeter of Stirrups, Ph= $2 * (b - 2 * co' + h - 2 * co') + 2 * b_L$ = 132.00 in

Maximum Stirrups Spacing Due to Torsion (According to Cl.11.6.6 of ACI318),

s_{max_t} = MIN(Ph/8; 12) = 12.00 in

Maximum Stirrups Spacing Due to Shear (According to Cl.11.4.5 of ACI318),

s_{max_v} = MIN(d/2; 24) = 22.75 in

Maximum Stirrups Spacing, s_{max} = MIN(s_{max_t} ; s_{max_v}) = 12.00 in

Check Validity= IF($s_{Prov} \leq s_{max}$; "Valid"; "Invalid") = Valid

Calculation of Longitudinal Torsion Reinforcement

Required Area of Longitudinal Torsion Reinforcement (According to Cl.11.5.3.7 of ACI318),

$$A_{l_i} = \frac{A'_{vt} * Ph * \frac{f_{yt}}{\tan(\Theta)}}{\frac{f_y}{2}} = 3.30 \text{ in}^2$$

Minimum Area of Longitudinal Torsion Reinforcement (According to Eq.11-24 of ACI318),

$$A_{l_{min}} = \frac{5 * \sqrt{f'_c} * A_{cp}}{f_y} - A'_{vt} * Ph * \frac{f_{yt}}{f_y} = 1.98 \text{ in}^2$$

$A_{l_{Req}}$ = MAX(A_{l_i} ; $A_{l_{min}}$) = 3.30 in²

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.5

Provided Reinforcement, A_{sb} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.31 in²

Number of Bars, n= 12

Provided Longitudinal Reinforcement, $A_{l_{Prov}}$ = $A_{sb} * n$ = 3.72 in²

Check Validity= IF($A_{l_{Prov}} \geq A_{l_{Req}}$; "Valid"; "Invalid") = Valid



Calculation of Required Flexural Reinforcement

$$R_n = \frac{M_u * 12 * 1000}{\Phi_t * b * d^2} = 530 \text{ psi}$$

$$\rho = \frac{0.85 * f_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_n}{0.85 * f_c}} \right) = 0.0095$$

$$\text{Area of Flexural Reinforcement, } A_s = \rho * b * d = 6.92 \text{ in}^2$$

Calculation of Total Bottom Reinforcement at Mid-Span

Percentage of Torsional Reinforcement Concentrated on Bottom Side, Per = 16 %

Total Area of Bottom Reinforcement at Mid-Span,

$$A_{sc_Req} = A_{l_Req} * \text{Per} / 100 + A_s = 7.45 \text{ in}^2$$

Provided Reinforcement, Bar = SEL("ACI/Bar"; Bar;) = No.11

Provided Reinforcement, A_{sb} = TAB("ACI/Bar"; Asb; Bar=Bar) = 1.56 in²

Number of Bars, n = 5

$$\text{Total Area of Bottom Reinforcement, } A_{sc_Prov} = A_{sb} * n = 7.80 \text{ in}^2$$

Check Validity = IF($A_{sc_Prov} \geq A_{sc_Req}$; "Valid"; "Invalid") = Valid

Design Summary

Total Required Area for Torsion & Shear per Stirrups Spacing,

$$A'_v = A'_v = 0.037 \text{ in}^2 \text{ per in per leg}$$

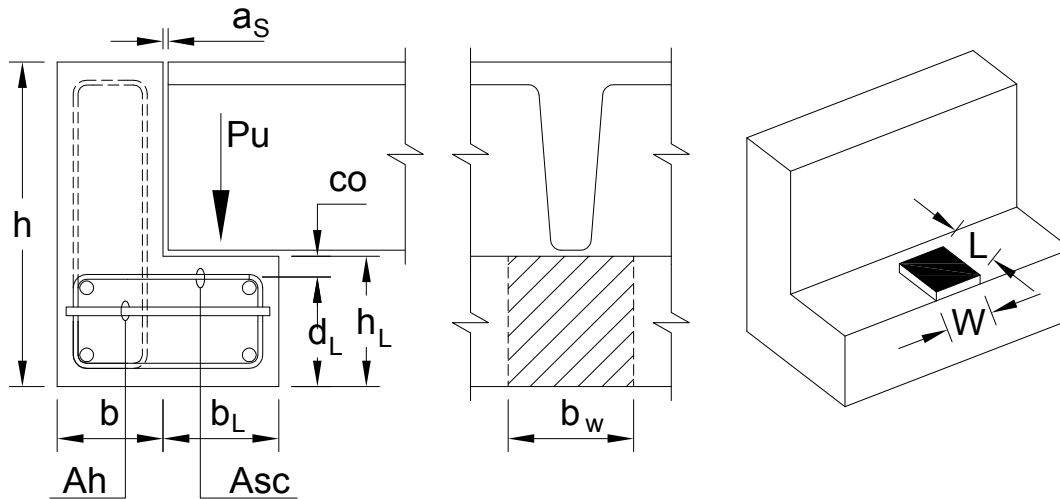
Provided Stirrups Spacing, $s_{Prov} = s_{Prov} = 5.00 \text{ in}$

Provided Longitudinal Reinforcement, $A_{l_Prov} = A_{l_Prov} = 3.72 \text{ in}^2$

Total Area of Bottom Reinforcement, $A_{sc_Prov} = A_{sc_Prov} = 7.80 \text{ in}^2$



Design of Beam Ledge as per ACI 318-11 Chapters 9 & 11



System

Width of Beam, b =			7.0 in
Height of Beam, h =			36.0 in
Width of Beam Ledge, b_L =			6.0 in
Height of Beam Ledge, h_L =			12.0 in
Concrete Cover, co =			1.25 in
Width of Bearing Pad, W =			4.5 in
Length of Bearing Pad, L =			4.5 in
Thickness of Bearing Pad, t_b =			0.3 in
Gap Spacing, a_s =			1.0 in
Shear Spacing, a_v =	$2/3 * L + a_s$	=	4.0 in
Flexural Spacing, a_f =	$a_v + co$	=	5.25 in
Effective Width According to Shear Requirements, b_{ws} =	$W + 4 * a_v$	=	20.5 in
Effective Width According to Flexural Requirements, b_{wf} =	$W + 5 * a_f$	=	30.8 in
Effective Depth of Beam Ledge, d_L =	$h_L - co$	=	10.75 in

Load

Dead Load, P_D =			11.0 kips
Live Load, P_L =			6.5 kips
Service Load, P =	$P_D + P_L$	=	17.5 kips
Ultimate Load, P_u =	$1.2 * P_D + 1.6 * P_L$	=	23.6 kips



Material Properties

Concrete Strength, f'_c =		5000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ_s =		0.75
Bearing Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ_b =		0.65
Modification Factor for Lightweight Concrete, λ =		1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), μ =	$1.4 * \lambda$	= 1.40
Maximum Service Load for Bearing Pads, q =		1000 psi

Check Bearing Plate Dimension

Capacity of Bearing Plate, B_p =	$W * L * q / 1000$	=	20.25 kips
Check Validity=	$IF(B_p > P, "Valid" ; "Increase Dimension")$	=	Valid

Check Concrete Bearing Strength

Bearing Strength of Concrete, ΦP_{nb} =	$\Phi_b * 0.85 * f'_c * L * W / 1000$	=	55.9 kips
Check Validity=	$IF(\Phi P_{nb} > P_u, "Valid" ; "Invalid")$	=	Valid

Check Maximum Nominal Shear-Transfer by Effective Section

Nominal Shear by Effective Section (According to Cl.11.9.3.2.1 of ACI318),			
V_{n1} =	$0.2 * f'_c * b_{ws} * d_L / 1000$	=	220.4 kips
V_{n2} =	$(480 + 0.08 * f'_c) * b_{ws} * d_L / 1000$	=	193.9 kips
V_{n3} =	$1600 * b_{ws} * d_L / 1000$	=	352.6 kips
ΦV_n =	$\Phi_s * \text{MIN}(V_{n1}; V_{n2}; V_{n3})$	=	145.4 kips
Check Validity=	$IF(\Phi V_n > P_u, "Valid" ; "Increase Dimension")$	=	Valid

Determine Shear Friction Reinforcement (A_{vf})

Required Reinforcement for Shear Friction (According to Cl.11.6.4.1 of ACI318),			
A_{vf} =	$P_u * 1000 / (\Phi_s * f_y * \mu)$	=	0.37 in ² per bws

Determine Direct Tension Reinforcement (A_n)

Required Reinforcement for Direct Tension (According to Cl.11.8.3.4 of ACI318),			
A_n =	$0.2 * P_u * 1000 / (\Phi_s * f_y)$	=	0.10 in ² per bwf

Determine Flexural Reinforcement (A_f)

M_u =	$P_u * a_f + 0.2 * P_u * (h_L - d_L)$	=	129.8 kip*in
Required Reinforcement for Flexural (According to Cl.11.8.3.3 of ACI318),			
A_f =	$M_u * 1000 / (\Phi_s * f_y * 0.8 * d_L)$	=	0.34 in ² per bwf



Chapter 1: Concrete Design

Beam Ledge Design

ACI 318

Page: 13

Determine Primary Tension Reinforcement (A_{sc})

Required Area of Reinforcement for Primary Tension (According to Cl.11.8.3.5 of ACI318),

$$A_{sc} = \text{MAX} (2/3 * A_{vf}/b_{ws} + A_n/b_{wf}; A_f/b_{wf} + A_n/b_{wf}) = 0.015 \text{ in}^2 \text{ per in}$$

Minimum Area of Reinforcement for Primary Tension (According to Cl.11.8.5 of ACI318),

$$A_{sc_min} = 0.04 * f'_c / f_y * d_L = 0.036 \text{ in}^2 \text{ per in}$$

$$A_{sc_req} = \text{MAX} (A_{sc}; A_{sc_min}) = 0.036 \text{ in}^2 \text{ per in}$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.5}$$

$$\text{Spacing between Bars, } s = 8.0 \text{ in}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.31 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{sb}/A_{sc_req} > s; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Determine Horizontal Reinforcement (A_h)

Required Area of Reinforcement for Horizontal Shear (According to Cl.11.8.4 of ACI318),

$$A_h = 0.5 * (A_{sc_req} - A_n / b_{wf}) = 0.016 \text{ in}^2 \text{ per in}$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.20 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{sb}/A_h > s; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Design Summary

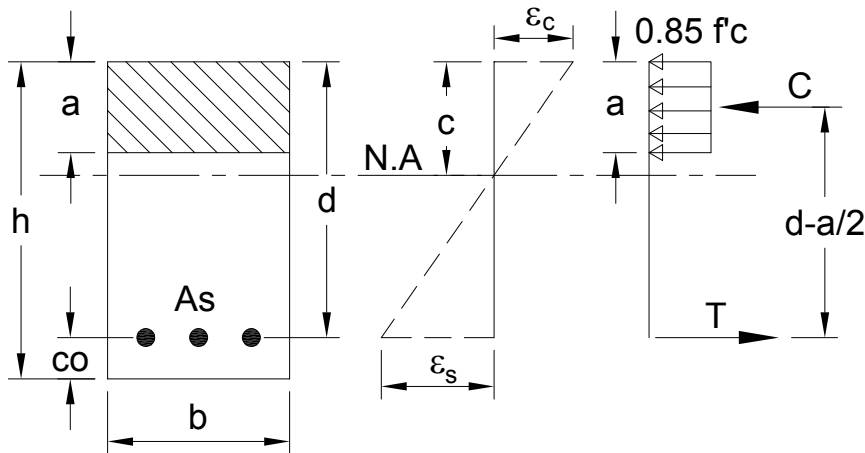
$$\text{Primary Tension Reinforcement, } A_{sc_req} = A_{sc_req} = 0.036 \text{ in}^2 \text{ per in}$$

$$\text{Horizontal Shear Reinforcement, } A_h = A_h = 0.016 \text{ in}^2 \text{ per in}$$

Distribute in two-thirds of Effective Ledge Depth adjacent to A_{sc}



Design of Rectangular Section with Tension Reinforcement only as per ACI 318-11 Chapters 9 & 10



System

Width of Concrete Section, b =	12.0 in
Depth of Concrete Section, h =	16.0 in
Concrete Cover, co =	2.5 in
Effective Depth of Concrete Section, $d = h - co = 16.0 - 2.5$	= 13.5 in

Load

Bending Moment due to Dead Load, M_D =	56.0 kip*ft
Bending Moment due to Live Load, M_L =	35.0 kip*ft
Ultimate Bending Moment, $M_U = (1.2 * M_D) + (1.6 * M_L)$	= 123.2 kip*ft

Material Properties

Concrete Strength, f'_c =	4000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.90
Factor for Rectangular Compressive Stress Block (According to Cl.10.2.7.3), β_1 =	IF ($f'_c \leq 4000$; 0.85; IF ($f'_c \geq 8000$; 0.65; $1.05 - 0.00005 * f'_c$)) = 0.85

Area of Reinforcement

R_n =	$\frac{M_U * 12000}{\Phi * b * d^2}$	= 751.1 psi
ρ =	$0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_n}{0.85 * f'_c}} \right)$	= 0.0143
Area of Reinforcement, A_s =	$\rho * b * d$	= 2.32 in ²



Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),

$$A_{s_min1} = \frac{3 * \sqrt{f'_c} * b * d}{f_y} = 0.51 \text{ in}^2$$

$$A_{s_min2} = \frac{200 * b * d}{f_y} = 0.54 \text{ in}^2$$

$$A_{s_min} = \text{MAX}(A_{s_min1}; A_{s_min2}) = 0.54 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{sc_Req} = \text{MAX}(A_s; A_{s_min}) = 2.32 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.10}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 1.27 \text{ in}^2$$

$$\text{Number of Bars, } n = 2$$

$$\text{Vertical Reinforcement, } A_{sc_Prov} = A_{sb} * n = 2.54 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{sc_Prov} \geq A_{sc_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Check Tension Controlled

$$\text{Depth of Rectangular Stress Block, } a = \frac{A_{sc_Prov} * f_y}{0.85 * f'_c * b} = 3.74 \text{ in}$$

$$\text{Distance from Extreme Compression Fiber to Neutral Axis, } c = a / \beta_1 = 4.40 \text{ in}$$

$$c/d = c / d = 4.40 / 13.5 = 0.326$$

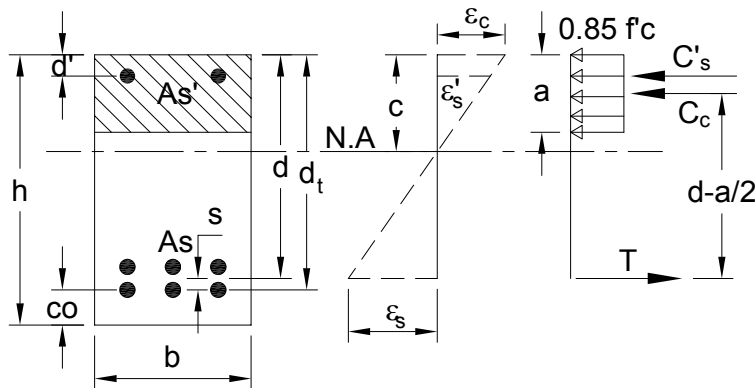
$$\text{IF}(c/d > 0.375; \text{"Add Com. RFT"}; \text{"Tension Controlled"}) = \text{Tension Controlled}$$

Design Summary

$$\text{Required Area of Reinforcement, } A_{sc} = A_{sc_Prov} = 2.54 \text{ in}^2$$



Design of Rectangular Section with Compression Reinforcement as per ACI 318-11 Chapters 9 & 10



System

Width of Concrete Section, $b =$	12.0 in
Depth of Concrete Section, $h =$	32.5 in
Concrete Cover, $co =$	2.5 in
Effective Depth of Concrete Section to Extreme Layer, $d_t = h - co = 32.5 - 2.5 =$	30.0 in
Distance between C.G of Tension Reinforcement and Extreme Layer, $s =$	1.2 in
Effective Depth of Concrete Section to C.G of Tension Reinforcement, $d = d_t - s =$	28.8 in
Depth of Compression Reinforcement, $d' =$	2.5 in

Load

Bending Moment due to Dead Load, $M_D =$	430.0 kip*ft
Bending Moment due to Live Load, $M_L =$	175.0 kip*ft
Ultimate Bending Moment, $M_U = (1.2 * M_D) + (1.6 * M_L) =$	796.0 kip*ft

Material Properties

Concrete Strength, $f'_c =$	4000 psi
Yield Strength of Reinforcement, $f_y =$	60000 psi
Modulus of Elasticity of Reinforcement, $E_s =$	29000000 psi
Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), $\Phi =$	0.90
Factor for Rectangular Compressive Stress Block (According to Cl.10.2.7.3), $\beta_1 = IF(f'_c \leq 4000; 0.85; IF(f'_c \geq 8000; 0.65; 1.05 - 0.00005 * f'_c)) =$	0.85



Check If Compression Reinforcement is Required

$\omega_t =$	$0.31875 * \beta_1$	=	0.271
$R_{nt} =$	$\omega_t * (1 - 0.59 * \omega_t) * f'_c$	=	910.7 pci
$R_n =$	$\frac{M_U * 12000}{\Phi * b * d_t^2}$	=	982.7 psi
Compression Reinforcement is: IF($R_n > R_{nt}$, "Required"; "Not Required")			= Required

Determine Required Moment Resisted by Compression Reinforcement

$\omega_t =$	$0.31875 * \beta_1$	=	0.271
$\rho_t =$	$0.31875 * f'_c * \beta_1 / f_y$	=	0.01806
$\rho =$	$\rho_t * d_t / d$	=	0.01881
$\omega =$	$\rho * f_y / f'_c$	=	0.28215
Moment Resisted by Tension RFT, $M_{nt} =$	$\omega * (1 - 0.59 * \omega) * \frac{f'_c * b * d^2}{12000}$	=	780.3 kip*ft
Moment Resisted by Compression RFT, $M'_n =$	$M_U / \Phi - M_{nt}$	=	104.1 kip*ft

Required Area of Compression Reinforcement

$d'/c_{limit} =$	$1 - \frac{f_y}{E_s * 0.003}$	=	0.31
$c_{limit} =$	$\left(1 - \frac{f_y}{E_s * 0.003}\right) * d_t$	=	9.3 in
$c_{cal} =$	$0.375 * d_t$	=	11.3 in
$d'/c_{cal} =$	$d' / (c_{cal})$	=	0.22
$f'_{si} =$	$\text{MIN}(0.003 * E_s * (1 - d'/c_{cal}); f_y)$	=	60000 psi
$f'_s =$	$\text{IF}(d'/c_{cal} \leq d'/c_{limit}; f_y; f'_{si})$	=	60000 psi
Required Reinforcement Area for Compression, $A'_s =$	$\frac{M'_n * 12000}{f'_s * (d - d')}$	=	0.79 in ²
Provided Reinforcement, Bar=	$\text{SEL}(\text{"ACI/Bar"}; \text{Bar};)$	=	No.6
Provided Reinforcement, $A_{sb} =$	$\text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar})$	=	0.44 in ²
Number of Bars, n=			2
Vertical Reinforcement, $A'_{s_Prov} =$	$A_{sb} * n$	=	0.88 in ²
Check Validity=	$\text{IF}(A'_{s_Prov} \geq A'_s; \text{"Valid"}; \text{"Invalid"})$	=	Valid
Required Reinforcement Area for Tension, $A_s =$	$A'_s + (\rho * b * d)$	=	7.29 in ²



Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),

$$A_{s_min1} = \frac{3 * \sqrt{f'_c} * b * d}{f_y} = 1.09 \text{ in}^2$$

$$A_{s_min2} = \frac{200 * b * d}{f_y} = 1.15 \text{ in}^2$$

$$A_{s_min} = \text{MAX}(A_{s_min1}; A_{s_min2}) = 1.15 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{sc_Req} = \text{MAX}(A_s; A_{s_min}) = 7.29 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.10}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 1.27 \text{ in}^2$$

$$\text{Number of Bars, } n = 6$$

$$\text{Vertical Reinforcement, } A_{sc_Prov} = A_{sb} * n = 7.62 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{sc_Prov} \geq A_{sc_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Design Summary

$$\text{Required Reinforcement Area for Compression, } A'_s = A'_{s_Prov} = 0.88 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{sc} = A_{sc_Prov} = 7.62 \text{ in}^2$$



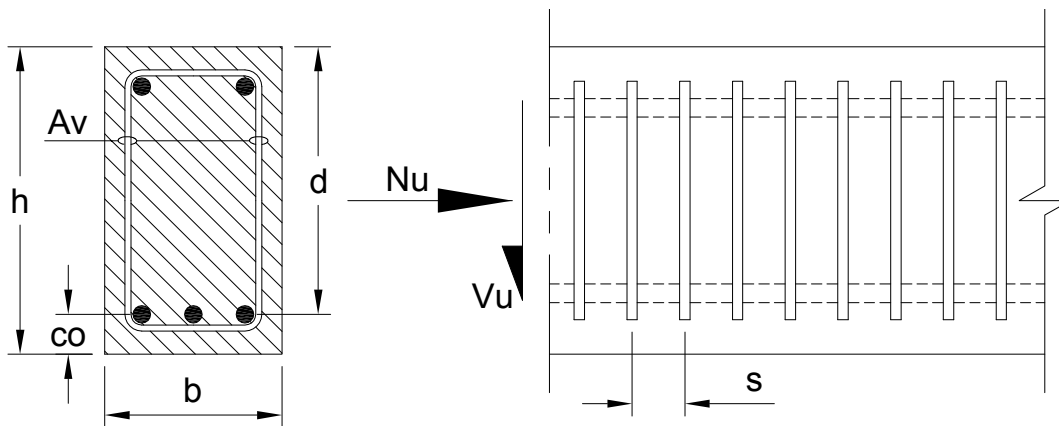
Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & N

ACI 318

Page: 19

Design of Shear Reinforcement for Section Subject to Shear & Axial Compression As per ACI318-11



System

Width of Concrete Section, b =		12.0 in
Depth of Concrete Section, h =		16.0 in
Concrete Cover, co =		2.25 in
Effective Depth of Concrete Section, d =	$h - co$	= 13.75 in

Load

Shear Force due to Dead Load, V_D =		10.0 kips
Shear Force due to Live Load, V_L =		5.0 kips
Ultimate Shear Force, V_u =	$(1.2 * V_D) + (1.6 * V_L)$	= 20.0 kips
Axial Compression Force due to Dead Load, N_D =		4.2 kips
Axial Compression Force due to Live Load, N_L =		3.1 kips
Ultimate Axial Compression Force, N_u =	$(1.2 * N_D) + (1.6 * N_L)$	= 10.0 kips

Material Properties

Concrete Strength, f'_c =		4000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =		0.75
Modification Factor for Lightweight Concrete, λ =		1.00



Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & N

ACI 318

Page: 20

Determine Concrete Shear Strength

Nominal Shear Strength provided by Concrete (According to Eq. 11-4 of ACI318),

$$V_c = 2 * \left(1 + \frac{N_u * 1000}{2000 * h * b} \right) * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 21.4 \text{ kips}$$

$$\text{Shear Reinforcement is : IF}(V_u > \Phi * V_c; \text{"Required"; "Not Required"}) = \text{Required}$$

Determine Area of Shear Reinforcement

Nominal Shear Strength provided by Reinforcement (According to Eq. 11-2 of ACI318),

$$V_s = \frac{V_u - \Phi * V_c}{\Phi} = 5.3 \text{ kips}$$

Maximum Allowable Shear Strength provided by Reinforcement (According to Cl.11.4.7.9 of ACI318),

$$V_{s_max} = 8 * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 83.5 \text{ kips}$$

$$\text{IF}(V_s > V_{s_max}; \text{"Increase Beam Dimension"; "OK"}) = \text{OK}$$

$$\text{Spacing of Provided Stirrups, } s = 6.75 \text{ in}$$

$$\text{Required Area of Reinforcement, } A_v = \frac{V_s * s * 1000}{f_y * d} = 0.04 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.11.4.6.3 of ACI318),

$$A_{v_min1} = \frac{0.75 * \sqrt{f'_c} * b * s}{f_y} = 0.06 \text{ in}^2$$

$$A_{v_min2} = \frac{50 * b * s}{f_y} = 0.07 \text{ in}^2$$

$$A_{v_min} = \text{MAX}(A_{v_min1}; A_{v_min2}) = 0.07 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{vc_Req} = \text{MAX}(A_v; A_{v_min}) = 0.07 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"; Bar; }) = \text{No.3}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"; Asb; Bar=Bar}) = 0.11 \text{ in}^2$$

$$\text{Number of Stirrups, } n = 1$$

$$\text{Provided Area of Reinforcement, } A_{vc_Prov} = A_{sb} * n * 2 = 0.22 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{vc_Prov} \geq A_{vc_Req}; \text{"Valid"; "Invalid"}) = \text{Valid}$$



Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & N

ACI 318

Page: 21

Determine Maximum Permissible Spacing of Stirrups

Allowable Shear Strength provided by Reinforcement for Spacing Limit (According to Cl.11.4.5.3 of ACI318),

$$V_{s_limit} = 4 * \lambda * \sqrt{f'_c} * b * d / 1000 = 41.7 \text{ kips}$$

$$\text{Factor for Maximum Spacing of Stirrups, } Fac = IF(V_s \leq V_{s_limit}; 1; 0.5) = 1.0$$

Maximum Spacing of Stirrups (According to Cl.11.4.5.1 of ACI318),

$$s_{max} = \text{MIN}(d/2; 24) * Fac = 6.88 \text{ in}$$

$$\text{Check Validity} = IF(s \leq s_{max}; "Valid"; "Invalid") = \text{Valid}$$

Design Summary

$$\text{Provided Area of Shear Reinforcement, } A_{vc_Prov} = A_{vc_Prov} = 0.22 \text{ in}^2$$

$$\text{Spacing of Stirrups, } s = s = 6.75 \text{ in}$$



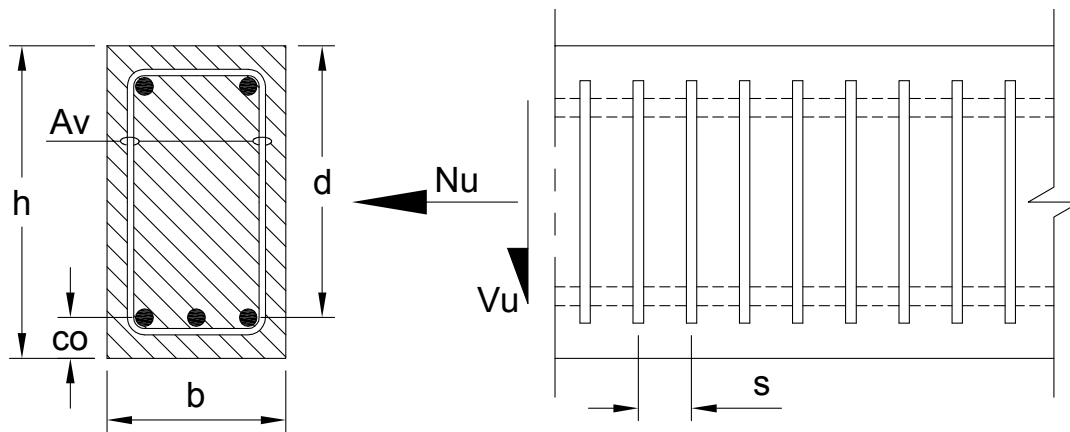
Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & T

ACI 318

Page: 22

Design of Shear Reinforcement for Section Subject to Shear & Axial Tension As per ACI318-11



System

Width of Concrete Section, b =	10.5 in
Depth of Concrete Section, h =	18.0 in
Concrete Cover, co =	2.0 in
Effective Depth of Concrete Section, $d = h - co$	= 16.0 in

Load

Shear Force due to Dead Load, V_D =	12.8 kips
Shear Force due to Live Load, V_L =	9.0 kips
Ultimate Shear Force, $V_u = (1.2 * V_D) + (1.6 * V_L)$	= 29.8 kips
Axial Tension Force due to Dead Load, N_D =	-2.0 kips
Axial Tension Force due to Live Load, N_L =	-15.2 kips
Ultimate Axial Tension Force, $N_u = (1.2 * N_D) + (1.6 * N_L)$	= -26.7 kips

Material Properties

Concrete Strength, f'_c =	3600 psi
Yield Strength of Reinforcement, f_y =	40000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	0.85

Determine Concrete Shear Strength

Nominal Shear Strength provided by Concrete (According to Eq. 11-8 of ACI318),

$$V_c = 2 * \left(1 + \frac{N_u * 1000}{500 * h * b} \right) * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 12.3 \text{ kips}$$

Shear Reinforcement is : IF ($V_u > \Phi * V_c$; "Required"; "Not Required") = Required



Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & T

ACI 318

Page: 23

Determine Area of Shear Reinforcement

Nominal Shear Strength provided by Reinforcement (According to Eq. 11-2 of ACI318),

$$V_s = \frac{V_u - \Phi * V_c}{\Phi} = 27.4 \text{ kips}$$

Maximum Allowable Shear Strength provided by Reinforcement (According to Cl.11.4.7.9 of ACI318),

$$V_{s_max} = 8 * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 68.5 \text{ kips}$$

$$\text{IF}(V_s > V_{s_max}; \text{"Increase Beam Dimension"}; \text{"OK"}) = \text{OK}$$

$$\text{Spacing of Provided Stirrups, } s = 5.0 \text{ in}$$

$$\text{Required Area of Reinforcement, } A_v = \frac{V_s * s * 1000}{f_y * d} = 0.21 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.11.4.6.3 of ACI318),

$$A_{v_min1} = \frac{0.75 * \sqrt{f'_c} * b * s}{f_y} = 0.06 \text{ in}^2$$

$$A_{v_min2} = \frac{50 * b * s}{f_y} = 0.07 \text{ in}^2$$

$$A_{v_min} = \text{MAX}(A_{v_min1}; A_{v_min2}) = 0.07 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{vc_Req} = \text{MAX}(A_v; A_{v_min}) = 0.21 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.3}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.11 \text{ in}^2$$

$$\text{Number of Stirrups, } n = 1$$

$$\text{Provided Area of Reinforcement, } A_{vc_Prov} = A_{sb} * n * 2 = 0.22 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{vc_Prov} \geq A_{vc_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Determine Maximum Permissible Spacing of Stirrups

Allowable Shear Strength provided by Reinforcement for Spacing Limit (According to Cl.11.4.5.3 of ACI318),

$$V_{s_limit} = 4 * \lambda * \frac{\sqrt{f'_c} * b * d}{1000} = 34.3 \text{ kips}$$

$$\text{Factor for Maximum Spacing of Stirrups, } Fac = \text{IF}(V_s \leq V_{s_limit}; 1; 0.5) = 1.0$$

Maximum Spacing of Stirrups (According to Cl.11.4.5.1 of ACI318),

$$S_{max} = \text{MIN}(d / 2; 24) * Fac = 8.00 \text{ in}$$

$$\text{Check Validity} = \text{IF}(s \leq S_{max}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Design Summary

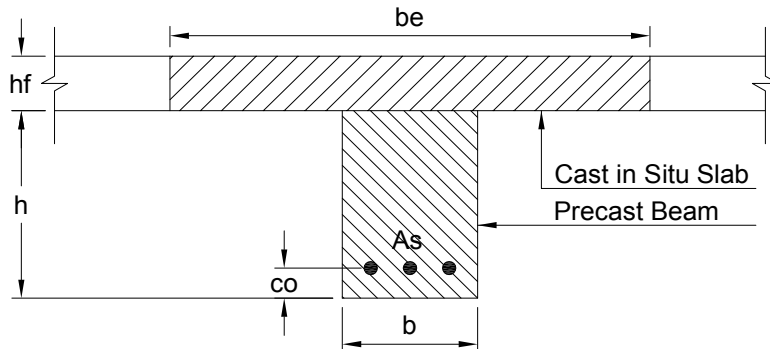
$$\text{Provided Area of Shear Reinforcement, } A_{vc_Prov} = A_{vc_Prov} = 0.22 \text{ in}^2$$

$$\text{Spacing of Stirrups, } s = 5.00 \text{ in}$$



Calculation of Deflection of Shored Nonprestressed Simple Support Concrete Composite Section

As per ACI318-11 Chapter 9



System

Beam Span, $L=$		26.0 ft
Beam Spacing, $S=$		8.0 ft
Width of Precast Beam, $b=$		12.0 in
Depth of Precast Beam, $h=$		20.0 in
Thickness of Cast in Situ Slab, $h_f=$		4.0 in
Area of Tension Reinforcement for Precast Beam, $A_s=$		3.00 in ²
Concrete Cover for Precast Beam, $co=$		2.5 in
Effective Width of Slab, $b_{e1}=$	$L*12 / 4$	= 78.0 in
Effective Width of Slab, $b_{e2}=$	$S*12$	= 96.0 in
Effective Width of Slab, $b_{e3}=$	$16*hf + b$	= 76.0 in
Effective Width of Slab, $b_e=$	$MIN(b_{e1}; b_{e2}; b_{e3})$	= 76.0 in

Material Properties

Concrete Strength of Cast in Situ Slab, $f'_{c1}=$		3000 psi
Concrete Strength of Precast Beam, $f'_{c2}=$		4000 psi
Yield Strength of Reinforcement, $f_y=$		40000 psi
Modulus of Elasticity of Reinforcement, $E_s=$		29000000 psi
Modification Factor for Lightweight Concrete, $\lambda=$		1.00
Concrete Density, $w_c=$		150 psi



Load

Superimposed Dead Load, SDL=		10.00 psf
Live Load, LL=		75.00 psf
Dead Load per Unit Length for Slab, w_{d1} =	$SDL * S + w_c * S * 12 * h_f / 144$	= 480.0 lb/ft
Dead Load per Unit Length for Beam, w_{d2} =	$w_c * b * h / 144$	= 250.0 lb/ft
Live Load per Unit Length, w_l =	$LL * S$	= 600.0 lb/ft
Percentage of Sustained Live Load, Sus=		20 %
Bending Moment of Dead Load 1, M_{D1} =	$1/1000 * w_{d1} * L^2 / 8$	= 40.6 kip*ft
Bending Moment of Dead Load 2, M_{D2} =	$1/1000 * w_{d2} * L^2 / 8$	= 21.1 kip*ft
Bending Moment of Live Load, M_L =	$1/1000 * w_l * L^2 / 8$	= 50.7 kip*ft
Bending Moment of Sustained Load, M_{sus} =	$M_{D1} + M_{D2} + (Sus/100) * M_L$	= 71.8 kip*ft

Calculation of Modular Ratio

For Cast in Situ Slab:

Modulus of Elasticity of Concrete (According to Cl. 8.5.1 of ACI318),

$$E_{c1} = w_c^{1.5} * 33 * \sqrt{f_{c1}} = 3320561 \text{ psi}$$

$$\text{Modulus of rupture (According to Eq. 9-10 of ACI318), } f_{r1} = 7.5 * \lambda * \sqrt{f_{c1}} = 411 \text{ psi}$$

For Precast Beam:

Modulus of Elasticity of Concrete (According to Cl. 8.5.1 of ACI318),

$$E_{c2} = w_c^{1.5} * 33 * \sqrt{f_{c2}} = 3834254 \text{ psi}$$

$$\text{Modulus of rupture (According to Eq. 9-10 of ACI318), } f_{r2} = 7.5 * \lambda * \sqrt{f_{c2}} = 474 \text{ psi}$$

$$n_c = E_{c2} / E_{c1} = 1.15$$

$$n_s = E_s / E_{c2} = 7.56$$

$$\text{Width of Slab considering relative Concrete Strength, } bs = be / n_c = 66.09 \text{ in}$$

Calculation of Moment of Inertia for Cracked Section

For Precast Beam

$$\text{Effective Depth of Section, } d = 17.5 \text{ in}$$

$$I_{g1} = b * h^3 / 12 = 8000 \text{ in}^4$$

$$B = b / (n_s * A_s) = 0.53 \text{ 1/in}$$

$$kd = \frac{\sqrt{2 * d * B + 1} - 1}{B} = 6.5 \text{ in}$$

$$I_{cr1} = \frac{b * kd^3}{3} + n_s * A_s * (d - kd)^2 = 3842.8 \text{ in}^4$$



Chapter 1: Concrete Design

Deflection of Shored Composite Section

ACI 318

Page: 26

For Composite Section

$$\text{Effective Depth of Section, } d = (h + hf) - c_o = 21.5 \text{ in}$$

$$h_1 = h + hf = 24.0 \text{ in}$$

$$bs_1 = bs - b = 54.1 \text{ in}$$

Distance from Centroidal Axis of Gross Section to Tension Face,

$$y_t = h_1 \frac{1}{2} \frac{bs_1 hf^2 + b h_1^2}{bs_1 hf + b h_1} = 16.3 \text{ in}$$

$$I_{g2} = \frac{bs_1 hf^3}{12} + \frac{b h_1^3}{12} + bs_1 hf \left(h + \frac{hf}{2} - y_t \right)^2 + b h_1 \left(y_t - \frac{h_1}{2} \right)^2 = 26468.49 \text{ in}^4$$

$$B = bs / (n_s \cdot A_s) = 2.91 \text{ 1/in}$$

$$kd = \frac{\sqrt{2 \cdot d \cdot B + 1} - 1}{B} = 3.5 \text{ in}$$

$$I_{cr2} = \frac{bs \cdot kd^3}{3} + n_s \cdot A_s \cdot (d - kd)^2 = 8292.9 \text{ in}^4$$

$$\text{Ratio between Cracking \& Gross Inertia, } r = \left(\frac{I_{g1}}{I_{g2}} + \frac{I_{cr1}}{I_{cr2}} \right) / 2 = 0.383$$

Cracking Moment (According to Eq. 9-9 of ACI318),

$$\text{Cracking Moment for Beam Section, } M_{cr1} = \frac{f_{r2} \cdot I_{g1}}{h/2 \cdot 12000} = 31.60 \text{ kip}\cdot\text{ft}$$

$$\text{Cracking Moment for Beam Section, } M_{cr2} = \frac{f_{r2} \cdot I_{g2}}{y_t \cdot 12000} = 64.14 \text{ kip}\cdot\text{ft}$$

Effective Moment of Inertia for Composite Section,

$$I_{e1,2} = \left(\frac{M_{cr1}}{M_{D1} + M_{D2}} \right)^3 \cdot I_{g1} + \left(1 - \left(\frac{M_{cr1}}{M_{D1} + M_{D2}} \right)^3 \right) \cdot I_{cr1} = 4401 \text{ in}^4$$

$$I_{ed,l} = \left(\frac{M_{cr2}}{M_{D1} + M_{D2} + M_L} \right)^3 \cdot I_{g2} + \left(1 - \left(\frac{M_{cr2}}{M_{D1} + M_{D2} + M_L} \right)^3 \right) \cdot I_{cr2} = 11670 \text{ in}^4$$

$$\text{Check Validity} = \text{IF}(I_{e1,2} < I_{g1}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Short Term Deflection

Short Term Deflection of composite section Due to Dead Load,

$$\Delta_{1,2} = \frac{5 \cdot (M_{D1} + M_{D2}) \cdot L^2 \cdot 12^3}{48 \cdot E_{c2} \cdot I_{g2} / 1000} = 0.074 \text{ in}$$



Chapter 1: Concrete Design

Deflection of Shored Composite Section

ACI 318

Page: 27

Deflection Due to Shrinkage

$$\text{For Simple Span, } K_{sh} = 0.125$$

$$\rho = \frac{A_s * 100}{b * d} = 1.16 \%$$

$$\text{(According to Fig.10-3 of PCA Note on ACI318), } A_{sh} = 0.789$$

$$\text{Time Dependant Shrinkage Strain, } \epsilon_{sh} = 400 * 10^{-6} = 0.00040$$

$$\text{Deflection Due to Shrinkage, } \Delta_{sh} = 0.64 * K_{sh} * A_{sh} * \epsilon_{sh} * L^2 * 12^2 * r/h = 0.047 \text{ in}$$

Deflection Due to Creep

$$\text{For No Compression Reinforcement Factor of, } k_r = 0.85$$

$$\text{Average Creep Coefficient (According to Cl.2.3.4 of ACI435), } C_u = 1.67$$

$$\text{Deflection Due to Creep, } \Delta_{cp} = C_u * \Delta_{i1,2} * k_r = 0.105 \text{ in}$$

Deflection Due to Live Load

$$\text{Deflection Due to Live Load, } \Delta_L = \frac{5 * (M_{D1} + M_{D2} + M_L) * L^2 * 12^3}{48 * E_{c2} * I_{ed,l} / 1000} * \Delta_{i1,2} = 0.232 \text{ in}$$

$$\text{Deflection Due to Creep Sustained Live Load, } \Delta_{cp,L} = C_u * \frac{C_{sus}}{100} * \Delta_L * k_r = 0.066 \text{ in}$$

Total Long Term Deflection

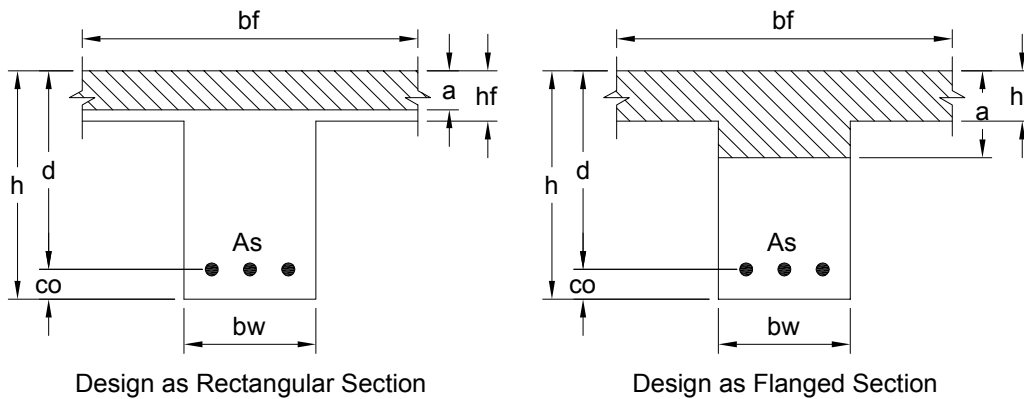
$$\text{Total Deflection, } \Delta_u = \Delta_{i1,2} * 3.53 + \Delta_{sh} + \Delta_{cp} + \Delta_L = 0.65 \text{ in}$$

Calculation Summary

$$\text{Total Deflection, } \Delta_u = \Delta_{i1,2} * 3.53 + \Delta_{sh} + \Delta_{cp} + \Delta_L = 0.65 \text{ in}$$



Design of Flanged Section with Tension Reinforcement only as per ACI 318-11 Chapters 9 & 10



System

Width of Concrete Flange, b_f =	30.0 in
Width of Concrete Web, b_w =	10.0 in
Depth of Concrete Section, h =	20.0 in
Thickness of Top Flange, h_f =	2.5 in
Concrete Cover, co =	1.0 in
Effective Depth of Concrete Section, $d = h - co = 20.0 - 1.0$	= 19.0 in

Load

Bending Moment due to Dead Load, M_D =	72.0 kip*ft
Bending Moment due to Live Load, M_L =	196.0 kip*ft
Ultimate Bending Moment, $M_U = (1.2 * M_D) + (1.6 * M_L)$	= 400.0 kip*ft

Material Properties

Concrete Strength, f'_c =	4000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.90
Factor for Rectangular Compressive Stress Block (According to Cl.10.2.7.3 of ACI318), β_1 =	$IF(f'_c \leq 4000; 0.85; IF(f'_c \geq 8000; 0.65; 1.05 - 0.00005 * f'_c)) = 0.85$



Chapter 1: Concrete Design

Flexural Design of Flanged Section

ACI 318

Page: 29

Design as Flanged Section

$$\text{Compressive Strength of Flange, } C_f = 0.85 * f'_c * h_f * \frac{b_f - b_w}{1000} = 170.0 \text{ kips}$$

$$\text{Area of Reinforcement for Flange in Compression, } A_{sf} = \frac{C_f}{f_y} * 1000 = 2.83 \text{ in}^2$$

$$\text{Nominal Moment for Flange, } M_{nf} = \frac{A_{sf} * f_y}{12000} * \left(d - \frac{h_f}{2} \right) = 251.2 \text{ kip*ft}$$

$$\text{Nominal Moment for Web, } M_{nw} = M_U / \Phi - M_{nf} = 193.24 \text{ kip*ft}$$

$$R_{nw} = \frac{M_{nw} * 12000}{\Phi * b_w * d^2} = 713.7 \text{ psi}$$

$$\rho_w = 0.85 * f'_c / f_y * \left(1 - \sqrt{1 - \frac{2 * R_{nw}}{0.85 * f'_c}} \right) = 0.0135$$

$$\text{Area of Reinforcement for Web in Compression, } A_{sw} = \rho_w * b_w * d = 2.56 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{s_T} = A_{sf} + A_{sw} = 5.39 \text{ in}^2$$

$$\text{Depth of Rectangular Stress Block for Web, } a_w = \frac{A_{sw} * f_y}{0.85 * f'_c * b_w} = 4.52 \text{ in}$$

Design as Rectangular Section

$$R_n = \frac{M_U * 12000}{\Phi * b_f * d^2} = 492.46 \text{ psi}$$

$$\rho = 0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_n}{0.85 * f'_c}} \right) = 0.0089$$

$$\text{Area of Reinforcement, } A_{s_R} = \rho * b_f * d = 5.07 \text{ in}^2$$

$$\text{Depth of Rectangular Stress Block, } a = \frac{A_{s_R} * f_y}{0.85 * f'_c * b_f} = 2.98 \text{ in}$$



Section Type and Reinforcement

Section Design as: IF($a > h_f$; "Flanged Sec."; "Rectangular Sec.") = Flanged Sec.

Area of Reinforcement, A_s = IF($a > h_f$; A_{s_T} ; A_{s_R}) = 5.39 in²

Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),

$A_{s_min1} = \frac{3 * \sqrt{f'_c} * b_f * d}{f_y} = 1.80 \text{ in}^2$

$A_{s_min2} = \frac{200 * b_f * d}{f_y} = 1.90 \text{ in}^2$

$A_{s_min} = \text{MAX}(A_{s_min1}; A_{s_min2}) = 1.90 \text{ in}^2$

Required Area of Reinforcement, $A_{sc_Req} = \text{MAX}(A_s; A_{s_min}) = 5.39 \text{ in}^2$

Provided Reinforcement, Bar = SEL("ACI/Bar"; Bar;) = No.10

Provided Reinforcement, $A_{sb} = \text{TAB}("ACI/Bar"; Asb; Bar=Bar) = 1.27 \text{ in}^2$

Number of Bars, n = 5

Vertical Reinforcement, $A_{sc_Prov} = A_{sb} * n = 6.35 \text{ in}^2$

Check Validity = IF($A_{sc_Prov} \geq A_{sc_Req}$; "Valid"; "Invalid") = Valid

Check Tension Controlled

Distance from Extreme Compression Fiber to Neutral Axis,

c = IF($a > h_f$; a_w / β_1 ; a / β_1) = 5.32 in

c/d = c / d = 5.32 / 19.0 = 0.280

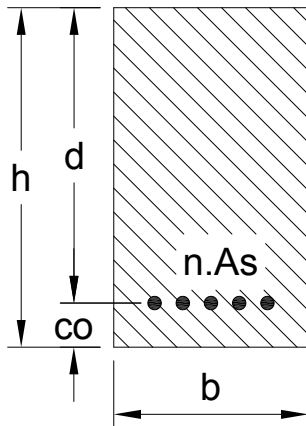
IF($c/d > 0.375$; "Add Com. RFT"; "Tension Controlled") = Tension Controlled

Design Summary

Required Area of Reinforcement, $A_{sc} = A_{sc_Prov} = 6.35 \text{ in}^2$



Cracking Moment Strength for Prestressed Sections as per ACI 318-11 Chapter 18



System

Width of Concrete Section, b =		12.0 in
Depth of Concrete Section, h =		24.0 in
Concrete Cover, co =		2.0 in
Effective Depth of Concrete Section, $d = h - co = 24.0 - 2.0$	=	22.0 in
Number of Strands, n =		6.0
Area of One Strand, A_s =		0.153 in ²

Material Properties

Concrete Strength, f'_c =		5000 psi
Tensile Strength of Prestressed Steel, f_{pu} =		270000 psi
Jacking Stress, $J_s = 0.7 * f_{pu}$	=	189000 psi
Percentage of Losses, L_s =		20.00 %
Modification Factor for Lightweight Concrete, λ =		1.00
Modulus of Rupture (According to Eq. 9-10 of ACI318), $f_r = 7.5 * \lambda * \sqrt{f'_c}$	=	530 psi

Calculation of Cracking Moment Strength

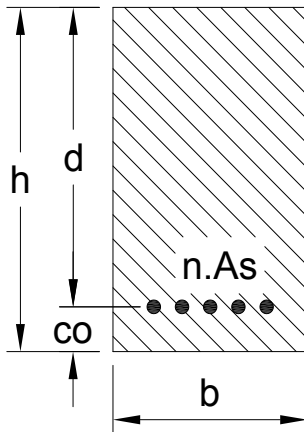
Area of Concrete, $A_c = b * h$		= 288.0 in ²
Concrete Section Modulus, $S_b = b * h^2 / 6$		= 1152.0 in ³
Eccentricity of Prestressing, $e = h/2 - co$		= 10.0 in
Effective Prestress Force, $P_{se} = (1 - L_s/100) * n * A_s * J_s / 1000$		= 138.8 kips
Cracking Moment Strength, $M_{cr} = \left(\frac{f_r}{1000} + \frac{P_{se}}{A_c} \right) * \frac{S_b}{12} + P_{se} * \frac{e}{12}$		= 212.8 kip*ft

Calculation Summary

Cracking Moment Strength, $M_{cr} = M_{cr}$		= 212.8 kip*ft
---	--	----------------



Flexural Strength of Prestressed Member Using Approximate Value of f_{ps} As per ACI 318-11



System

Width of Concrete Section, b =	12.0 in
Depth of Concrete Section, h =	24.0 in
Concrete Cover, co =	2.0 in
Effective Depth of Concrete Section, $d = h - co = 24.0 - 2.0$	= 22.0 in
Number of Strands, n =	6
Area of One Strand, A_s =	0.153 in ²

Material Properties

Concrete Strength, f'_c =	5000 psi
Tensile Strength of Prestressed Steel, f_{pu} =	270000 psi
Yield Strength of Prestressed Steel, $f_{py} = 0.9 * f_{pu}$	= 243000 psi
Factor for Type of Prestressing Steel (According to Cl.18.7.2 of ACI318), γ_p =	0.28
Factor for Rectangular Compressive Stress Block (According to Cl.10.2.7.3 of ACI318), $\beta_1 = IF(f'_c \leq 4000; 0.85; IF(f'_c \geq 8000; 0.65; 1.05 - 0.00005 * f'_c))$	= 0.80



Chapter 1: Concrete Design

Flexural Strength of Prestressed Member

ACI 318

Page: 33

Calculation of Stress for Prestressed Reinforcement

$$\text{Prestressed Reinforcement Ratio, } \rho_p = n * A_s / (b * d) = 0.00348$$

Prestressing Force (According to Eq. 18-1 of ACI318),

$$f_{ps} = \frac{f_{pu}}{1000} * \left(1 - \frac{\gamma_p}{\beta_1} * \rho_p * \frac{f_{pu}}{f_c} \right) = 252 \text{ ksi}$$

Calculation of Nominal Moment Strength

$$\text{Distance of Compression Block, } a = \frac{n * A_s * f_{ps}}{0.85 * b * f_c / 1000} = 4.54 \text{ in}$$

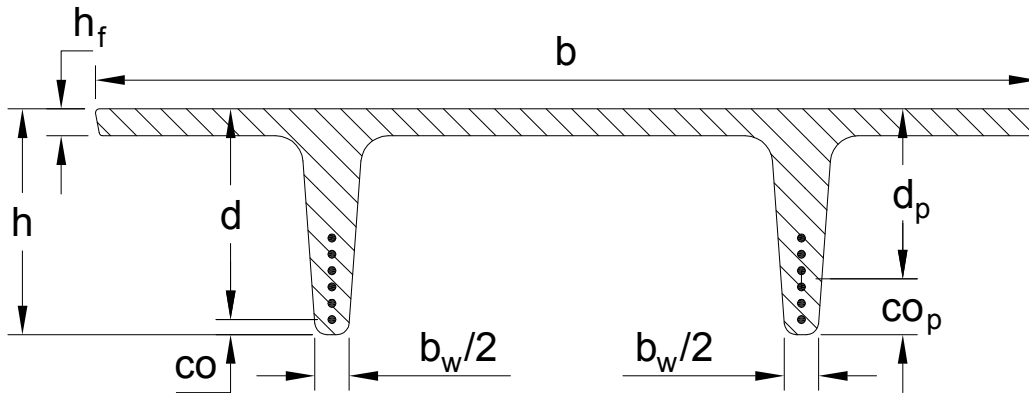
$$\text{Nominal Moment Strength, } M_n = \frac{n * A_s * f_{ps}}{12} * \left(d - \frac{a}{2} \right) = 380.4 \text{ kip*ft}$$

Calculation Summary

$$\text{Nominal Moment Strength, } M_n = M_n = 380.4 \text{ kip*ft}$$



Tension Controlled Limit for Prestressed Flexural Member as per ACI 318-11 Chapters 10 & 18



System

Width of Concrete Double Tee Section, $b=$		84.0 in
Width of Web of Concrete Double Tee Section, $b_w=$		15.5 in
Depth of Concrete Double Tee Section, $h=$		32.0 in
Thickness of Concrete Top Slab, $h_f=$		2.0 in
Concrete Cover, $co=$		2.0 in
Concrete Cover to CG of Prestressed Steel, $co_p=$		4.5 in
Effective Depth of Concrete Section, $d=$	$h - co$	$= 30.0$ in
Effective Depth of Concrete Section, $d_p=$	$h - co_p$	$= 27.5$ in
Number of Strands, $n=$		22.0
Area of One Strand, $A_s=$		0.153 in ²

Material Properties

Concrete Strength, $f'_c=$		5000 psi
Tensile Strength of Prestressed Steel, $f_{pu}=$		270000 psi
Yield Strength of Prestressed Steel, $f_{py}=$	$0.9 * f_{pu}$	$= 243000$ psi
Factor for Type of Prestressing Steel (According to Cl.18.7.2 of ACI318), $\gamma_p=$		0.28
Factor for Rectangular Compressive Stress Block (According to Cl.10.2.7.3 of ACI318),		
$\beta_1=$	$IF(f'_c \leq 4000; 0.85; IF(f'_c \geq 8000; 0.65; 1.05 - 0.00005 * f'_c))$	$= 0.80$



Calculation of Stress in Prestressed Reinforcement

$$\omega_{pu} = \frac{(n * A_s) * f_{pu}}{(b * d_p * f_c)} = 0.079$$

Prestressing Force (According to Eq.18-1 of ACI318),

$$f_{ps} = f_{pu} * \left(1 - \frac{\gamma_p}{\beta_1} * \omega_{pu} \right) = 262535 \text{ psi}$$

Area of Reinforcement for Compression in Flange,

$$A_{pf} = \frac{0.85 * h_f * f_c * (b - b_w)}{f_{pu}} = 2.16 \text{ in}^2$$

Calculation of Depth of Concrete Stress Block

$$a_i = \frac{(n * A_s) * f_{ps}}{(0.85 * b * f_c)} = 2.48 \text{ in}$$

For $a_i > h_f$:

$$a_1 = \frac{(n * A_s - A_{pf}) * f_{ps}}{(0.85 * b_w * f_c)} = 4.81 \text{ in}$$

For $a_i \leq h_f$:

$$a_2 = a_i = 2.48 \text{ in}$$

$$a = \text{IF}(a_i > h_f ; a_1 ; a_2) = 4.81 \text{ in}$$

$$c = \frac{a}{\beta_1} = 6.01 \text{ in}$$

Check Tension Controlled

$$c/d = \frac{c}{d} = 0.200$$

$$\text{IF}(c/d > 0.375; \text{"Compression Controlled"}; \text{"Tension Controlled"}) = \text{Tension Controlled}$$

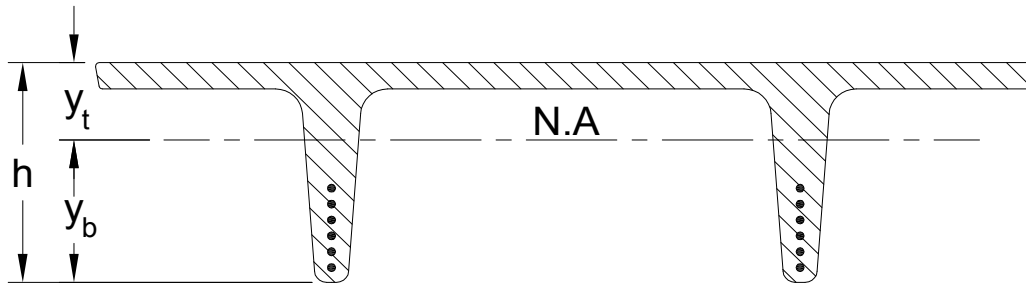
Calculation Summary

Type of Section:

$$\text{IF}(c/d > 0.375; \text{"Compression Controlled"}; \text{"Tension Controlled"}) = \text{Tension Controlled}$$



Estimating Prestress Losses as per ACI 318-11 Chapter 18



System

Area of Concrete Section, A_c =	449 in ²
Depth of Concrete Section, h =	24 in
Concrete Cover, co =	2 in
Effective Depth of Concrete Section, d = $h - co$	= 22 in
Moment of Inertia for Concrete Section, I_c =	22469 in ⁴
Distance from Bottom Fiber to Neutral Axis, y_b =	17.77 in
Distance from Top Fiber to Neutral Axis, y_t = $h - y_b$	= 6.23 in
Number of Strands, n =	8.0
Area of One Strand, A_s =	0.153 in ²
Eccentricity of Strands, e =	9.77 in
Volume per Surface Area, $V.S$ =	1.35 in
Average Relative Humidity, RH =	75.00 %

Load

Factored Moment due to Dead Load, M_D =	1617 kip*in
Factored Moment due to Superimposed Dead Load, M_{SD} =	691 kip*in
Factored Moment due to Live Load, M_L =	1382.00 kip*in



Material Properties

Concrete Strength, f_{ci} =		3500 psi
Concrete Strength, f_c =		5000 psi
Tensile Strength of Prestressed Steel, f_{pu} =		270000 psi
Yield Strength of Prestressed Steel, f_{py} =	$0.9 * f_{pu}$	= 243000 psi
Jacking Stress, J_s =	$0.74 * f_{pu}$	= 199800 psi
Modification Factor for Lightweight Concrete, λ =		1.00
Modulus of Rupture (According to Eq. 9-10 of ACI318), f_r =	$7.5 * \lambda * \sqrt{f_c}$	= 530 psi
Concrete Density, w_c =		150 psi
Modulus of Elasticity of Concrete (According to Cl. 8.5.1 of ACI318),		
Modulus of Elasticity for Initial Concrete, E_{ci} =	$w_c^{1.5} * 33 * \sqrt{f_{ci}}$	= 3586616 psi
Modulus of Elasticity for Concrete, E_c =	$w_c^{1.5} * 33 * \sqrt{f_c}$	= 4286826 psi
Modulus of Elasticity of Prestressed Steel, E_s =		28500000 psi

Calculation of Losses

1- Elastic Shortening of Concrete (ES)

Initial Force of Prestress, P_{pi} =	$J_s * (n * A_s) / 1000$	= 244.6 kips
Prestress Type=	SEL("ACI/Kes" ;Type;)	= Pretensioned
K_{es} =	TAB("ACI/Kes" ;Kes ;Type=Type)	= 1.00
K_{cir} =	TAB("ACI/Kcir" ;Kcir ;Type=Type)	= 0.90
f_{cir} =	$K_{cir} * \left(\frac{P_{pi}}{A_c} + \frac{P_{pi}}{I_c} * e^2 \right) - \frac{M_D * e}{I_c}$	= 0.722 ksi
Elastic Shortening of Concrete, ES=	$K_{es} * E_s * f_{cir} / E_{ci}$	= 5.74 ksi

2- Creep of Concrete (CR)

Prestress Type=	SEL("ACI/Kcr" ;Type;)	= Pretensioned
Factor of, K_{cr} =	TAB("ACI/Kcr" ;Kcr ;Type=Type)	= 2.00
Creep Losses, CR=	$K_{cr} * \frac{E_s}{E_c} * \left(f_{cir} - M_{SD} * \frac{e}{I_c} \right)$	= 5.61 ksi

3- Shrinkage of Concrete (SH)

Prestress Type=	SEL("ACI/Ksh" ;Type;)	= Pretensioned
Factor of, K_{sh} =	TAB("ACI/Ksh" ;Ksh ;Type=Type)	= 1.00
Shrinkage Losses, SH=	$8.2 * 10^{-6} * K_{sh} * \frac{E_s}{1000} * (1 - 0.06 * V.S) * (100 - RH)$	= 5.37 ksi



Chapter 1: Concrete Design

Prestress Losses

ACI 318

Page: 38

4- Relaxation of Tendon (RE)

Prestress Type= SEL("ACI/KreJ" ;Type;) = relaxation strand-Grade Low 270

Factor of, K_{re} = TAB("ACI/KreJ" ;Kre ;Type=Type) = 5000 psi

Factor of, J= TAB("ACI/KreJ" ;J ;Type=Type) = 0.04

Ratio of f_{pi}/f_{pu} , r= SEL("ACI/r" ;r;) = 0.74

Factor of, C= TAB("ACI/r" ;C ;r=r) = 0.95

Relaxation of Tendon, RE= $\left(\frac{K_{re}}{1000} - J * (SH + CR + ES) \right) * C$ = 4.11 ksi

5- Total Allowance of Losses and Effective Prestress Force after all Losses

Total Allowance of Losses, L_s = ES + CR + SH + RE = 21 ksi

Effective Prestress Stress, f_{se} = $J_s / 1000 - L_s$ = 179 ksi

Effective Prestress Force after All Losses, P_e = $f_{se} * (n * A_s)$ = 219 kips

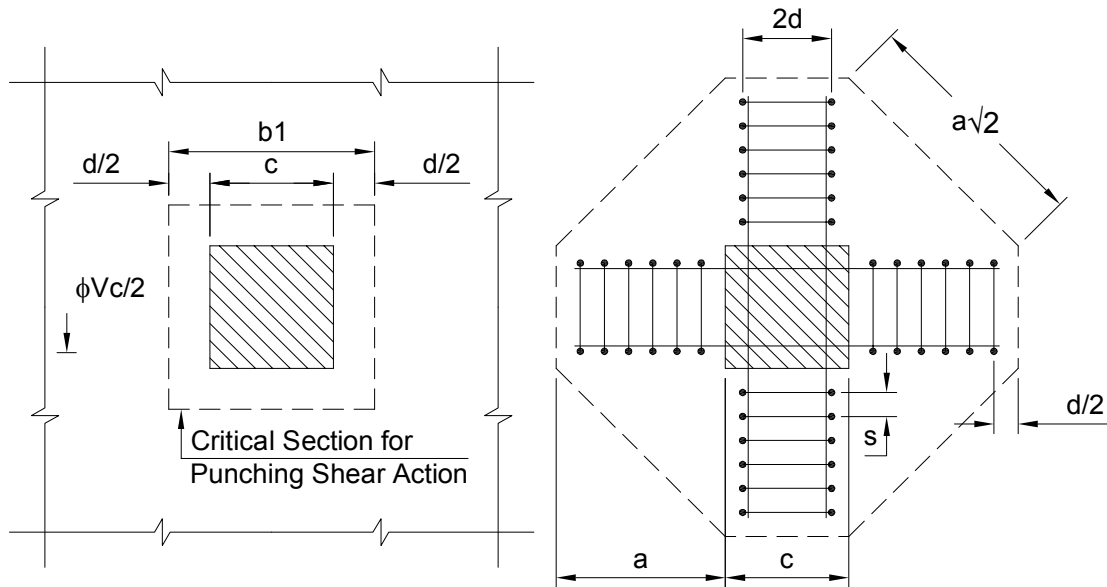
Calculation Summary

Total Allowance of Losses, L_s = L_s = 21 ksi

Effective Prestress Force after All Losses, P_e = P_e = 219 kips



**Design Shear Reinforcement for Slab which to resist Punching Stress around Interior Square Column
As per ACI318-11 Chapter 11**



System

Column Dimension, c =			12.0 in
Thickness of Concrete Slab, h =			7.5 in
Concrete Cover, co =			1.5 in
Effective Depth of Concrete Section, d =	$h - co = 7.5 - 1.5$	=	6.0 in
Bar Diameter of Shear Reinforcement, Dia =			0.375 in

Load

Ultimate Shear Force, V_u =			120.0 kips
-------------------------------	--	--	------------

Material Properties

Concrete Strength, f'_c =			4000 psi
Yield Strength of Reinforcement, f_y =			60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =			0.75
Modification Factor for Lightweight Concrete, λ =			1.00

Determine Concrete Shear Strength

b_1 =	$c + d$	=	18.0 in
Perimeter of Critical Section, b_0 =	$4 * b_1$	=	72.0 in
Nominal Shear Strength provided by Concrete (According to Eq. 11-33 of ACI318),			
V_c =	$4 * \lambda * \sqrt{f'_c} * b_0 * d / 1000$	=	109.3 kips
Punching Shear Reinforcement is :	IF ($V_u > \Phi * V_c$;"Required";"Not Required")	=	Required



Chapter 1: Concrete Design

Punching Shear Reinforcement on Slab

ACI 318

Page: 40

Determine Area of Shear Reinforcement

Minimum Effective Depth of Slab with Shear Reinforcement (According to Cl.11.11.3 of ACI318),

$$d_{\min} = \text{MIN}(6; 16 * \text{Dia}) = 6.0 \text{ in}$$

$$\text{Effective Depth of Slab : IF}(d > d_{\min}; \text{"Should Increase"}; \text{"OK"}) = \text{OK}$$

Maximum Shear Strength of Slab with Shear Reinforcement (According to Cl.11.11.3.2 of ACI318),

$$V_n = 6 * \sqrt{f'_c} * b_0 * d / 1000 = 163.9 \text{ kips}$$

$$\text{Validity : IF}(V_u > \Phi * V_n; \text{"Not Valid"}; \text{"Valid"}) = \text{Valid}$$

Shear Strength provided by Concrete with Shear RFT (According to Cl.11.11.3.1 of ACI318),

$$V_{ci} = 2 * \lambda * \sqrt{f'_c} * b_0 * d / 1000 = 54.6 \text{ kips}$$

Nominal Shear Strength provided by Reinforcement (According to Eq. 11-2 of ACI318),

$$V_s = \frac{V_u - \Phi * V_{ci}}{\Phi} = 105.4 \text{ kips}$$

$$\text{Spacing of Provided Bars, } s = 3.0 \text{ in}$$

$$\text{Required Area of Reinforcement, } A_v = \frac{V_s * s * 1000}{f_y * d} = 0.88 \text{ in}^2$$

$$\text{Required Area of Reinforcement for each side of Column, } A_{v_side} = A_v / 4 = 0.22 \text{ in}^2$$

Perimeter of Critical Section where Shear Reinforcement may be terminated,

$$b'_0 = \frac{V_u * 1000}{\Phi * 2 * \lambda * \sqrt{f'_c} * d} = 210.8 \text{ in}$$

Distance from Column Face where Shear Reinforcement may be terminated,

$$a = \left(\frac{b'_0}{4} - c \right) / \sqrt{2} = 28.8 \text{ in}$$

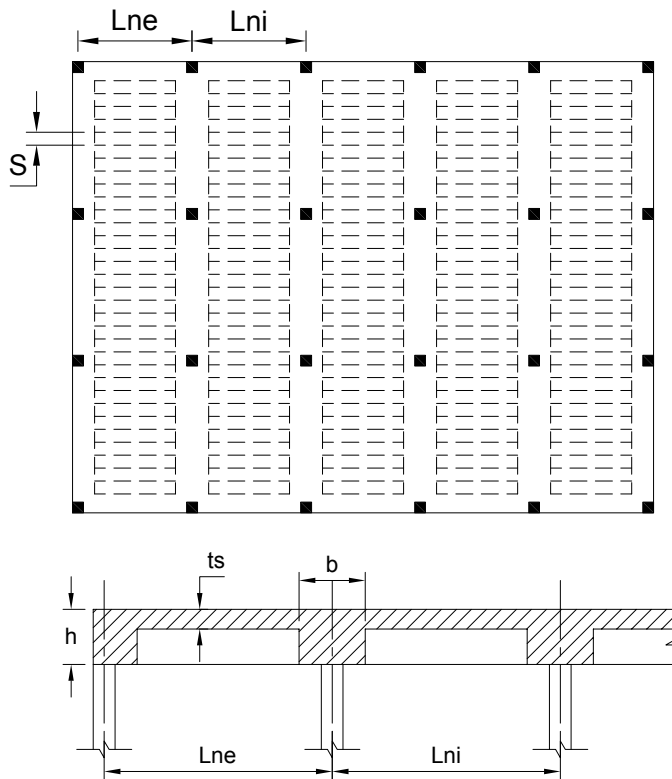
Design Summary

$$\text{Required Area of Reinforcement, } A_v = A_v = 0.88 \text{ in}^2$$

$$\text{Distance from Column Face where Shear Reinforcement may be terminated: } a = 28.8 \text{ in}$$



Design of One Way Joist as per ACI 318-11 Chapters 9 & 11



System

Width of Beam, b =	30.0 in
Width of Joist, b_j =	6.0 in
Spacing between Joists, s =	36.0 in
Slab Thickness, t_s =	3.5 in
Exterior Joist Span, L_{ne} =	27.5 ft
Interior Joist Span, L_{ni} =	27.0 ft
Concrete Cover, co =	1.25 in

Load

Dead Load, DL =	130 psf
Live Load, LL =	60 psf
Ultimate Load, w_u =	$\frac{1.2 * DL + 1.6 * LL}{1000} * \frac{s}{12} = 0.756 \text{ kip/ft}$



Chapter 1: Concrete Design

One Way Joist

ACI 318

Page: 42

Material Properties

Concrete Strength, f'_c =		4000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), ϕ =		0.90
Modification Factor for Lightweight Concrete, λ =		1.00
Factor for Rectangular Compressive Stress Block (According to Cl.10.2.7.3), β_1 = IF($f'_c \leq 4000$;0.85;IF($f'_c \geq 8000$;0.65;1.05-0.00005* f'_c))	=	0.85

Moment Distribution for Joist

1. End Span

$$\text{Edge Negative Moment for Exterior Joist, } M_{nee} = \frac{w_u * L_{ne}^2}{24} = 23.8 \text{ kip*ft}$$

$$\text{Positive Moment for Exterior Joist, } M_{pe} = \frac{w_u * L_{ne}^2}{14} = 40.8 \text{ kip*ft}$$

$$\text{Negative Moment for Exterior Joist, } M_{ne} = \frac{w_u * ((L_{ne} + L_{ni})/2)^2}{10} = 56.1 \text{ kip*ft}$$

2. Interior Spans

$$\text{Negative Moment for Interior Joist, } M_{ni} = \frac{w_u * L_{ni}^2}{11} = 50.1 \text{ kip*ft}$$

$$\text{Positive Moment for Interior Joist, } M_{pi} = \frac{w_u * L_{ni}^2}{16} = 34.4 \text{ kip*ft}$$

3. Maximum Moment

$$M_{max} = \text{MAX}(M_{nee}; M_{pe}; M_{ne}; M_{ni}; M_{pi}) = 56.1 \text{ kip*ft}$$



Calculation of Required Depth for Joist

$\rho_t =$	$0.319 * f'_c * \beta_1 / f_y$	=	0.01808
For Reasonable Deflection Control, choose a Reinforcement Ratio (ρ) equal to about one-half (ρ_t)			
Reinforcement Ratio, $\rho =$	$\rho_t / 2$	=	0.00904
$\omega =$	$\rho * \frac{f_y}{f'_c}$	=	0.13560
Required Depth, $d =$	$\sqrt{\frac{M_{max} * 12000}{\Phi * b_j * f'_c * \omega * (1 - 0.59 * \omega)}}$	=	15.8 in
Required Thickness, $h_{req} =$	$d + c_o$	=	17.1 in
$h_{min} =$	$MAX(L_{ne} * 12 + b; L_{ni} * 12 + b) / 18.5$	=	19.5 in
Provided Thickness, $h =$	$MAX(h_{req}; h_{min})$	=	19.5 in
Effective Depth of Joist, $d_j =$	$h - c_o$	=	18.25 in

Calculation of Required Reinforcement for Exterior Negative Moment of End Span (A_{sc1})

$R_{n1} =$	$\frac{M_{nee} * 12000}{\Phi * b_j * d_j^2}$	=	159 psi
Reinforcement Ratio, $\rho_1 =$	$0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - 2 * \frac{R_{n1}}{0.85 * f'_c}} \right)$	=	0.0027
Area of Reinforcement, $A_{s1} =$	$\rho_1 * b_j * d_j$	=	0.30 in ²
Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),			
$A_{s_min1} =$	$\frac{3 * \sqrt{f'_c} * b_j * d_j}{f_y}$	=	0.35 in ²
$A_{s_min2} =$	$\frac{200 * b_j * d_j}{f_y}$	=	0.36 in ²
$A_{s_min} =$	$MAX(A_{s_min1}; A_{s_min2})$	=	0.36 in ²
Required Area of Reinforcement, $A_{sc1} =$	$MAX(A_{s1}; A_{s_min})$	=	0.36 in ²
Provided Reinforcement, Bar =	SEL("ACI/Bar"; Bar;)	=	No.3
Provided Reinforcement, $A_{sb} =$	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.11 in ²
Number of Bars, $n =$			4
Vertical Reinforcement, $A_{sc1_Prov} =$	$A_{sb} * n$	=	0.44 in ²
Check Validity =	IF($A_{sc1_Prov} \geq A_{sc1}$; "Valid"; "Invalid")	=	Valid



Calculation of Required Reinforcement for Positive Moment of End Span (A_{sc2})

$$R_{n2} = \frac{M_{pe} * 12000}{\Phi * b_j * d_j^2} = 272 \text{ psi}$$
$$\text{Reinforcement Ratio, } \rho_2 = 0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - 2 * \frac{R_{n2}}{0.85 * f'_c}} \right) = 0.0047$$
$$\text{Area of Reinforcement, } A_{s2} = \rho_2 * b_j * d_j = 0.51 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),

$$A_{s_min1} = \frac{3 * \sqrt{f'_c} * b_j * d_j}{f_y} = 0.35 \text{ in}^2$$
$$A_{s_min2} = \frac{200 * b_j * d_j}{f_y} = 0.36 \text{ in}^2$$
$$A_{s_min} = \text{MAX}(A_{s_min1}; A_{s_min2}) = 0.36 \text{ in}^2$$
$$\text{Required Area of Reinforcement, } A_{sc2} = \text{MAX}(A_{s2}; A_{s_min}) = 0.51 \text{ in}^2$$
$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"; Bar; }) = \text{No.5}$$
$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"; Asb; Bar=Bar}) = 0.31 \text{ in}^2$$
$$\text{Number of Bars, } n = 2$$
$$\text{Vertical Reinforcement, } A_{sc2_Prov} = A_{sb} * n = 0.62 \text{ in}^2$$
$$\text{Check Validity} = \text{IF}(A_{sc2_Prov} \geq A_{sc2}; \text{"Valid"; "Invalid"}) = \text{Valid}$$

Calculation of Required Reinforcement for Interior Negative Moment of End Span (A_{sc3})

$$R_{n3} = \frac{M_{ne} * 12000}{\Phi * b_j * d_j^2} = 374 \text{ psi}$$
$$\text{Reinforcement Ratio, } \rho_3 = 0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - 2 * \frac{R_{n3}}{0.85 * f'_c}} \right) = 0.0066$$
$$\text{Area of Reinforcement, } A_{s3} = \rho_3 * b_j * d_j = 0.72 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),

$$A_{s_min1} = \frac{3 * \sqrt{f'_c} * b_j * d_j}{f_y} = 0.35 \text{ in}^2$$
$$A_{s_min2} = \frac{200 * b_j * d_j}{f_y} = 0.36 \text{ in}^2$$
$$A_{s_min} = \text{MAX}(A_{s_min1}; A_{s_min2}) = 0.36 \text{ in}^2$$
$$\text{Required Area of Reinforcement, } A_{sc3} = \text{MAX}(A_{s3}; A_{s_min}) = 0.72 \text{ in}^2$$



Chapter 1: Concrete Design

One Way Joist

ACI 318

Page: 45

Provided Reinforcement, Bar=	SEL("ACI/Bar"; Bar;)	=	No.5
Provided Reinforcement, A_{sb} =	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.31 in ²
Number of Bars, n=			3
Vertical Reinforcement, A_{sc3_Prov} =	$A_{sb} * n$	=	0.93 in ²
Check Validity=	IF($A_{sc3_Prov} \geq A_{sc3}$; "Valid"; "Invalid")	=	Valid

Calculation of Required Reinforcement for Interior Negative Moment of Interior Span (A_{sc4})

R_{n4} =	$\frac{M_{ni} * 12000}{\Phi * b_j * d_j^2}$	=	334 psi
Reinforcement Ratio, ρ_4 =	$0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - 2 * \frac{R_{n4}}{0.85 * f'_c}} \right)$	=	0.0059
Area of Reinforcement, A_{s4} =	$\rho_4 * b_j * d_j$	=	0.65 in ²
Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),			
A_{s_min1} =	$\frac{3 * \sqrt{f'_c} * b_j * d_j}{f_y}$	=	0.35 in ²
A_{s_min2} =	$\frac{200 * b_j * d_j}{f_y}$	=	0.36 in ²
A_{s_min} =	MAX(A_{s_min1} ; A_{s_min2})	=	0.36 in ²
Required Area of Reinforcement, A_{sc4} =	MAX(A_{s4} ; A_{s_min})	=	0.65 in ²
Provided Reinforcement, Bar=	SEL("ACI/Bar"; Bar;)	=	No.5
Provided Reinforcement, A_{sb} =	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.31 in ²
Number of Bars, n=			3
Vertical Reinforcement, A_{sc4_Prov} =	$A_{sb} * n$	=	0.93 in ²
Check Validity=	IF($A_{sc4_Prov} \geq A_{sc4}$; "Valid"; "Invalid")	=	Valid



Calculation of Required Reinforcement for Interior Positive Moment of Interior Span (A_{sc5})

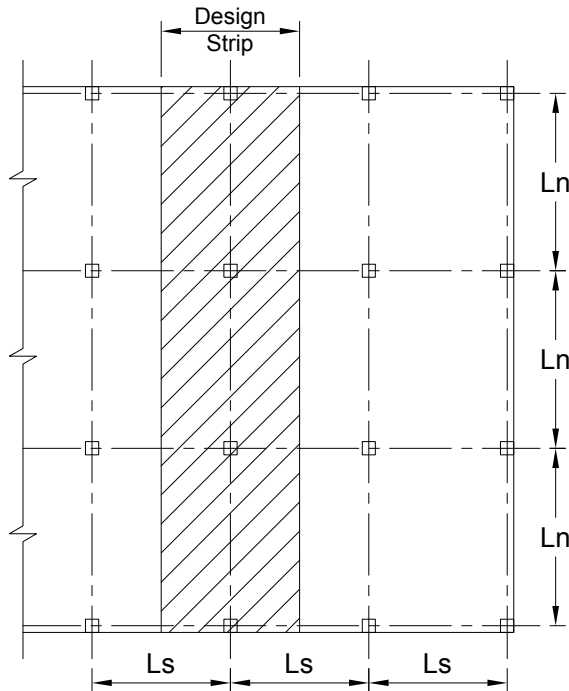
$R_{n5} =$	$\frac{M_{pi} * 12000}{\Phi * b_j * d_j^2}$	=	230 psi
Reinforcement Ratio, $\rho_5 =$	$0.85 * \frac{f'_c}{f_y} * \left(1 - \sqrt{1 - 2 * \frac{R_{n5}}{0.85 * f'_c}}\right)$	=	0.0040
Area of Reinforcement, $A_{s5} =$	$\rho_5 * b_j * d_j$	=	0.44 in ²
Minimum Area of Reinforcement (According to Cl.10.5 of ACI318),			
$A_{s_min1} =$	$\frac{3 * \sqrt{f'_c} * b_j * d_j}{f_y}$	=	0.35 in ²
$A_{s_min2} =$	$\frac{200 * b_j * d_j}{f_y}$	=	0.36 in ²
$A_{s_min} =$	$MAX(A_{s_min1}; A_{s_min2})$	=	0.36 in ²
Required Area of Reinforcement, $A_{sc5} =$	$MAX(A_{s5}; A_{s_min})$	=	0.44 in ²
Provided Reinforcement, Bar =	SEL("ACI/Bar"; Bar;)	=	No.5
Provided Reinforcement, $A_{sb} =$	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.31 in ²
Number of Bars, n =			2
Vertical Reinforcement, $A_{sc5_Prov} =$	$A_{sb} * n$	=	0.62 in ²
Check Validity =	IF($A_{sc5_Prov} \geq A_{sc5}$; "Valid"; "Invalid")	=	Valid

Design Summary

Area of Reinforcement for Exterior Negative Moment of End Span:	A_{sc1_Prov}	=	0.44 in ²
Area of Reinforcement for Positive Moment of End Span:	A_{sc2_Prov}	=	0.62 in ²
Area of Reinforcement for Interior Negative Moment of End Span:	A_{sc3_Prov}	=	0.93 in ²
Area of Reinforcement for Interior Negative Moment of Interior Span:	A_{sc4_Prov}	=	0.93 in ²
Area of Reinforcement for Interior Positive Moment of Interior Span:	A_{sc5_Prov}	=	0.62 in ²



Design Two-Way Slab without Beams Analyzed by the Direct Design Method As per ACI 318-11



System

Longer Span for Two-Way Slab, L_n =		18.00 ft
Shorter Span for Two-Way Slab, L_s =		14.00 ft
Thickness of Slab, h =		7.00 in
Concrete Cover, co =		1.25 in
Depth of Slab, d =	$h - co$	= 5.75 in
Square Column Dimension, b_c =		16.00 in
Width of Column Strip, b =	$L_s * 12 / 2$	= 84 in
Width of Middle Strip, b_m =	$L_s * 12 - b$	= 84 in

Load

Slab Self Weight, q_s =	$h/12 * 150$	= 87.50 psf
Partition Load, q_p =		20.00 psf
Dead Load, q_D =	$q_s + q_p$	= 107.50 psf
Live Load, q_L =		40.00 psf
Ultimate Load, q_U =	$1.2 * q_D + 1.6 * q_L$	= 193.00 psf

Material Properties

Concrete Strength, f'_c =		3000 psi
Yield Strength of Reinforcement, f_y =		60000 psi



Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), $\Phi = 0.90$
 Minimum Reinforcement Ratio (According to Cl.7.12.2 of ACI318),
 $\rho_{min} = \text{IF}(f_y \leq 50000; 0.002; \text{IF}(f_y \geq 77143; 0.0014; 0.0018)) = 0.0018$

Total Static Moment of Slab

Total Factored Static Moment Per Span (According to Eq. 13-4 of ACI318),

$$M_0 = \frac{q_U * L_s}{8 * 1000} * \left(L_n - \frac{b_c}{12} \right)^2 = 93.82 \text{ kip*ft}$$

Flexural Reinforcement Required for Negative Moment of Column Strip

$$R_{n1} = \frac{M_0 * 12000 * 0.53}{\Phi * b * d^2} = 239 \text{ psi}$$

$$\text{Ratio of RFT, } \rho_1 = \frac{0.85 * f_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_{n1}}{0.85 * f_c}} \right) = 0.00419$$

Area of Steel, $A_{s1_Req} = \text{MAX}(\rho_1; \rho_{min}) * b * d = 2.02 \text{ in}^2$
 Provided Reinforcement, Bar = SEL("ACI/Bar"; Bar;) = No.6
 Provided Reinforcement, $A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.44 \text{ in}^2$
 Number of Bars, n = 5
 Vertical Reinforcement, $A_{s1_Prov} = A_{sb} * n = 2.20 \text{ in}^2$
 Check Validity = IF($A_{s1_Prov} \geq A_{s1_Req}$; "Valid"; "Invalid") = Valid

Flexural Reinforcement Required for Positive Moment of Column Strip

$$R_{n2} = \frac{M_0 * 12000 * 0.31}{\Phi * b * d^2} = 140 \text{ psi}$$

$$\text{Ratio of RFT, } \rho_2 = \frac{0.85 * f_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_{n2}}{0.85 * f_c}} \right) = 0.00240$$

Area of Steel, $A_{s2_Req} = \text{MAX}(\rho_2; \rho_{min}) * b * d = 1.16 \text{ in}^2$
 Provided Reinforcement, Bar = SEL("ACI/Bar"; Bar;) = No.6
 Provided Reinforcement, $A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.44 \text{ in}^2$
 Number of Bars, n = 3
 Vertical Reinforcement, $A_{s2_Prov} = A_{sb} * n = 1.32 \text{ in}^2$
 Check Validity = IF($A_{s2_Prov} \geq A_{s2_Req}$; "Valid"; "Invalid") = Valid



Flexural Reinforcement Required for Negative Moment of Middle Strip

$R_{n3} =$	$\frac{M_0 * 12000 * 0.17}{\phi * b * d^2}$	=	77 psi
Ratio of RFT, $\rho_3 =$	$\frac{0.85 * f_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_{n3}}{0.85 * f_c}} \right)$	=	0.00130
Area of Steel, $A_{s3_Req} =$	$MAX(\rho_3; \rho_{min}) * b * d$	=	0.87 in ²
Provided Reinforcement, Bar =	SEL("ACI/Bar"; Bar;)	=	No.6
Provided Reinforcement, $A_{sb} =$	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.44 in ²
Number of Bars, n =			2
Vertical Reinforcement, $A_{s3_Prov} =$	$A_{sb} * n$	=	0.88 in ²
Check Validity =	IF($A_{s3_Prov} \geq A_{s3_Req}$; "Valid"; "Invalid")	=	Valid

Flexural Reinforcement Required for Positive Moment of Middle Strip

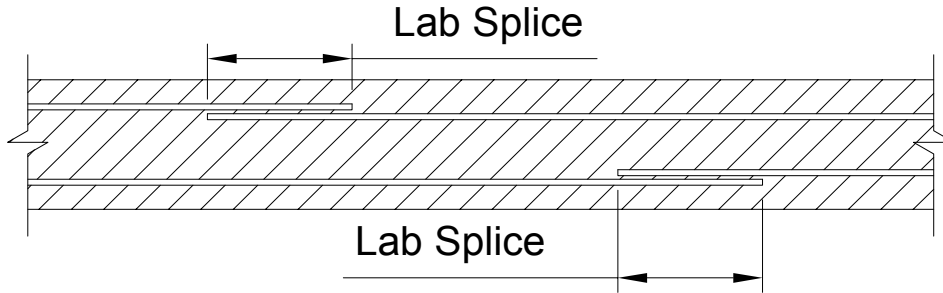
$R_{n4} =$	$\frac{M_0 * 12000 * 0.21}{\phi * b * d^2}$	=	95 psi
Ratio of RFT, $\rho_4 =$	$\frac{0.85 * f_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_{n4}}{0.85 * f_c}} \right)$	=	0.00161
Area of Steel, $A_{s4_Req} =$	$MAX(\rho_4; \rho_{min}) * b * d$	=	0.87 in ²
Provided Reinforcement, Bar =	SEL("ACI/Bar"; Bar;)	=	No.6
Provided Reinforcement, $A_{sb} =$	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.44 in ²
Number of Bars, n =			2
Vertical Reinforcement, $A_{s4_Prov} =$	$A_{sb} * n$	=	0.88 in ²
Check Validity =	IF($A_{s4_Prov} \geq A_{s4_Req}$; "Valid"; "Invalid")	=	Valid

Design Summary

Area of Reinforcement Required for Negative Moment of Middle Strip,	A_{s1_Prov}	=	2.20 in ²
Area of Reinforcement Required for Negative Moment of Middle Strip,	A_{s2_Prov}	=	1.32 in ²
Area of Reinforcement Required for Negative Moment of Middle Strip,	A_{s3_Prov}	=	0.88 in ²
Area of Reinforcement Required for Positive Moment of Middle Strip,	A_{s4_Prov}	=	0.88 in ²



Calculating Development Length of Bars in Tension as per ACI 318-11 Chapter 12



Material Properties

Concrete Strength, f'_c =			4000 psi
Yield Strength of Reinforcement, f_y =			60000 psi
Modification Factor for Lightweight Concrete, λ =			0.75
Factor of Development Length Based on RFT Location (According to Cl.12.2.4 of ACI318), ψ_t =			1.30
Factor of Development Length Based on RFT Coating (According to Cl.12.2.4 of ACI318), ψ_e =			1.50
Maximum Modifying Factor, ψ_{te} =	MIN($\psi_t * \psi_e$; 1.7)	=	1.70
Identification of, Bar=	SEL("ACI/Bar" ;Bar;)	=	No.7
Diameter of Bars, d_b =	TAB("ACI/Bar" ;Dia ;Bar=Bar)	=	0.88 in

Calculation of Development Length

1. Class A Splice

Development Length for Bars No.6 and Smaller (According to Cl.12.2.2 of ACI318),

$$L_{d_A1} = \left(\frac{3 * f_y * \psi_{te}}{50 * \lambda * \sqrt{f'_c}} \right) * d_b = 114 \text{ in}$$

Development Length for Bars No.7 and Greater (According to Cl.12.2.2 of ACI318),

$$L_{d_A2} = \left(\frac{3 * f_y * \psi_{te}}{40 * \lambda * \sqrt{f'_c}} \right) * d_b = 142 \text{ in}$$

$$L_{d_A} = \text{IF}(d_b \leq 0.75 ; L_{d_A1} ; L_{d_A2}) = 142 \text{ in}$$

2. Class B Splice

Development Length for Bars No.6 and Smaller (According to Cl.12.2.2 of ACI 318),

$$L_{d_B1} = \left(\frac{3 * f_y * \psi_{te}}{50 * \lambda * \sqrt{f'_c}} \right) * 1.3 * d_b = 148 \text{ in}$$



Chapter 1: Concrete Design

Development Length of Bars in Tension

ACI 318

Page: 51

Development Length for Bars No.7 and Greater (According to Cl.12.2.2 of ACI318),

$$L_{d_B2} = \left(\frac{3 * f_y * \psi_{te}}{40 * \lambda * \sqrt{f_c}} \right) * 1.3 * d_b = 184 \text{ in}$$

$$L_{d_B} = \text{IF}(d_b \leq 0.75 ; L_{d_B1} ; L_{d_B2}) = 184 \text{ in}$$

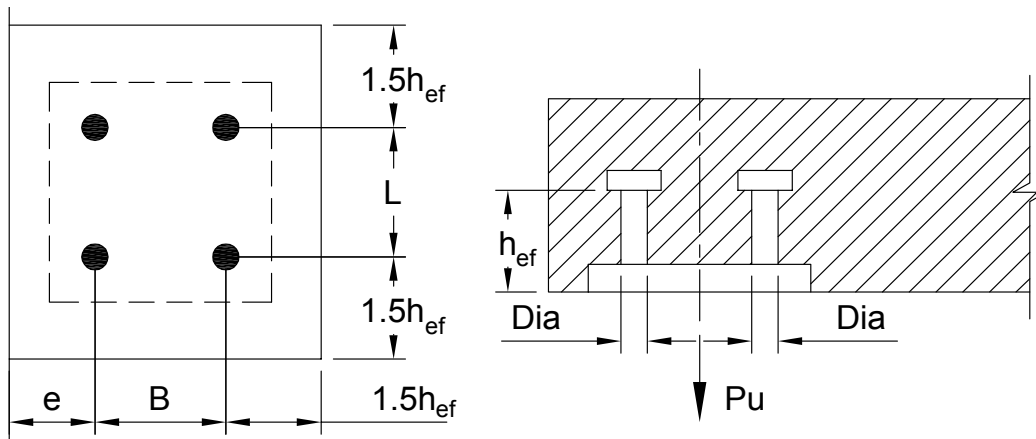
Calculation Summary

$$\text{Development Length for Class A, } L_{d_A} = L_{d_A} = 142 \text{ in}$$

$$\text{Development Length for Class B, } L_{d_B} = L_{d_B} = 184 \text{ in}$$



Group of Headed Studs in Tension Near an Edge as per ACI 318-11 Appendix D



System

Spacing between Bolts along x-x, B=	6.00 in
Spacing between Bolts along y-y, L=	6.00 in
Distance to Edge from Nearst bolt, e=	3.00 in

Load

Ultimate Load, P_u =	14000 lb
Number of Anchors, n=	4

Material Properties

Concrete Strength, f'_c =	4000 psi
Tensile Strength of Anchor Bolt Grade, f_{uta} =	60000 psi
Strength Reduction Factor (According to Cl.D.4.4.a of ACI318), Φ_1 =	0.75
Strength Reduction Factor (According to Cl.D.4.4.c of ACI318), Φ_2 =	0.70
Modification Factor for Lightweight Concrete, λ =	1.00

Determine Anchor Diameter

Required Effective Area of Anchor Bolt (According to Eq.D.2 of ACI318),

A_{se_Req} =	$\frac{P_u}{\Phi_1 * n * f_{uta}}$	=	0.078 in ²
Provided Anchor Bolt, Dia=	SEL("ACI/Anchor"; Dia;)	=	0.500 in
Provided Area of Anchor Bolt, A_{se_Prov} =	TAB("ACI/Anchor"; Ase; Dia=Dia)	=	0.142 in ²
Check Validity=	IF($A_{se_Prov} \geq A_{se_Req}$; "Valid"; "Increase Dia")	=	Valid



Determine Embedment Length

Assume that, $h_{ef_Prov} = 4.50$ in

Projected Area of Failure Surface for Anchors (According to Cl.D.5.2.1 of ACI318),

$$A_{nc} = (1.5 * h_{ef_Prov} + L + e) * (1.5 * 2 * h_{ef_Prov} + B) = 307 \text{ in}^2$$

Projected Area of Failure Surface for Single Anchor (According to Cl.D.5.2.1 of ACI318),

$$A_{nco} = 9 * h_{ef_Prov}^2 = 182 \text{ in}^2$$

Check Validity = IF($A_{nc} < n * A_{nco}$; "Valid"; "Increase hef") = Valid

Factor (According to Cl.D.5.2.4 of ACI318), $\psi_{ec,N} = 1.00$

$$\text{Factor (According to Cl.D.5.2.5 of ACI318), } \psi_{ed,N} = 0.7 + \frac{0.3 * e}{1.5 * h_{ef_Prov}} = 0.83$$

Factor (According to Cl.D.5.2.6 of ACI318), $\psi_{c,N} = 1.00$

Factor (According to Cl.D.5.2.6 of ACI318), $\psi_{cp,N} = 1.00$

Basic Strength of Concrete Breakout (According to Eq.D-6 of ACI318),

$$N_b = 24 * \lambda * \sqrt{f_c} * h_{ef_Prov}^{1.5} = 14490 \text{ lb}$$

Nominal Strength of Concrete Breakout (According to Eq.D-5 of ACI318),

$$N_{cbg} = \frac{A_{nc}}{A_{nco}} * \psi_{ec,N} * \psi_{ed,N} * \psi_{c,N} * \psi_{cp,N} * N_b = 20287 \text{ lb}$$

Check Validation = IF($P_u < \Phi_2 * N_{cbg}$; "Valid"; "Increase hef") = Valid

Calculation of Required Head Size

Factor (According to Cl.D.5.3.6 of ACI318), $\psi_{c,P} = 1.00$

Required Head Size for Anchor Bolt (According to Eq.D-15 of ACI318),

$$A_{brg} = \frac{P_u / n}{\Phi_2 * \psi_{c,P} * 8 * f_c} = 0.156 \text{ in}^2$$

Design Summary

Diameter of Anchor Bolt, Dia = Dia = 0.500 in

Embedment Length of Anchor Bolt, $h_{ef} = h_{ef_Prov} = 4.50$ in

Head Size of Anchor Bolt, $A_{brg} = A_{brg} = 0.156 \text{ in}^2$



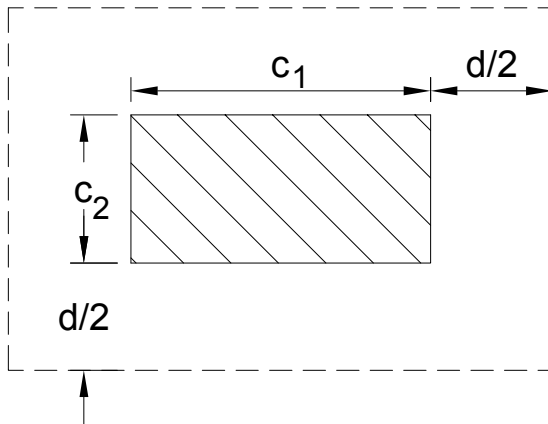
Chapter 1: Concrete Design

Shear Strength of Slab at Column Support

ACI 318

Page: 54

Shear Strength of Slab at Column Support as per ACI 318-11 Chapter 11



System

Width of Column, c_1 =	48.0 in
Length of Column, c_2 =	8.0 in
Thickness of Slab, t =	10.0 in
Concrete Cover, co =	3.5 in
Effective Depth of Slab, $d = t - co$	= 6.5 in

Load

Ultimate Shear Force, V_u =	20 kips
-------------------------------	---------

Material Properties

Concrete Strength, f'_c =	4000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	1.00

Check Slab Thickness

Perimeter of Critical Section for Two-Way Shear, $b_0 = 2*(c_1 + d) + 2*(c_2 + d)$	= 138 in
Column Type=	SEL("ACI/Alfa S";Type;) = Interior
Alfa Constant, α_s =	TAB("ACI/AlfaS"; Alfa; Type=Type) = 40.00
Ratio of Long to Short Column Dimensions, $\beta = \text{MAX}(c_1;c_2)/\text{MIN}(c_1;c_2)$	= 6.00
Concrete Shear Strength (According to Eq. 11-31 of ACI318),	
$V_{c1} = (2 + 4/\beta) * \lambda * \sqrt{f'_c} * b_0 * d / 1000$	= 151.3 kips
Concrete Shear Strength (According to Eq. 11-32 of ACI318),	
$V_{c2} = (\alpha_s * d / b_0 + 2) * \lambda * \sqrt{f'_c} * b_0 * d / 1000$	= 220.3 kips



Chapter 1: Concrete Design

Shear Strength of Slab at Column Support

ACI 318

Page: 55

Concrete Shear Strength (According to Eq. 11-33 of ACI318),

$$V_{c3} = 4 * \lambda * \sqrt{f'_c} * b_0 * d / 1000 = 226.9 \text{ kips}$$

$$\text{Nominal Concrete Shear Strength, } \Phi V_c = \Phi * \text{MIN}(V_{c1}; V_{c2}; V_{c3}) = 113.5 \text{ kips}$$

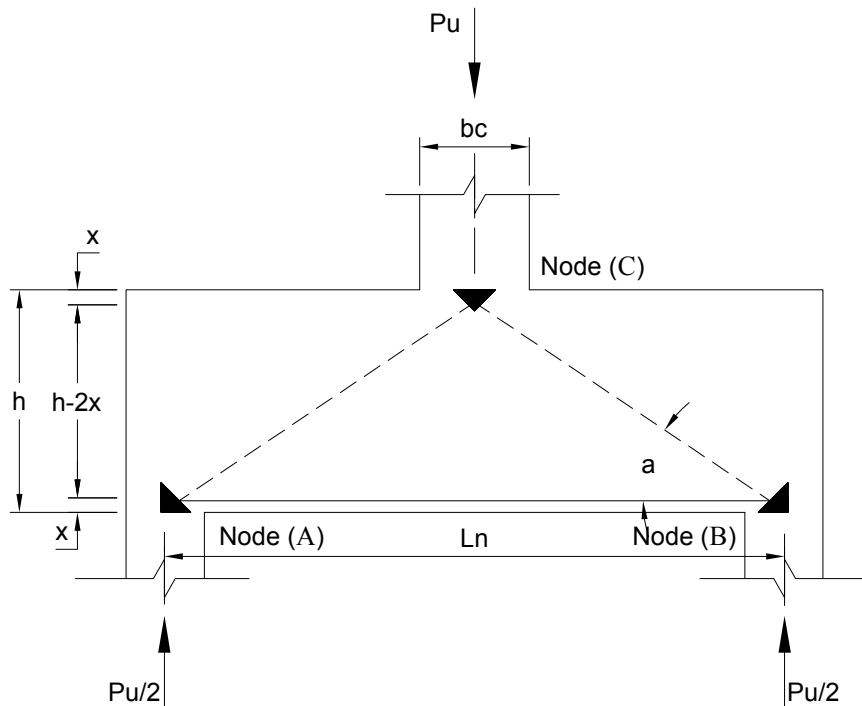
$$\text{Validation} = \text{IF}(\Phi V_c > V_u; \text{"O.K."}; \text{"Increase Depth"}) = \text{O.K.}$$

Calculation Summary

$$\text{Thickness of Slab, } t = t = 10 \text{ in}$$



Design of Simple Span Deep Beam by the Strut-and-Tie Model as per ACI318 Appendix A



System

Width of Deep Beam, b_c =		7.0 in
Height of Deep Beam, h =		60.0 in
Concrete Cover, c_o =		1.25 in
Depth of Deep Beam, d =	$h - c_o$	= 58.75 in
End Distance of Truss Model, x =		5.0 in
Span of Deep Beam, L_n =		13.3 ft
Column Width, b_c =		20.0 in

Load

Dead Load for Column, P_D =		173.35 kips
Live Load for Column, P_L =		270.0 kips
Service Load for Column, P =	$1.0 * P_D + 1.0 * P_L$	= 443.4 kips
Ultimate Load for Column, P_u =	$1.2 * P_D + 1.6 * P_L$	= 640.0 kips



Chapter 1: Concrete Design

Simple Span Deep Beam by Strut-and-Tie Model

ACI 318

Page: 57

Material Properties

Concrete Strength, f'_c =		4000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =		0.75
Modification Factor for Lightweight Concrete, λ =		1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), μ =	$1.4 * \lambda$	= 1.40

Check Deep Beam Requirements

Check on Height of Deep Beam Requirements (According to Cl.11.7.1 of ACI318),

$$R = \text{IF}(12 * L_n / h < 4; \text{"Deep Beam Design"}; \text{"Normal Beam Design"}) = \text{Deep Beam Design}$$

Estimation of Truss Model

$$\text{Length of Diagonal Strut, } L_1 = \sqrt{\left(\frac{L_n * 12}{2}\right)^2 + (h - 2 * x)^2} = 94.17 \text{ in}$$

$$\text{The Force in Diagonal Strut, } F_s = \frac{P_u}{2} * \frac{L_1}{h - 2 * x} = 602.69 \text{ kips}$$

$$\text{The Force in Horizontal Tie, } F_t = \frac{P_u}{2} * \frac{0.5 * L_n * 12}{h - 2 * x} = 510.72 \text{ kips}$$

$$\text{Angle Between Diagonal Strut and Horizontal Tie, } \alpha = \text{atan}\left(\frac{h - 2 * x}{0.5 * L_n * 12}\right) = 32.07^\circ$$

$$\text{Check Validity (According to Cl.A.2.5 of ACI318)} = \text{IF}(\alpha > 25; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Calculation of Effective Concrete Strength

$$\text{(According to Cl.3.2.2(a) of ACI318) Factor of, } \beta_s = 0.75$$

Effective Concrete Strength (According to Eq.A-3 of ACI 318),

$$f_{ce1} = 0.85 * \beta_s * f'_c = 2550 \text{ psi}$$

Calculation of Effective Concrete Strength for Nodal Zones

For Nodal Zone C Bounded by Three Struts (C-C-C Nodal Zone)

$$\text{(According to Cl.A.5.2.1 of ACI318) Factor of, } \beta_n = 1.00$$

Effective Concrete Strength (According to Eq.A-3 of ACI 318),

$$f_{ce2} = 0.85 * \beta_n * f'_c = 3400 \text{ psi}$$

For Nodal Zone A&B Bounded by Three Struts (C-C-T Nodal Zone)

$$\text{(According to Cl.A.5.2.2 of ACI318) Factor of, } \beta_n = 0.80$$

Effective Concrete Strength (According to Eq.A-3 of ACI 318),

$$f_{ce3} = 0.85 * \beta_n * f'_c = 2720 \text{ psi}$$

$$\text{Minimum Effective Concrete Strength, } f_{ce} = \text{MIN}(f_{ce1}; f_{ce2}; f_{ce3}) = 2550 \text{ psi}$$



Check Strength at Node C

The Length of The Horizontal Face of Nodal Zone C,

$$L_{hc} = \frac{P_u * 1000}{\Phi * b_c * f_{ce}} = 16.73 \text{ in}$$

The Length of Other Faces of Nodal Zone C,

$$L_c = L_{hc} * \frac{F_s}{P_u} = 15.75 \text{ in}$$

Check Strength at Node A&B

The Length of The Horizontal Face of Nodal Zone A,

$$L_{ha} = \frac{F_t * 1000}{\Phi * b_c * f_{ce}} = 13.35 \text{ in}$$

Width of Node at Support A,

$$L_a = \frac{0.5 * P_u * 1000}{\Phi * b_c * f_{ce}} = 8.37 \text{ in}$$

Calculation VL and HZ Reinforcement to Resist Splitting Diagonal Struts

1. Vertical Reinforcement

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.4

Provided Reinforcement, A_{sbv} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.20 in²

Number of Bars, n_v = 4

Vertical Reinforcement, A_{sv} = $A_{sbv} * n_v$ = 0.80 in²

Provided Spacing between Bars, s= 11.00 in

Vertical Reinforcement (According to Eq.A4 of ACI318),

$$VL = \frac{A_{sv}}{b_c * s} * \sin(90 - \alpha) = 0.00308$$

2. Horizontal Reinforcement

Provided Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.5

Provided Reinforcement, A_{sbh} = TAB("ACI/Bar"; Asb; Bar=Bar) = 0.31 in²

Number of Bars, n_h = 2

Vertical Reinforcement, A_{sh} = $A_{sbh} * n_h$ = 0.62 in²

Provided Spacing between Bars, s= 11.00 in

Horizontal Reinforcement (According to Eq.A4 of ACI318),

$$HZ = \frac{A_{sh}}{b_c * s} * \sin(\alpha) = 0.00150$$

Check Validity= IF(VL+HZ>0.003; "Valid"; "Invalid") = Valid



Calculation of Tension Reinforcement for Tie Connecting Node A&B

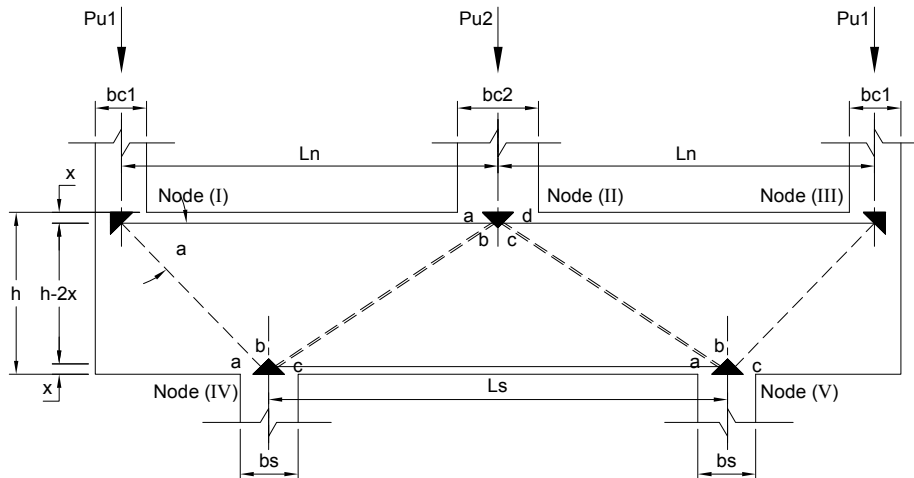
Required Reinforcement Area, A_{sreq}	$\frac{F_t * 1000}{\phi * f_y}$	=	11.35 in ²
Provided Reinforcement, Bar	SEL("ACI/Bar"; Bar;)	=	No.8
Provided Reinforcement, A_{sb}	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.79 in ²
Number of Bars, n			16
Total Provided Area, A_{sprov}	$n * A_{sb}$	=	12.64 in ²
Check Validity	IF(Asprov>Asreq; "Valid"; "Invalid")	=	Valid

Design Summary

Provided Vertical Reinforcement, A_{sv}	A_{sv}	=	0.80 in ²
Provided Horizontal Reinforcement, A_{sh}	A_{sh}	=	0.62 in ²
Provided Tension Reinforcement, A_{sprov}	A_{sprov}	=	12.64 in ²



Design of Continuous Deep Beam by the Strut-and-Tie Model as per ACI318 Appendix A



System

Width of Deep Beam, b =		24.0 in
Height of Deep Beam, h =		144.0 in
Concrete Cover, co =		1.25 in
Depth of Deep Beam, d =	$h - co$	= 142.75 in
Upper End Distance of Truss Model, x_1 =		6.0 in
Lower End Distance of Truss Model, x_2 =		9.0 in
Span of Deep Beam, L_n =		24.0 ft
Exterior Planted Column Width, b_{c1} =		24.0 in
Interior Planted Column Width, b_{c2} =		56.0 in
Distance between Supports of Deep Beam, L_s =		24.0 ft
Support Column Width, b_s =		48.0 in
Support Column Depth, d_s =		24.0 in

Load

Dead Load for Exterior Column, P_{D1} =		100.0 kips
Live Load for Exterior Column, P_{L1} =		237.5 kips
Ultimate Load for Exterior Column, P_{u1} =	$1.2 * P_{D1} + 1.6 * P_{L1}$	= 500.0 kips
Dead Load for Interior Column, P_{D2} =		750.0 kips
Live Load for Interior Column, P_{L2} =		1000.0 kips
Ultimate Load for Interior Column, P_{u2} =	$1.2 * P_{D2} + 1.6 * P_{L2}$	= 2500.0 kips
Support Column Ultimate Load, P_u =	$P_{u1} + P_{u2} / 2$	= 1750.0 kips



Chapter 1: Concrete Design

Continuous Deep Beam by Strut-and-Tie Model

ACI 318

Page: 61

Material Properties

Concrete Strength, f'_c =		4000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =		0.75
Modification Factor for Lightweight Concrete, λ =		1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), μ =	$1.4 * \lambda$	= 1.40

Check Deep Beam Requirements

Check on Height of Deep Beam Requirements (According to Cl.11.7.1 of ACI318),
 $R = \text{IF}(12 * L_n / h < 4; \text{"Deep Beam Design"}; \text{"Normal Beam Design"}) = \text{Deep Beam Design}$

Calculation of Effective Concrete Strength

(According to Cl.A.3.2 of ACI318) Factor of, β_s = 1.00
 Effective Concrete Strength (According to Eq.A-3 of ACI 318),
 $f_{ce1} = 0.85 * \beta_s * f'_c = 3400 \text{ psi}$

Calculation of Effective Concrete Strength for Nodal Zones

For Nodal Zone IV Bounded by Three Struts (C-C-C Nodal Zone)
 (According to Cl.A.5.2.1 of ACI318) Factor of, β_n = 1.00
 Effective Concrete Strength (According to Eq.A-3 of ACI 318),
 $f_{ce2} = 0.85 * \beta_n * f'_c = 3400 \text{ psi}$

For Nodal Zone A&B Bounded by Three Struts (C-C-T Nodal Zone)
 (According to Cl.A.5.2.2 of ACI318) Factor of, β_n = 0.80
 Effective Concrete Strength (According to Eq.A-3 of ACI 318),
 $f_{ce3} = 0.85 * \beta_n * f'_c = 2720 \text{ psi}$

Minimum Effective Concrete Strength, $f_{ce} = \text{MIN}(f_{ce1}; f_{ce2}; f_{ce3}) = 2720 \text{ psi}$

Calculation of Forces in Struts

For Node IV Will Carry Exterior Column Load Strut, $F_a = P_{u1} = 500.00 \text{ kips}$
 For Node IV Other Struts B and C, $F_{bc} = 0.5 * (P_u - F_a) = 625.00 \text{ kips}$

Check Width of Struts at Node IV

Width of Strut a, $W_{sa} = \frac{F_a * 1000}{\Phi * f_{ce} * b} = 10.21 \text{ in}$

Width of Strut b&c, $W_{sbc} = \frac{F_{bc} * 1000}{\Phi * f_{ce} * b} = 12.77 \text{ in}$

Total Width of Struts, $W_s = W_{sa} + W_{sbc} * 2 = 35.75 \text{ in}$

Check Validity= $\text{IF}(W_s < b_s; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$



Chapter 1: Concrete Design

Continuous Deep Beam by Strut-and-Tie Model

ACI 318

Page: 62

Check Width of Struts at Node I

$$\text{Width of Strut, } W_{sI} = \frac{P_{u1} * 1000}{\Phi * f_{ce} * b} = 10.21 \text{ in}$$

$$\text{Check Validity} = \text{IF}(W_{sI} < b_{c1}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Check Width of Struts at Node II

$$\text{Width of Strut, } W_{sII} = \frac{P_{u2} * 1000}{\Phi * f_{ce} * b} = 51.06 \text{ in}$$

$$\text{Check Validity} = \text{IF}(W_{sII} < b_{c2}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Calculation of Force in Strut I-IVa and Tie I-IIa

$$\text{Horizontal Projection of Strut I-IVa, } L_{hiiva} = \frac{(L_n * 2 - L_s) * 12}{2} - W_{sbc} = 131.23 \text{ in}$$

$$\text{Vertical Projection of Strut I-IVa, } L_{viiva} = h - (x_1 + x_2) = 129.00 \text{ in}$$

$$\text{Horizontal Force in Strut I-IVa and Tie I-IIa, } F_{iiva} = P_{u1} * \frac{L_{hiiva}}{L_{viiva}} = 508.64 \text{ kips}$$

$$\text{Length of Strut I-IVa, } L_{iiva} = \sqrt{L_{hiiva}^2 + L_{viiva}^2} = 184.02 \text{ in}$$

$$\text{Compression Force in Strut I-IVa at Node I, } F_i = \frac{P_{u1} * L_{iiva}}{h - (x_1 + x_2)} = 713.26 \text{ kips}$$

$$\text{Check Validity} = \text{IF}(F_i < f_{ce}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Calculation of Width of Strut IIa-IVb

$$\text{Horizontal Projection of Strut IIa-IVb, } L_{hiiaivb} = \frac{(L_n * 2 - L_s) * 12}{2} - \frac{W_{sII} * 3}{8} = 124.9 \text{ in}$$

$$\text{Vertical Projection of Strut IIa-IVb, } L_{viiiaivb} = h - (x_1 + x_2 * 2) = 120.0 \text{ in}$$

$$\text{Vertical Force in Strut IIa-IVb, } F_{iiaivb} = F_{iiva} * \frac{L_{hiiaivb}}{L_{viiiaivb}} = 529.4 \text{ kips}$$

Calculation of Width of Strut IIa-IVc

$$\text{Horizontal Projection of Strut IIa-IVb, } L_{hiiaivb} = \frac{(L_n * 2 - L_s) * 12}{2} - \frac{W_{sII} * 3}{8} = 124.9 \text{ in}$$

$$\text{Vertical Projection of Strut IIa-IVb, } L_{viiiaivb} = h - (x_1 + x_2 * 2) = 120.0 \text{ in}$$

$$\text{Vertical Force in Strut IIa-IVb, } F_{iiaivb} = F_{iiva} * \frac{L_{hiiaivb}}{L_{viiiaivb}} = 529.4 \text{ kips}$$



Calculation of Width of Strut IIb-IVc

$$\begin{aligned} \text{Horizontal Projection of Strut IIa-IVb, } L_{hIIaIVb} &= \frac{(L_n * 2 - L_s) * 12}{2} - \frac{W_{sII} * 7}{50} = 136.9 \text{ in} \\ \text{Vertical Projection of Strut IIa-IVb, } L_{vIIaIVb} &= h - (x_1 + x_2 * 2) = 120.0 \text{ in} \\ \text{Vertical Force in Strut IIa-IVb, } F_{IIaIVb} &= F_i * \frac{L_{hIIaIVb}}{L_{vIIaIVb}} = 813.7 \text{ kips} \end{aligned}$$

Calculation of Width of Tie IVc-Va

$$\text{Force in Tie IVc-Va, } F_{IVcVa} = \frac{F_{IIaIVb} * 1000}{\Phi * f_{ce} * b} = 16.62 \text{ in}$$

Calculation VL and HZ Reinforcement to Resist Splitting of Diagonal Struts

1. Vertical Reinforcement

$$\begin{aligned} \text{Angle of Strut, } \alpha &= 46.60^\circ \\ \text{Provided Reinforcement, Bar} &= \text{SEL("ACI/Bar"; Bar;)} = \text{No.5} \\ \text{Provided Reinforcement, } A_{sbv} &= \text{TAB("ACI/Bar"; Asb; Bar=Bar)} = 0.31 \text{ in}^2 \\ \text{Number of Bars, } n_v &= 2 \\ \text{Vertical Reinforcement, } A_{sv} &= A_{sbv} * n_v = 0.62 \text{ in}^2 \\ \text{Provided Spacing between Bars, } s &= 10.00 \text{ in} \end{aligned}$$

Vertical Reinforcement (According to Eq.A4 of ACI318),

$$VL = \frac{A_{sv}}{b * s} * \sin(90 - \alpha) = 0.00177$$

2. Horizontal Reinforcement

$$\begin{aligned} \text{Provided Reinforcement, Bar} &= \text{SEL("ACI/Bar"; Bar;)} = \text{No.5} \\ \text{Provided Reinforcement, } A_{sbh} &= \text{TAB("ACI/Bar"; Asb; Bar=Bar)} = 0.31 \text{ in}^2 \\ \text{Number of Bars, } n_h &= 2 \\ \text{Vertical Reinforcement, } A_{sh} &= A_{sbh} * n_h = 0.62 \text{ in}^2 \\ \text{Provided Spacing between Bars, } s &= 10.00 \text{ in} \end{aligned}$$

Horizontal Reinforcement (According to Eq.A4 of ACI318),

$$HZ = \frac{A_{sh}}{b * s} * \sin(\alpha) = 0.00188$$

$$\text{Check Validity} = \text{IF}(VL + HZ > 0.003; \text{"Valid"; "Invalid"}) = \text{Valid}$$



Chapter 1: Concrete Design

Continuous Deep Beam by Strut-and-Tie Model

ACI 318

Page: 64

Calculation of Tension Reinforcement for Tie Connecting Joint I-IIa

Required Reinforcement Area, A_{sreq}	$\frac{F_{iiva} * 1000}{\phi * f_y}$	=	11.30 in ²
Provided Reinforcement, Bar	SEL("ACI/Bar"; Bar;)	=	No.9
Number of Bars, n			12.00
Provided Reinforcement, A_{sb}	TAB("ACI/Bar"; Asb; Bar=Bar)	=	1.00 in ²
Total Provided Area, A_{sprov}	n * Asb	=	12.00 in ²
Check Validity	IF(Asprov>Asreq; "Valid"; "Invalid")	=	Valid

Design Summary

Provided Vertical Reinforcement, A_{sv}	A_{sv}	=	0.62 in ²
Provided Horizontal Reinforcement, A_{sh}	A_{sh}	=	0.62 in ²
Provided Tension Reinforcement, A_{sprov}	A_{sprov}	=	12.00 in ²



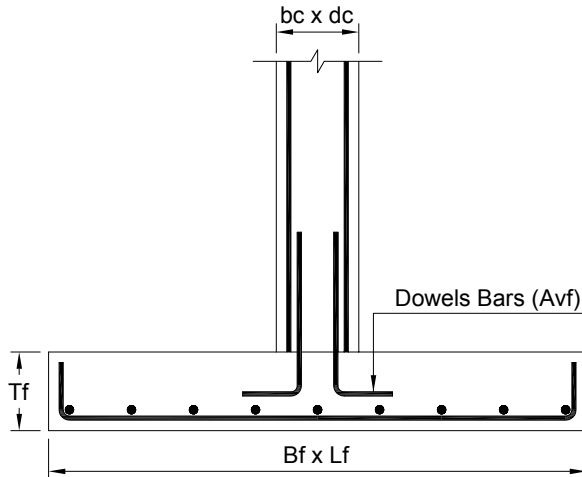
Chapter 1: Concrete Design

Transfer of Horizontal Force at Base of Column

ACI 318

Page: 65

Design for Transfer of Horizontal Force at Base of Column where The Footing Surface is not Intentionally Roughened as per ACI 318-11 Chapter 12



System

Column Width, b_c =	12.0 in
Column Depth, d_c =	12.0 in
Footing Width, B_f =	9.0 ft
Footing Length, L_f =	9.0 ft
Footing Thickness, T_f =	22.0 in

Load

Ultimate Horizontal Force at the Base of Column, V_u =	84.0 kips
--	-----------

Material Properties

Concrete Strength, f'_c =	4000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), $\mu = 0.6 * \lambda$	= 0.60

Check on Maximum Shear Transfer Permitted

Nominal Shear Force (According to Cl.11.6.5 of ACI318),		
ΦV_{n1} =	$\Phi * (0.2 * f'_c / 1000 * b_c * d_c)$	= 86.4 kips
ΦV_{n2} =	$\Phi * (800 * b_c * d_c) / 1000$	= 86.4 kips
Minimum Nominal Shear, ΦV_n =	$\text{MIN}(\Phi V_{n1}; \Phi V_{n2};)$	= 86.4 kips
Check Validity=	$\text{IF}(V_u < \Phi V_n; \text{"Valid"; "Increase Dimension"})$	= Valid



Chapter 1: Concrete Design

Transfer of Horizontal Force at Base of Column

ACI 318

Page: 66

Required Area of Reinforcement (According to Eq.11-25 of ACI318),

$$A_{vf} = \frac{V_u * 1000}{\Phi * f_y * \mu} = 3.11 \text{ in}^2$$

Provided Shear Reinforcement, Bar= SEL("ACI/Bar"; Bar;) = No.8

Diameter of Bars, Dia= TAB("ACI/Bar"; Dia; Bar=Bar) = 1.0000 in

Number of Bars, n= 4

$$\text{Provided Area of Reinforcement, } A_s = n * \frac{\pi * \text{Dia}^2}{4} = 3.14 \text{ in}^2$$

Check Validity= IF($A_s > A_{vf}$; "Valid"; "Increase RFT") = Valid

Check on Development Length of Tensile Reinforcement with Column

Clear Cover to Center of Bars, c= 3.25 in

Center to Center Bar Spacing, S= 4.50 in

Factor of, cb= MIN(c+Dia/2; S/2) = 2.25 in

(According to Cl.12.2.3 of ACI318) Factor of, Ktr= 0.00

(According to Cl.12.2.4 of ACI318) Factor of, Ψ_t = 1.00

(According to Cl.12.2.4 of ACI318) Factor of, Ψ_e = 1.00

(According to Cl.12.2.4 of ACI318) Factor of, Ψ_s = 1.00

Development Length within Column

Development Length (According to Eq.12-1 of ACI318),

$$L_{d1} = \frac{3}{40} * \frac{f_y}{\lambda * \sqrt{f_c}} * \frac{\Psi_t * \Psi_e * \Psi_s}{(cb + Ktr) / \text{Dia}} * \text{Dia} = 31.6 \text{ in}$$

Development Length within Footing

Development Length (According to Cl.12.5.2 of ACI318),

$$L_{d2} = \frac{0.02 * \Psi_e * f_y}{\lambda * \sqrt{f_c}} * \text{Dia} = 19.0 \text{ in}$$

Design Summary

Provided Area of Reinforcement, A_s = A_s = 3.14 in²

Development Length within Column, L_{d1} = L_{d1} = 31.6 in

Development Length within Footing, L_{d2} = L_{d2} = 19.0 in



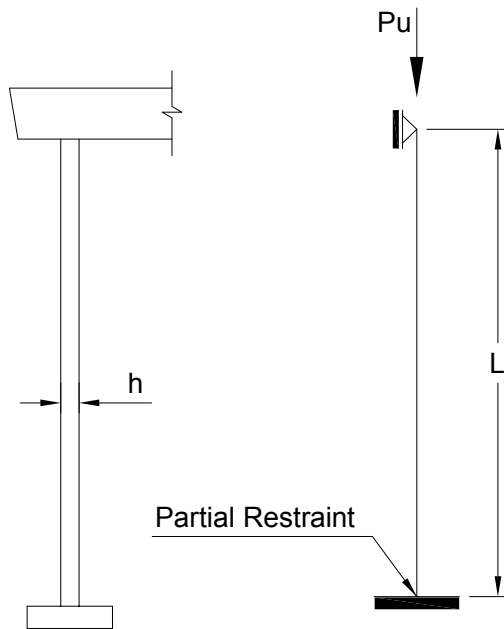
Chapter 1: Concrete Design

Bearing Wall by Empirical Method

ACI 318

Page: 67

Design of Bearing Wall by Empirical Method as per ACI 318-11 Chapters 10 & 14



System

Height of Wall, $L =$	15 ft
Spacing of Wall Panels, $s_p =$	8 ft
Width of Stem for Bearing Wall, $b_w =$	7 in

Load

Service Dead Load, $P_D =$	28 kips
Service Live Load, $P_L =$	14 kips
Ultimate Load, $P_u =$	$1.2 * P_D + 1.6 * P_L = 56$ kips

Material Properties

Concrete Strength, $f'_c =$	4000 psi
Bearing Strength Reduction Factor (According to Cl.9.3.2 of ACI318), $\Phi =$	0.65
Modification Factor for Lightweight Concrete, $\lambda =$	1.00

Determine Wall Thickness

Assume Wall Thickness, $h =$	7.5 in
Minimum Wall Thickness, $h_{min} = \text{MAX}(L * 12 / 25 ; 4)$	$= 7.2$ in
Check Validation $=$	$\text{IF}(h > h_{min}; \text{"O.K."}; \text{"Increase Thickness"}) = \text{O.K.}$



Chapter 1: Concrete Design

Bearing Wall by Empirical Method

ACI 318

Page: 68

Check Concrete Bearing Strength

$$\text{Loaded Area, } A_1 = h * b_w = 52.50 \text{ in}^2$$

Nominal Concrete Bearing Capacity (According to Cl.10.14.1 of ACI318),

$$\Phi V_b = \Phi * 0.85 * f'_c * A_1 / 1000 = 116 \text{ kips}$$

$$\text{Check Validation} = \text{IF}(\Phi V_b > P_u; \text{"Valid."}; \text{"Invalid"}) = \text{Valid.}$$

Calculate Design Strength of Wall

$$\text{Effective Width of Wall, } w = \text{MIN}(b_w + 4 * h; s_p * 12) = 37 \text{ in}$$

Wall Resistant Type,

Type-1 : Restrained Rotation - One or Both Ends (T/B/Both)

Type-2 : Unrestrained Rotation at Both Ends

Type-3 : For Walls not Braced Against Lateral Translation

$$\text{Type} = \text{SEL}(\text{"ACI/K"}; \text{Type};) = \text{Type-1}$$

$$\text{Effective Length Factor, } K = \text{TAB}(\text{"ACI/K"}; K; \text{Type} = \text{Type}) = 0.80$$

Nominal Strength of Wall (According to Eq.14-1 of ACI 318),

$$\Phi P_n = 0.55 * \Phi * f'_c * w * h * \frac{1 - \left(\frac{K * L * 12}{32 * h} \right)^2}{1000} = 254 \text{ kips}$$

$$\text{Check Validity} = \text{IF}(\Phi P_n > P_u; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Determine Single Layer of Reinforcement

Vertical Area of Reinforcement for Wall (According to Cl.14.3.2 of ACI318),

$$A_{sv} = 0.0012 * 12 * h = 0.108 \text{ in}^2 / \text{ft}$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; A_{sb}; \text{Bar} = \text{Bar}) = 0.20 \text{ in}^2$$

$$\text{Bar Spacing, } s = 18 \text{ in}$$

$$A_{sv_Prov} = A_{sb} * 12 / s = 0.13 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{sv_Prov} > A_{sv}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Horizontal Area of Reinforcement for Wall (According to Cl.14.3.3 of ACI318),

$$A_{sh} = 0.0020 * 12 * h = 0.180 \text{ in}^2 / \text{ft}$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; A_{sb}; \text{Bar} = \text{Bar}) = 0.20 \text{ in}^2$$

$$\text{Bar Spacing, } s = 12 \text{ in}$$

$$A_{sh_Prov} = A_{sb} * 12 / s = 0.20 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{sh_Prov} > A_{sh}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$



Chapter 1: Concrete Design

Bearing Wall by Empirical Method

ACI 318

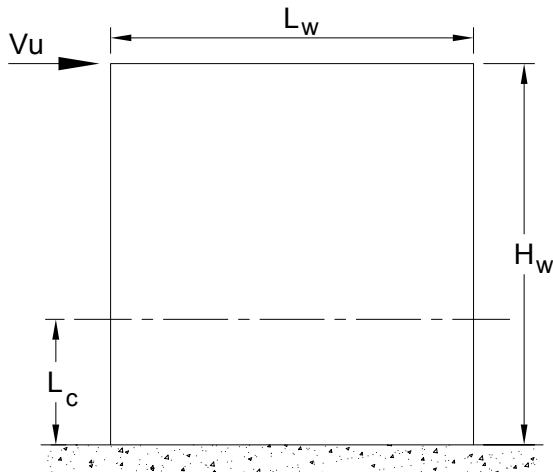
Page: 69

Design Summary

Wall Thickness, h=	h	=	8 in
Length of Footing, L=	L	=	15 ft
Vertical Area of Reinforcement for Wall, $A_{sv_Prov} = A_{sv_Prov}$		=	0.13 in ²
Horizontal Area of Reinforcement for Wall, $A_{sh_Prov} = A_{sh_Prov}$		=	0.20 in ²



Shear Design of Wall as per ACI 318-11 Chapter 11



System

Height of Wall, h_w =			12.0 ft
Width of Wall, L_w =			8.0 ft
Over All Wall Depth, d =	$0.8 * L_w$	=	6.4 ft
Thickness of Wall, h =			8.0 in
Concrete Cover, co =			2.0 in
Effective Depth of Wall Section, d_c =	$h - co = 8.0 - 2.0$	=	6.0 in

Load

Ultimate Bending Moment, M_u =			19200 kip*ft
Ultimate Shear Force, V_u =			200 kips
Ultimate Normal Force, N_u =			0 kips

Material Properties

Concrete Strength, f'_c =			3000 psi
Yield Strength of Reinforcement, f_y =			60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =			0.75
Modification Factor for Lightweight Concrete, λ =			1.00



Chapter 1: Concrete Design

Shear Design of Wall

ACI 318

Page: 71

Check Shear Reinforcement Requirement

Maximum Shear Strength of Wall (According to Cl.11.9.3 of ACI318),

$$\Phi V_n = \Phi * 10 * \sqrt{f'_c} * h * d * 12 / 1000 = 252 \text{ kips}$$

$$\text{Check Validity} = \text{IF}(V_u \leq \Phi V_n, \text{"Valid"}, \text{"Invalid"}) = \text{Valid}$$

$$\text{Critical Section of Shear Force, } L_c = \text{MIN}(L_w/2; h_w/2) = 4.00 \text{ ft}$$

Concrete Shear Strength (According to Eq.11-27 of ACI318),

$$V_{c1} = 3.3 * \lambda * \sqrt{f'_c} * \frac{h * d * 12}{1000} + \frac{N_u * d}{4 * L_w} = 111 \text{ kips}$$

Concrete Shear Strength (According to Eq.11-28 of ACI318),

$$V_{c2} = \left(0.6 * \lambda * \sqrt{f'_c} + \frac{L_w * 12 * \left(1.25 * \lambda * \sqrt{f'_c} + \frac{0.2 * N_u}{L_w * 12 * h} \right)}{M_u / V_u - L_w * 12 / 2} \right) * \frac{h * d * 12}{1000} = 104 \text{ kips}$$

$$\text{Concrete Shear Strength, } V_c = \text{MIN}(V_{c1}; V_{c2}) = 104 \text{ kips}$$

$$\text{Shear Reinforcement: } \text{IF}(V_u < \Phi * V_c / 2, \text{"Not Required"}, \text{"Required"}) = \text{Required}$$

Determine Horizontal Shear Reinforcement

$$\text{Identification of, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; A_{sb}; \text{Bar}=\text{Bar}) = 0.20 \text{ in}^2$$

$$\text{Number of Bars, } n = 2$$

$$\text{Area of Shear Reinforcement, } A_h = n * A_{sb} = 0.40 \text{ in}^2$$

Spacing between Bars (According to Eq.11-29 of ACI318),

$$s_{hi} = \frac{\Phi * f_y / 1000 * d * 12 * A_h}{V_u - \Phi * V_c} = 11.3 \text{ in}$$

$$\text{Provided Reinforcement Spacing, } s_h = 10 \text{ in}$$

$$\text{Check Validity} = \text{IF}(s_h \leq s_{hi}, \text{"Valid"}, \text{"Invalid"}) = \text{Valid}$$

Ratio of Horizontal Shear Reinforcement (According to Cl.11.9.9.2 of ACI318),

$$\rho_{hi} = \frac{A_h}{h * s_h} = 0.005$$

$$\rho_h = \text{MAX}(\rho_{hi}; 0.0025) = 0.005$$



Chapter 1: Concrete Design

Shear Design of Wall

ACI 318

Page: 72

Calculation of Vertical Shear Reinforcement

Ratio of Vertical Shear Reinforcement (According to Eq.11-30 of ACI318),

$$\rho_{vi} = 0.0025 + 0.5 * \left(2.5 - \frac{h_w}{L_w} \right) * (\rho_h - 0.0025) = 0.0037$$

$$\rho_v = \text{MAX}(\rho_{vi}; 0.0025) = 0.0037$$

$$\text{Identification of, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.20 \text{ in}^2$$

$$\text{Number of Bars, } n = 2$$

$$\text{Area of Shear Reinforcement, } A_v = n * A_{sb} = 0.40 \text{ in}^2$$

Spacing between Bars (According to Eq.11-29 of ACI318),

$$s_{vi} = \frac{A_v}{\rho_v * h} = \frac{0.40}{0.0037 * 8.0} = 13.5 \text{ in}$$

$$\text{Provided Reinforcement Spacing, } s_v = 13 \text{ in}$$

$$\text{Check Validity} = \text{IF}(s_v \leq s_{vi}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Design Summary

$$\text{Horizontal Shear Reinforcement, } A_h = A_h = 0.40 \text{ in}^2$$

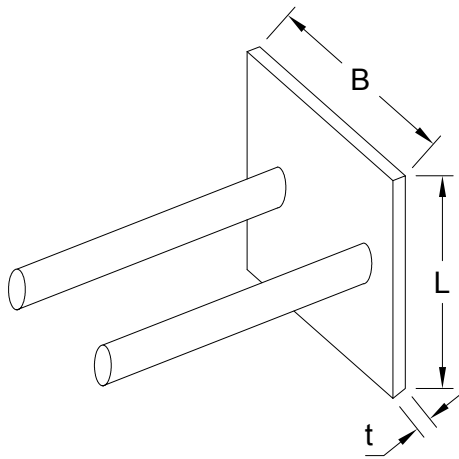
$$\text{Spacing Between Horizontal Shear Reinforcement, } s_h = s_h = 10 \text{ in}$$

$$\text{Vertical Shear Reinforcement, } A_v = A_v = 0.40 \text{ in}^2$$

$$\text{Spacing Between Horizontal Shear Reinforcement, } s_v = s_v = 13 \text{ in}$$



Design of Shear Friction as per ACI 318-11 Chapter 11



System

Width of Steel Plate, B=			2.00 in
Length of Steel Plate, L=			4.00 in
Thickness of Steel Plate, t=			0.25 in
Identification of, Bar=	SEL("ACI/Bar" ;Bar;)	=	No.3
Diameter of Bars, d_b =	TAB("ACI/Bar" ;Dia ;Bar=Bar)	=	0.38 in
Number of Bars, n=			2

Load

Ultimate Shear Force, V_u =			3570 lb
-------------------------------	--	--	---------

Material Properties

Concrete Strength, f'_c =			4000 psi
Yield Strength of Reinforcement, f_y =			60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =			0.75
Modification Factor for Lightweight Concrete, λ =			0.75
Friction Factor (According to Cl.11.6.4.3 of ACI318), $\mu= 0.7 * \lambda$		=	0.525



Chapter 1: Concrete Design

Shear Friction

ACI 318

Page: 74

Calculation of Required Reinforcement Area

Area of Shear Friction Reinforcement (According to Eq.11-25 of ACI318),

$$A_{vf} = \frac{V_u}{\Phi * f_y * \mu} = 0.151 \text{ in}^2$$

$$\text{Provided Area, } A_{act} = n * \frac{\pi * d_b^2}{4} = 0.23 \text{ in}^2$$

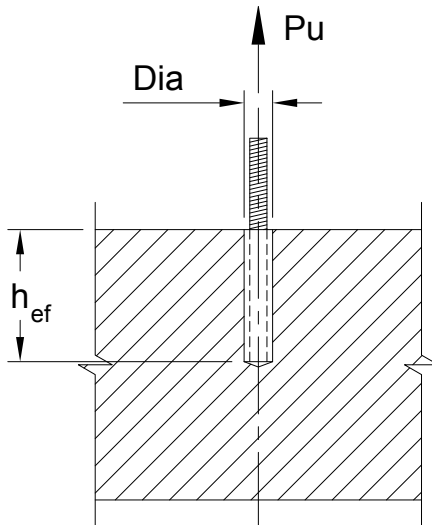
$$\text{Check Validity} = \text{IF}(A_{act} > A_{vf}; \text{"Valid"} ; \text{"Invalid"}) = \text{Valid}$$

Design Summary

$$\text{Provided Area of Reinforcement, } A_{act} = A_{act} = 0.23 \text{ in}^2$$



Design a Single Adhesive Anchor in Tension Away from Edges as per ACI 318-11 Appendix D



System

Diameter of Adhesive Anchor Bolt, Dia=	SEL("ACI/Anchor"; Dia;)	=	0.500 in
Area of Adhesive Anchor Bolt, A_{se_N} =	TAB("ACI/Anchor"; Ase; Dia=Dia)	=	0.142 in ²
Effective Embedment Length, h_{ef} =			4.0 in

Material Properties

Concrete Strength, f'_c =			4000 psi
Characteristic Bond Stress in Cracked Concrete, τ_{cr} =			300 psi
Characteristic Bond Stress in Uncracked Concrete, τ_{uncr} =			1000 psi
Tensile Strength of Anchor Bolt Grade, f_{uta} =			58000 psi
Strength Reduction Factor (According to Cl.D.4.4.a of ACI318), Φ_1 =			0.75
Strength Reduction Factor (According to Cl.D.4.4.c of ACI318), Φ_2 =			0.45
Modification Factor for Lightweight Concrete, λ =			1.00

Determine The Steel Strength of Adhesive Anchor

The Steel Strength of Anchor Bolt (According to Cl.D.4.1.1 of ACI318),

$$\Phi N_{sa} = \Phi_1 * A_{se_N} * f_{uta} = 6177 \text{ lb}$$



Chapter 1: Concrete Design

Single Adhesive Anchor in Tension

ACI 318

Page: 76

Determine The Bond Strength of Adhesive Anchor

$$\text{(According to Eq.D-21 of ACI318), } c_{Na} = 10 * \text{Dia} * \sqrt{\tau_{uncr} / 1100} = 4.77 \text{ in}$$

$$\text{(According to Eq.D-20 of ACI318), } A_{Nao} = (2 * c_{Na})^2 = 91.0 \text{ in}^2$$

$$\text{(According to Cl.D.5.5.1 of ACI318), } A_{Na} = A_{Nao} = 91.0 \text{ in}^2$$

The Basic Bond Strength (According to Eq.D-22 of ACI318),

$$N_{ba} = \lambda * \tau_{cr} * \pi * \text{Dia} * h_{ef} = 1885 \text{ lb}$$

$$\text{Factor (According to Cl.D.5.5.3 of ACI318), } \psi_{ed,Na} = 1.00$$

$$\text{Factor (According to Cl.D.5.5.5 of ACI318), } \psi_{c,Na} = 1.00$$

The Basic Bond Strength for A Single Anchor (According to Eq.D-3 of ACI318),

$$\Phi N_a = \Phi_2 * (A_{Na} / A_{Nao}) * \psi_{ed,Na} * \psi_{c,Na} * N_{ba} = 848 \text{ lb}$$

Determine The Concrete Breakout Strength

$$\text{(According to Eq.D-6 of ACI318), } \kappa_c = 17.0$$

Basic Strength of Concrete Breakout (According to Eq.D-6 of ACI318),

$$N_a = \kappa_c * \lambda * \sqrt{f'_c} * h_{ef}^{1.5} = 8601 \text{ lb}$$

$$\text{Factor (According to Cl.D.5.2.6 of ACI318), } \psi_{cp,Na} = 1.00$$

The Strength of Concrete Breakout (According to Eq.D-3 of ACI318),

$$\Phi N_{cb} = \Phi_2 * (A_{Na} / A_{Nao}) * \psi_{ed,Na} * \psi_{c,Na} * \psi_{cp,Na} * N_a = 3870 \text{ lb}$$

Determine The Tension Force Carried by Adhesive Anchor Bolt

$$\text{The Tension Force Carried by Adhesive Anchor, } T_u = \text{MIN}(\Phi N_{sa}; \Phi N_a; \Phi N_{cb}) = 848 \text{ lb}$$

Design Summary

$$\text{The Steel Strength of Adhesive Anchor Bolt, } \Phi N_{sa} = \Phi N_{sa} = 6177 \text{ lb}$$

$$\text{The Bond Strength of Adhesive Anchor Bolt, } \Phi N_a = \Phi N_a = 848 \text{ lb}$$

$$\text{The Concrete Breakout Strength of Adhesive Anchor Bolt, } \Phi N_{cb} = \Phi N_{cb} = 3870 \text{ lb}$$

$$\text{The Tension Force Carried by Adhesive Anchor, } T_u = T_u = 848 \text{ lb}$$



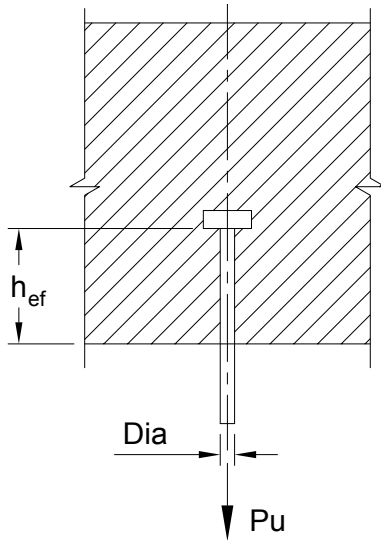
Chapter 1: Concrete Design

Single Headed Anchor Bolt in Tension

ACI 318

Page: 77

Design a Single Headed Anchor Bolt in Tension Away from Edges as per ACI 318-11 Appendix D



Load

Ultimate Load, $P_u =$ 7000 lb

Material Properties

Concrete Strength, $f'_c =$ 4000 psi

Tensile Strength of Anchor Bolt Grade, $f_{uta} =$ 58000 psi

Strength Reduction Factor (According to Cl.D.4.4.a of ACI318), $\Phi_1 =$ 0.75

Strength Reduction Factor (According to Cl.D.4.4.c of ACI318), $\Phi_2 =$ 0.70

Modification Factor for Lightweight Concrete, $\lambda =$ 1.00

Determine Anchor Diameter

Required Effective Area of Anchor Bolt (According to Eq.D.3 of ACI318),

$$A_{se_Req} = \frac{P_u}{\Phi_1 * 1.0 * f_{uta}} = 0.161 \text{ in}^2$$

Provided Anchor Bolt, Dia = SEL("ACI/Anchor"; Dia;) = 0.625 in

Provided Area of Anchor Bolt, $A_{se_Prov} =$ TAB("ACI/Anchor"; Ase; Dia=Dia) = 0.226 in²

Check Validity = IF($A_{se_Prov} \geq A_{se_Req}$; "Valid"; "Increase Dia") = Valid



Chapter 1: Concrete Design

Single Headed Anchor Bolt in Tension

ACI 318

Page: 78

Determine Emended Length

Factor (According to Cl.D.5.2.6 of ACI318), $\psi_{c,N}$ = 1.00

Effective Embedment Length (According to Cl.D.5.2.1 of ACI318),

$$h_{ef_Req} = \left(\frac{P_u}{\Phi_2 * \psi_{c,N} * 24 * \lambda * \sqrt{f'_c}} \right)^{2/3} = 3.51 \text{ in}$$

Provided Embedment Length, h_{ef_Prov} = 4.00 in

Check Validity = IF($h_{ef_Prov} \geq h_{ef_Req}$; "Valid"; "Increase h_{ef} ") = Valid

Determine Head Size

Factor (According to Cl.D.5.3.6 of ACI318), $\psi_{c,P}$ = 1.00

Required Head Size for Anchor Bolt (According to Eq.D-15 of ACI318),

$$A_{brg} = \frac{P_u}{\Phi_2 * \psi_{c,P} * 8 * f'_c} = 0.313 \text{ in}^2$$

Design Summary

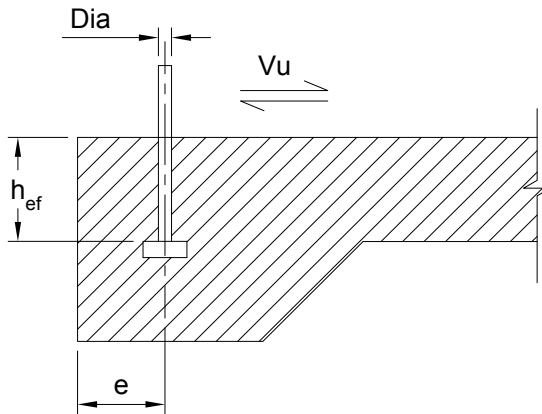
Diameter of Anchor Bolt, Dia = Dia = 0.625 in

Embedment Length of Anchor Bolt, h_{ef} = h_{ef_Prov} = 4.00 in

Head Size of Anchor Bolt, A_{brg} = A_{brg} = 0.313 in²



Design a Single Headed Anchor Bolt in Shear Near an Edge as per ACI 318-11 Appendix D



System

Edge Distance, $e =$ 1.75 in

Load

Ultimate Load, $V_u =$ 700 lb

Material Properties

Concrete Strength, $f'_c =$ 4000 psi

Tensile Strength of Anchor Bolt Grade, $f_{uta} =$ 58000 psi

Strength Reduction Factor (According to Cl.D.4.4.a of ACI318), $\Phi_1 =$ 0.65

Strength Reduction Factor (According to Cl.D.4.4.c of ACI318), $\Phi_2 =$ 0.70

Modification Factor for Lightweight Concrete, $\lambda =$ 1.00

Determine Anchor Diameter

Required Effective Area of Anchor Bolt (According to Eq.D.29 of ACI318),

$$A_{se_Req} = \frac{V_u}{\Phi_1 * 1.0 * 0.6 * f_{uta}} = 0.031 \text{ in}^2$$

Provided Anchor Bolt, $Dia =$ SEL("ACI/Anchor"; Dia;) = 0.500 in

Provided Area of Anchor Bolt, $A_{se_Prov} =$ TAB("ACI/Anchor"; Ase; Dia=Dia) = 0.142 in²

Check Validity= IF($A_{se_Prov} \geq A_{se_Req}$; "Valid"; "Increase Dia") = Valid



Calculation of Embedment Strength

Assume that, h_{ef_Prov} =		7.00 in
Ratio A_{vc}/A_{vco} , A' =		1.00
Factor (According to Cl.D.6 of ACI318), $\psi_{ed,V}$ =		1.00
Factor (According to Cl.D.6.2.7 of ACI318), $\psi_{c,V}$ =		1.00
Length of Load Bearing of Anchor Bolt (According to Cl.D.6.2.2 of ACI318), l_e =	$\text{MIN}(h_{ef_Prov}; 8 \cdot \text{Dia};)$	= 4.00 in
Basic Strength of Concrete Breakout (According to Eq.D-33 of ACI318), V_{b1} =	$7 \cdot \left(\frac{l_e}{\text{Dia}}\right)^{0.2} \cdot \sqrt{\text{Dia}} \cdot \lambda \cdot \sqrt{f_c} \cdot e^{1.5}$	= 1098 lb
Basic Strength of Concrete Breakout (According to Eq.D-34 of ACI318), V_{b2} =	$9 \cdot \lambda \cdot \sqrt{f_c} \cdot e^{1.5}$	= 1318 lb
Basic Strength of Concrete Breakout, $V_b = \text{MIN}(V_{b1}; V_{b2})$		= 1098 lb
Nominal Strength of Concrete Breakout (According to Eq.D-30 of ACI318), ΦV_{cb} =	$A' \cdot \Phi_2 \cdot \psi_{ed,V} \cdot \psi_{c,V} \cdot V_b$	= 769 lb
Check Validation=	$\text{IF}(V_u \leq \Phi V_{cb}; \text{"Valid"}; \text{"Invalid"})$	= Valid

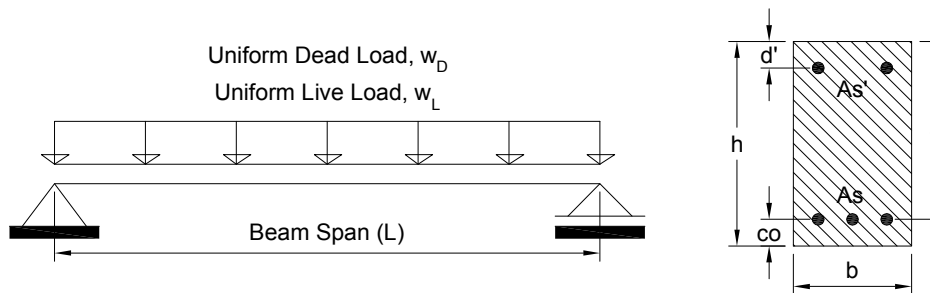
Design Summary

Diameter of Anchor Bolt, Dia =	Dia	= 0.500 in
Embedment Length of Anchor Bolt, $h_{ef} = h_{ef_Prov}$		= 7.00 in



Calculation of Deflection for Simple Support Concrete Beam Under Uniform Loads

As per ACI 318-11 Chapter 9



System

Width of Concrete Section, b =		12.0 in
Depth of Concrete Section, h =		22.0 in
Concrete Cover, co =		2.5 in
Effective Depth of Concrete Section, $d = h - co = 22.0 - 2.5$	=	19.5 in
Depth of Compression Reinforcement, d' =		2.5 in
Area of Tension Reinforcement, A_s =		1.80 in ²
Area of Compression Reinforcement, A_s' =		0.6 in ²
ρ =	$A_s / (b * d)$	= 0.0077
ρ' =	$A_s' / (b * d)$	= 0.0026
Distance from Centroidal Axis of Gross Section, $y_t = h / 2$		= 11.0 in
Beam Span, L =		25.0 ft

Load

Uniform Dead Load, w_D =		0.395 kip/ft
Uniform Live Load, w_L =		0.300 kip/ft
Percentage of Sustained Live Load, Sus =		50 %
Moment due to Dead Load, $M_D = w_D * L^2 / 8$	=	30.9 kip*ft
Moment due to Live Load, $M_L = w_L * L^2 / 8$	=	23.4 kip*ft
Sustained Moment, $M_{sus} = M_D + (Sus/100)*M_L$	=	42.6 kip*ft

Material Properties

Concrete Strength, f'_c =		3000 psi
Yield Strength of Reinforcement, f_y =		40000 psi
Modulus of Elasticity of Reinforcement, E_s =		29000000 psi
Modification Factor for Lightweight Concrete, λ =		1.00
Concrete Density, w_c =		150 psi



Properties of Cracked Section

Modulus of Rupture (According to Eq. 9-10 of ACI318), $f_r = 7.5 \lambda \sqrt{f'_c}$ = 411 psi

Modulus of Elasticity of Concrete (According to Cl. 8.5.1 of ACI318),

$$E_c = w_c^{1.5} * 33 * \sqrt{f'_c} = 3320561 \text{ psi}$$

$$n_s = E_s / E_c = 8.7$$

$$I_g = b * h^3 / 12 = 10648 \text{ in}^4$$

$$B = b / (n_s * A_s) = 0.77 \text{ in}$$

$$r = \frac{(n_s - 1) * A_s'}{n_s * A_s} = 0.295$$

$$kd = \frac{\sqrt{2 * d * B * \left(1 + r * \frac{d'}{d}\right) + (1 + r)^2} - (1 + r)}{B} = 5.76 \text{ in}$$

$$I_{cr} = \frac{b * kd^3}{3} + n_s * A_s * (d - kd)^2 + (n_s - 1) * A_s' * (kd - d')^2 = 3770 \text{ in}^4$$

Cracking Moment (According to Eq. 9-9 of ACI318),

$$M_{cr} = f_r * I_g / (y_t * 12000) = 33.2 \text{ kip*ft}$$

Properties of Effective Section

Effective Moment of Inertia (According to Eq 9-8 of ACI318):

$$I_{e_Dead1} = \left(\frac{M_{cr}}{M_D}\right)^3 * I_g + \left(1 - \left(\frac{M_{cr}}{M_D}\right)^3\right) * I_{cr} = 12301 \text{ in}^4$$

$$I_{e_Dead} = \text{MIN}(I_g ; I_{e_Dead1}) = 10648 \text{ in}^4$$

$$I_{e_Sus1} = \left(\frac{M_{cr}}{M_{sus}}\right)^3 * I_g + \left(1 - \left(\frac{M_{cr}}{M_{sus}}\right)^3\right) * I_{cr} = 7026 \text{ in}^4$$

$$I_{e_Sus} = \text{MIN}(I_g ; I_{e_Sus1}) = 7026 \text{ in}^4$$

$$I_{e_All1} = \left(\frac{M_{cr}}{M_D + M_L}\right)^3 * I_g + \left(1 - \left(\frac{M_{cr}}{M_D + M_L}\right)^3\right) * I_{cr} = 5342 \text{ in}^4$$

$$I_{e_All} = \text{MIN}(I_g ; I_{e_All1}) = 5342 \text{ in}^4$$



Short Term Deflection

$$\Delta_{i_Dead} = \frac{5 * M_D * L^2 * 12^3}{48 * E_c * I_{e_Dead} / 1000} = 0.098 \text{ in}$$

$$\Delta_{i_Sus} = \frac{5 * M_{sus} * L^2 * 12^3}{48 * E_c * I_{e_Sus} / 1000} = 0.205 \text{ in}$$

$$\Delta_{i_All} = \frac{5 * (M_D + M_L) * L^2 * 12^3}{48 * E_c * I_{e_All} / 1000} = 0.344 \text{ in}$$

$$\Delta_{i_Live} = \Delta_{i_All} - \Delta_{i_Dead} = 0.246 \text{ in}$$

Long Term Deflection

Duration of Sustained loads, Dur: SEL("ACI/Sustained";Dur;) = 5 Years or more

Time-Dependent Factor for Sustained Loads (According to Cl. 9.5.2.5 of ACI318):

$$\xi = \text{TAB}(\text{"ACI/Sustained";x;Dur=Dur; }) = 2.00$$

Multiplier Factor for Long-Term Deflection (According to Eq. 9-11 of ACI318),

$$\lambda_{\Delta} = \xi / (1 + 50 * \rho') = 1.77$$

$$\text{Creep and Shrinkage Deflection, } \Delta_{cp_sh} = \lambda_{\Delta} * \Delta_{i_Sus} = 0.36 \text{ in}$$

$$\Delta_{total} = \Delta_{cp_sh} + \Delta_{i_Live} = 0.61 \text{ in}$$

Calculation Summary

$$\text{Long Term Deflection, } \Delta_{total} = \Delta_{cp_sh} + \Delta_{i_Live} = 0.61 \text{ in}$$



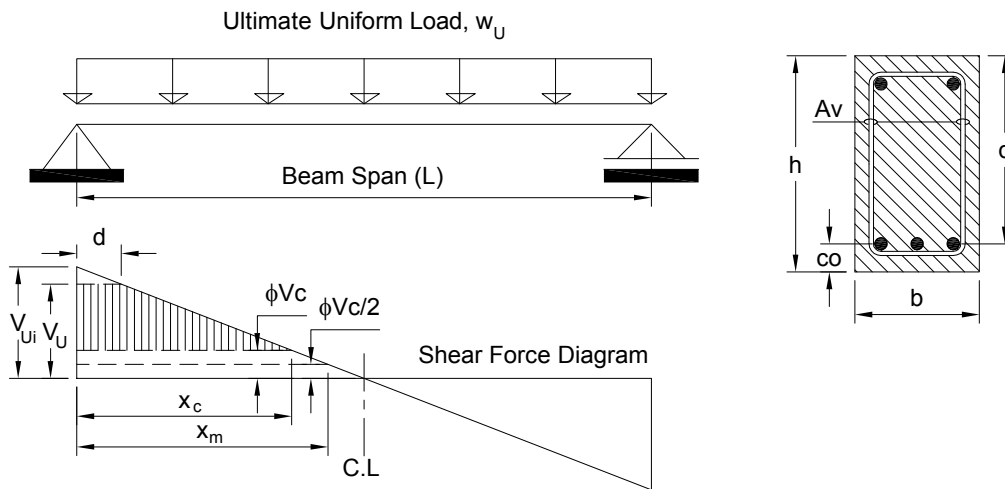
Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & M

ACI 318

Page: 84

Design of Shear Reinforcement for Section Subject to Shear & Flexure as per ACI318-11 Chapter 11



System

Width of Concrete Section, $b =$	13.0 in
Depth of Concrete Section, $h =$	22.5 in
Concrete Cover, $co =$	2.5 in
Effective Depth of Concrete Section, $d = h - co = 22.5 - 2.5$	$= 20.0$ in
Beam Span, $L =$	30.0 ft

Load

Ultimate Uniform Load, $w_u =$	4.5 kip/ft
Ultimate Shear Force at Support, $V_{ui} = w_u * L / 2$	$= 67.5$ kips
Ultimate Shear Force at Distance $[d]$ from Support, $V_u = V_{ui} - w_u * (d / 12)$	$= 60.0$ kips

Material Properties

Concrete Strength, $f'_c =$	3000 psi
Yield Strength of Reinforcement, $f_y =$	40000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), $\Phi =$	0.75
Modification Factor for Lightweight Concrete, $\lambda =$	1.00
Concrete Density, $w_c =$	150 psi

Determine Concrete Shear Strength

Nominal Shear Strength provided by Concrete (According to Eq. 11-3 of ACI318),

$$V_c = 2 * \lambda * \sqrt{f'_c} * \frac{b * d}{1000} = 28.5 \text{ kips}$$

Shear Reinforcement is : $IF(V_u > \Phi * V_c; \text{"Required"; "Not Required"}) = \text{Required}$



Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & M

ACI 318

Page: 85

Determine Area of Shear Reinforcement

Nominal Shear Strength provided by Reinforcement (According to Eq. 11-2 of ACI318),

$$V_s = \frac{V_u - \Phi * V_c}{\Phi} = 51.5 \text{ kips}$$

Maximum Allowable Shear Strength provided by Reinforcement (According to Cl.11.4.7.9 of ACI318),

$$V_{s_max} = 8 * \sqrt{f'_c} * \frac{b * d}{1000} = 113.9 \text{ kips}$$

$$\text{IF}(V_s > V_{s_max}; \text{"Increase Beam Dimension"; "OK"}) = \text{OK}$$

$$\text{Spacing of Provided Stirrups, } s = 6.0 \text{ in}$$

$$\text{Required Area of Reinforcement, } A_v = \frac{V_s * s * 1000}{f_y * d} = 0.39 \text{ in}^2$$

Minimum Area of Reinforcement (According to Cl.11.4.6.3 of ACI318),

$$A_{v_min1} = \frac{0.75 * \sqrt{f'_c} * b * s}{f_y} = 0.08 \text{ in}^2$$

$$A_{v_min2} = \frac{50 * b * s}{f_y} = 0.10 \text{ in}^2$$

$$A_{v_min} = \text{MAX}(A_{v_min1}; A_{v_min2}) = 0.10 \text{ in}^2$$

$$\text{Required Area of Reinforcement, } A_{vc_Req} = \text{MAX}(A_v; A_{v_min}) = 0.39 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"; Bar; }) = \text{No.4}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB}(\text{"ACI/Bar"; Asb; Bar=Bar}) = 0.20 \text{ in}^2$$

$$\text{Number of Stirrups, } n = 1$$

$$\text{Provided Area of Reinforcement, } A_{vc_Prov} = A_{sb} * n * 2 = 0.40 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{vc_Prov} \geq A_{vc_Req}; \text{"Valid"; "Invalid"}) = \text{Valid}$$

Determine Maximum Permissible Spacing of Stirrups

Allowable Shear Strength provided by Reinforcement for Spacing Limit (According to Cl.11.4.5.3 of ACI318),

$$V_{s_limit} = 4 * \lambda * \sqrt{f'_c} * \frac{b * d}{1000} = 57.0 \text{ kips}$$

$$\text{Factor for Maximum Spacing of Stirrups, } Fac = \text{IF}(V_s \leq V_{s_limit}; 1; 0.5) = 1.0$$

Maximum Spacing of Stirrups (According to Cl.11.4.5.1 of ACI318),

$$S_{max} = \text{MIN}(d/2; 24) * Fac = 10.00 \text{ in}$$

$$\text{Check Validity} = \text{IF}(s \leq S_{max}; \text{"Valid"; "Invalid"}) = \text{Valid}$$



Chapter 1: Concrete Design

Shear Reinforcement for Section Subject to Q & M

ACI 318

Page: 86

Determine Distribution Distance of Shear Reinforcement

Distance from Support beyond which Minimum Shear Reinforcement is Required,

$$x_c = \frac{V_{ui} - \Phi * V_c}{W_u} = 10.3 \text{ ft}$$

Distance from Support beyond which Concrete can carry Shear Force,

$$x_m = \frac{V_{ui} - \Phi * V_c / 2}{W_u} = 12.6 \text{ ft}$$

Design Summary

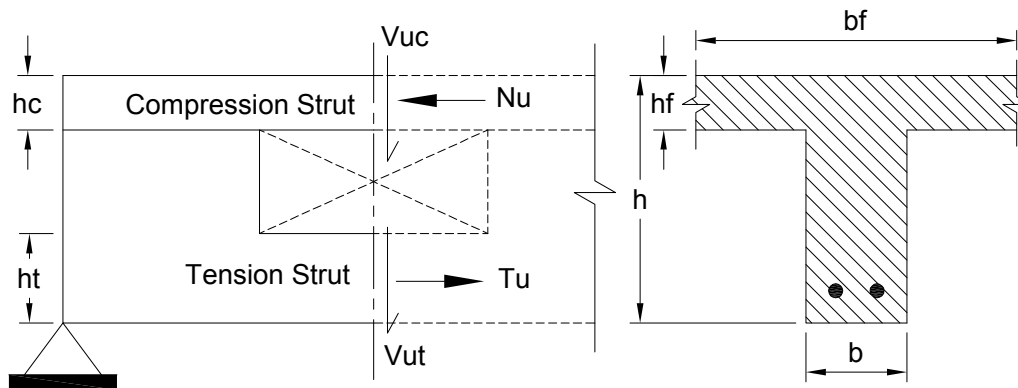
$$\text{Provided Area of Shear Reinforcement, } A_{vc_Prov} = A_{vc_Prov} = 0.40 \text{ in}^2$$

$$\text{Distance from Support beyond which Minimum Shear Reinforcement, } x_c = x_c = 10.3 \text{ ft}$$

$$\text{Distance from Support beyond which Concrete can carry Shear Force, } x_m = x_m = 12.6 \text{ ft}$$



Check Shear Reinforcement at Opening as per ACI 318-11 Chapter 11



System

Width of Beam, b =	4.3 in
Width of Top Flange, b_f =	48.0 in
Height of Beam, h =	26.0 in
Height of Compression Strut, h_c =	4.0 in
Height of Tension Strut, h_t =	12.0 in

Load

Ultimate Shear Force at Center of Opening, V_u =	7.2 kips
Ultimate Axial Tension Force in Tension Strut, T_u =	-10.8 kips
Ultimate Axial Compression Force in Compression Strut, N_u =	60.0 kips
Ultimate Shear Force in Tension Strut, V_{ut} =	6.0 kips
Ultimate Shear Force in Compression Strut, V_{uc} =	5.4 kips

Material Properties

Concrete Strength for Beam, f'_{c1} =	6000 psi
Concrete Strength for Topping, f'_{c2} =	3000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	1.00



Chapter 1: Concrete Design

Shear Reinforcement at Opening

ACI 318

Page: 88

Calculation of Required Shear Reinforcement

Required Shear RFT, A_{v_Req} =	$\frac{V_u}{\Phi * f_y / 1000}$	=	0.16 in ²
Identification of, Bar=	SEL("ACI/Bar" ;Bar;)	=	No.3
Provided Reinforcement, A_{sb} =	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.11 in ²
Number of Bars, n=			2
Provided Shear Reinforcement, A_{v_Prov} = n * A_{sb}		=	0.22 in ²
Check Validity=	IF($A_{v_Prov} \geq A_{v_Req}$; "Valid"; "Invalid")	=	Valid

Calculation of Shear Reinforcement of Tensile Strut

Strut Depth, d_t =	$0.8 * h_t$	=	9.6 in
Concrete Shear Strength for Tensile Strut (According to Eq.11-8 of ACI318),			
V_{ct} =	$2 * \left(1 + \frac{T_u * 1000}{500 * b * h_t} \right) * \lambda * \frac{\sqrt{f_{c1}}}{1000} * b * d_t$	=	3.72 kips
Shear Reinforcement for Ten. Strut=IF($V_{ut} \leq \Phi * V_{ct}$;"Not Required";"Required")		=	Required
Spacing between Stirrups (According to Cl.11.4.5.1 of ACI318),			
s=	$0.75 * h_t$	=	9.00 in
Required RFT Area, A_{vt_Req} =	$\frac{(V_{ut} - \Phi * V_{ct}) * s}{\Phi * f_y * d_t / 1000}$	=	0.07 in ²
Identification of, Bar=	SEL("ACI/Bar" ;Bar;)	=	No.3
Provided Reinforcement, A_{sb} =	TAB("ACI/Bar"; Asb; Bar=Bar)	=	0.11 in ²
Number of Bars, n=			1
Provided Shear Reinforcement, A_{vt_Prov} = n * A_{sb}		=	0.11 in ²
Check Validity=	IF($A_{vt_Prov} \geq A_{vt_Req}$; "Valid"; "Invalid")	=	Valid

Calculation of Shear Reinforcement of Compression Strut

Strut Depth, d_c =	$0.8 * h_c$	=	3.2 in
Concrete Shear Strength for Tensile Strut (According to Eq.11-8 of ACI318),			
V_{cc} =	$2 * \left(1 + \frac{N_u * 1000}{2000 * b_f * h_c} \right) * \lambda * \frac{\sqrt{f_{c2}}}{1000} * b_f * d_c$	=	19.46 kips
Shear Reinforcement for Comp. Strut=IF($V_{uc} \leq \Phi * V_{cc}$;"Not Required";"Required")		=	Not Required



Chapter 1: Concrete Design

Shear Reinforcement at Opening

ACI 318

Page: 89

Spacing between Stirrups (According to Cl.11.4.5.1 of ACI318),

$$s = 0.75 * h_c = 3.00 \text{ in}$$

$$\text{Required RFT Area, } A_{vc_Req} = \frac{(V_{uc} - \Phi * V_{cc}) * s}{\Phi * f_y * d_c / 1000} = -0.19 \text{ in}^2$$

$$\text{Identification of, Bar} = \text{SEL("ACI/Bar" ; Bar;)} = \text{No.3}$$

$$\text{Provided Reinforcement, } A_{sb} = \text{TAB("ACI/Bar"; Asb; Bar=Bar)} = 0.11 \text{ in}^2$$

$$\text{Number of Bars, } n = 1$$

$$\text{Provided Shear Reinforcement, } A_{vc_Prov} = n * A_{sb} = 0.11 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{vc_Prov} \geq A_{vc_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

Design Summary

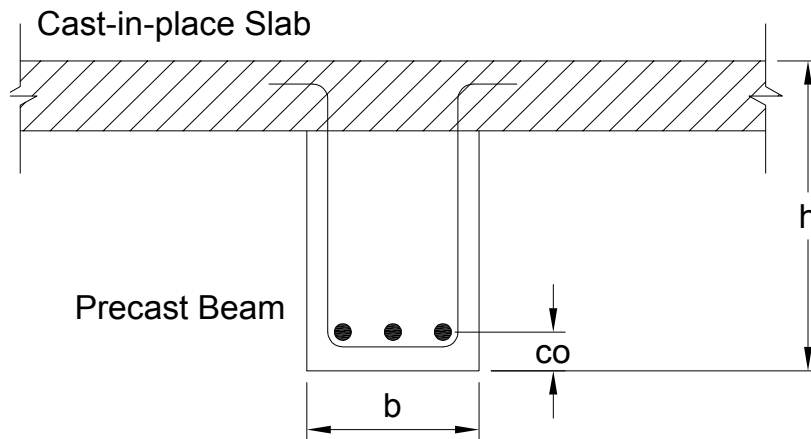
$$\text{Shear Reinforcement for Beam, } A_{v_Prov} = A_{v_Prov} = 0.22 \text{ in}$$

$$\text{Shear Reinforcement for Ten. Strut, } A_{vt_Prov} = \text{IF}(V_{ut} \leq \Phi * V_{ct}; \text{"Zero"} ; A_{vt_Prov}) = 0.11 \text{ in}^2$$

$$\text{Shear Reinforcement for Com. Strut, } A_{vc_Prov} = \text{IF}(V_{uc} \leq \Phi * V_{cc}; \text{"Zero"} ; A_{vc_Prov}) = \text{Zero}$$



Design of Horizontal Shear for Composite Slab and Precast Beam as per ACI 318-11 Chapters 11 & 17



System

Width of Beam, b =		10.0 in
Height of Beam, h =		20.5 in
Concrete Cover, co =		1.5 in
Depth of Beam, d =	$h - co$	= 19.0 in
Span of Simple Beam, L =		30.0 ft
Identification of, Bar=	SEL("ACI/Bar" ;Bar;)	= No.5
Diameter of Bars, d_b =	TAB("ACI/Bar" ;Dia ;Bar=Bar)	= 0.63 in
Number of Bars, n =		2

Load

Service Dead Load, W_D =		315 lb/ft
Service Live Load, W_L =		3370 lb/ft
Ultimate Load, W_u =	$1.2 * W_D + 1.6 * W_L$	= 5770 lb/ft

Material Properties

Concrete Strength, f'_c =		3000 psi
Yield Strength of Reinforcement, f_y =		60000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =		0.75
Modification Factor for Lightweight Concrete, λ =		1.00
Friction Factor (According to Cl.11.6.4.3 of ACI318), $\mu = 1.0 * \lambda$		= 1.00



Calculation of Horizontal Shear Reinforcement

Ultimate Shear Force at Distance (d) from Support

$$V_u = \frac{\left(W_u \cdot \frac{L}{2}\right) - \left(W_u \cdot \frac{d}{12}\right)}{1000} = 77.4 \text{ kips}$$

Horizontal Shear Strength (According to Cl.17.5.3 of ACI318),

$$\Phi V_{nh} = \frac{\Phi \cdot 500 \cdot b \cdot d}{1000} = 71.3 \text{ kips}$$

Horizontal Shear Reinforcement= IF($V_u \leq \Phi V_{nh}$; "Not Required"; "Required") = Required

Horizontal Shear Force Per one foot, v_{uh} = $\frac{V_u}{d \cdot b} = 0.407 \text{ ksi}$

Required RFT Area for Shear Friction, A_{vf} = $\frac{v_{uh} \cdot b \cdot 12}{\Phi \cdot f_y \cdot \mu / 1000} = 1.09 \text{ in}^2 / \text{ft}$

Spacing Between Links, s = $\frac{\pi \cdot n \cdot 12 \cdot d_b^2}{A_{vf} \cdot 4} = 6.9 \text{ in}$

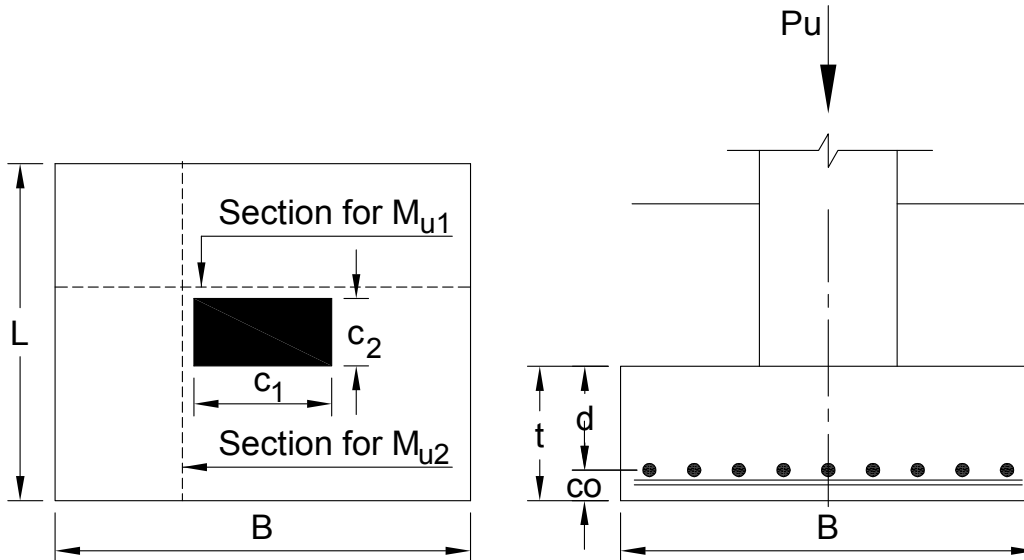
Design Summary

Spacing Between Links, s = $s = 6.9 \text{ in}$



Chapter 2: Foundation Design

Design of Reinforcement for Shallow Foundation as per ACI 318-11 Chapter 15



System

Width of Column, c_1 =		30.0 in
Length of Column, c_2 =		12.0 in
Width of Footing, B =		13 ft
Length of Footing, L =		13 ft
Area of Footing, A_f =	$B * L$	= 169 ft ²
Depth of Footing, t =		30.5 in
Concrete Cover, co =		2.5 in
Effective Depth of Footing, d =	$t-co$	= 28.0 in

Load

Service Dead Load, P_D =		350 kips
Service Live Load, P_L =		275 kips
Ultimate Load, P_u =	$1.2 * P_D + 1.6 * P_L$	= 860 kips
Ultimate Pressure, q_s =	P_u / A_f	= 5.09 ksf



Material Properties

Concrete Strength, f'_c =	3000 psi
Yield Strength of Reinforcement, f_y =	60000 psi
Tension Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.90

Determine Area of Reinforcement Distributed in Footing Width (B)

$$M_{u1} = q_s * B * \left(0.5 * \left(L - \frac{c_2}{12} \right) \right)^2 / 2 = 1191 \text{ kip*ft}$$

$$R_{n1} = \frac{M_{u1} * 12000}{\Phi * B * 12 * d^2} = 130 \text{ psi}$$

$$\rho_1 = \frac{0.85 * f'_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_{n1}}{0.85 * f'_c}} \right) = 0.0022$$

Minimum Reinforcement Ratio (According to Cl.7.12.2 of ACI318),

$$\rho_{min} = \text{IF}(f_y \leq 50000; 0.002; \text{IF}(f_y \geq 77143; 0.0014; 0.0018)) = 0.0018$$

$$\text{Required Area of Reinforcement, } A_{s1_Req} = \text{MAX}(\rho_{min}; \rho_1) * B * d * 12 = 9.61 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.8}$$

$$\text{Provided Reinforcement, } A_{sb1} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.79 \text{ in}^2$$

$$\text{Number of Bars, } n_1 = 13$$

$$\text{Provided Area of Reinforcement, } A_{s1_Prov} = n_1 * A_{sb1} = 10.27 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{s1_Prov} \geq A_{s1_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$



Chapter 2: Foundation Design

Reinforcement of Shallow Foundation

ACI 318

Page: 94

Determine Area of Reinforcement Distributed in Footing Length (L)

$$M_{u2} = q_s * L * \left(0.5 * \left(B - \frac{c_1}{12} \right) \right)^2 / 2 = 912 \text{ kip*ft}$$

$$R_{n2} = \frac{M_{u2} * 12000}{\phi * L * 12 * d^2} = 99 \text{ psi}$$

$$\rho_2 = \frac{0.85 * f'_c}{f_y} * \left(1 - \sqrt{1 - \frac{2 * R_{n2}}{0.85 * f'_c}} \right) = 0.0017$$

Minimum Reinforcement Ratio (According to Cl.7.12.2 of ACI318),

$$\rho_{min} = \text{IF}(f_y \leq 50000; 0.002; \text{IF}(f_y \geq 77143; 0.0014; 0.0018)) = 0.0018$$

$$\text{Required Area of Reinforcement, } A_{s2_Req} = \text{MAX}(\rho_{min}; \rho_2) * L * d * 12 = 7.86 \text{ in}^2$$

$$\text{Provided Reinforcement, Bar} = \text{SEL}(\text{"ACI/Bar"}; \text{Bar};) = \text{No.8}$$

$$\text{Provided Reinforcement, } A_{sb2} = \text{TAB}(\text{"ACI/Bar"}; \text{Asb}; \text{Bar}=\text{Bar}) = 0.79 \text{ in}^2$$

$$\text{Number of Bars, } n_2 = 11$$

$$\text{Provided Area of Reinforcement, } A_{s2_Prov} = n_2 * A_{sb2} = 8.69 \text{ in}^2$$

$$\text{Check Validity} = \text{IF}(A_{s2_Prov} \geq A_{s2_Req}; \text{"Valid"}; \text{"Invalid"}) = \text{Valid}$$

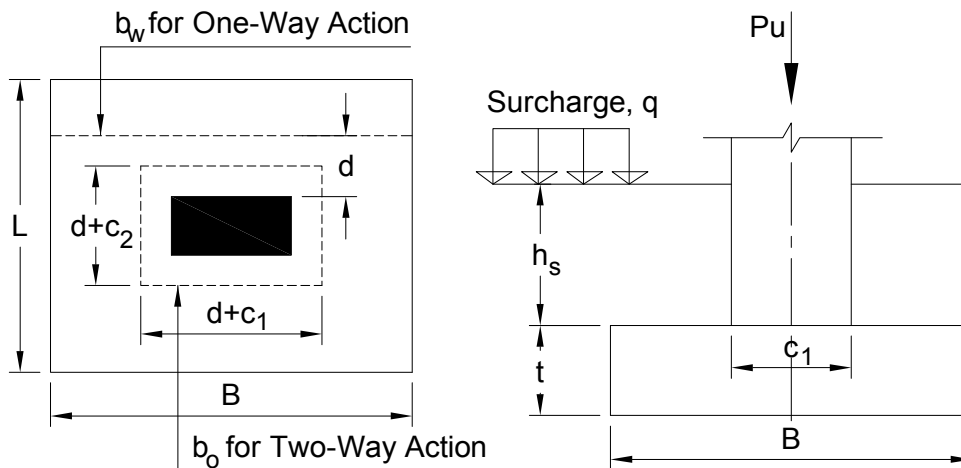
Design Summary

$$\text{Area of Reinforcement Distributed in Footing Width, } A_{s1} = A_{s1_Prov} = 10.27 \text{ in}^2$$

$$\text{Area of Reinforcement Distributed in Footing Length, } A_{s2} = A_{s2_Prov} = 8.69 \text{ in}^2$$



Design for Depth of Shallow Foundation as per ACI 318-11 Chapters 11 & 15



System

Width of Column, c_1 =	30.0 in
Length of Column, c_2 =	12.0 in
Concrete Cover, c_o =	5.0 in
Height of Soil above Footing, h_s =	5 ft

Load

Service Dead Load, P_D =	350 kips
Service Live Load, P_L =	275 kips
Ultimate Load, P_u =	$1.2 * P_D + 1.6 * P_L$ = 860 kips
Service Surcharge, q =	0.1 ksf
Allowable Soil Pressure at Bottom of Footing, P_a =	4.5 ksf
Average Weight of Soil and Concrete above Footing Base, w =	130.0 pcf

Material Properties

Concrete Strength, f'_c =	3000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	1.00



Calculation of Base Area

Net Allowable Soil Pressure, P_{na} =	$P_a - q - \frac{w * h_s}{1000}$	=	3.75 ksf
Required Area of Footing, A_f =	$\frac{P_D + P_L}{P_{na}}$	=	166.7 ft ²
Assume Width of Footing, B=			13 ft
Assume Length of Footing, L=			13 ft
Check Validity=	IF($A_f > L * B$; "Invalid"; "Valid")	=	Valid
Ultimate Pressure, q_s =	$P_u / (B * L)$	=	5.09 ksf

Calculation of Required Thickness for One-Way Action

Assume that Thickness of Footing, t=			33 in
Depth of Footing, d=	t - co	=	28 in
Critical Area of One-Way Shear, A_{1B} =	$B * \left(\frac{L - c_2 / 12}{2} - \frac{d}{12} \right)$	=	47.67 ft ²
Critical Area of One-Way Shear, A_{1L} =	$L * \left(\frac{B - c_1 / 12}{2} - \frac{d}{12} \right)$	=	37.92 ft ²
Critical Area of One-Way Shear, A_1 =	MAX(A_{1B} ; A_{1L})	=	47.67 ft ²
Width of Critical Section for One-Way Shear, b_w =	IF($A_{1B} > A_{1L}$; B; L)	=	13 ft
Ultimate Shear force at Critical Area Section, V_{u1} =	$q_s * A_1$	=	243 kips
Nominal Concrete Shear Strength, ΦV_c =	$\Phi * 2 * \lambda * \sqrt{f'_c} * \frac{b_w * 12 * d}{1000}$	=	359 kips
Check Validation =	IF($\Phi V_c > V_{u1}$; "O.K."; "Increase Depth")	=	O.K.

Calculation of Required Thickness for Two-Way Action

Critical Area of Two-Way Shear, A_2 =	$B * L - \left(\frac{(c_1 + d) * (c_2 + d)}{144} \right)$	=	152.89 ft ²
Ultimate Shear force at Critical Area Section, V_{u2} =	$q_s * A_2$	=	778.2 kips
Perimeter of Critical Section for Two-Way Shear, b_0 =	$2 * (c_1 + d) + 2 * (c_2 + d)$	=	196.0 in
Column Type=	SEL("ACI/Alfa S";Type;)	=	Interior
Alfa Constant, α_s =	TAB("ACI/AlfaS"; Alfa; Type=Type)	=	40.00
Ratio of Long to Short Column Dimensions, β =	MAX(c_1 ; c_2)/MIN(c_1 ; c_2)	=	2.50



Chapter 2: Foundation Design

Depth of Shallow Foundation

ACI 318

Page: 97

Concrete Shear Strength (According to Eq. 11-31 of ACI318),

$$V_{c1} = \left(2 + \frac{4}{\beta}\right) * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000} = 1082 \text{ kips}$$

Concrete Shear Strength (According to Eq. 11-32 of ACI318),

$$V_{c2} = \left(\alpha_s * \frac{d}{b_0} + 2\right) * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000} = 2319 \text{ kips}$$

Concrete Shear Strength (According to Eq. 11-33 of ACI318),

$$V_{c3} = 4 * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000} = 1202 \text{ kips}$$

$$\text{Nominal Concrete Shear Strength, } \Phi V_c = \Phi * \text{MIN}(V_{c1}; V_{c2}; V_{c3}) = 812 \text{ kips}$$

$$\text{Check Validation} = \text{IF}(\Phi V_c > V_{u2}; \text{"O.K."}; \text{"Increase Depth"}) = \text{O.K.}$$

Calculation Summary

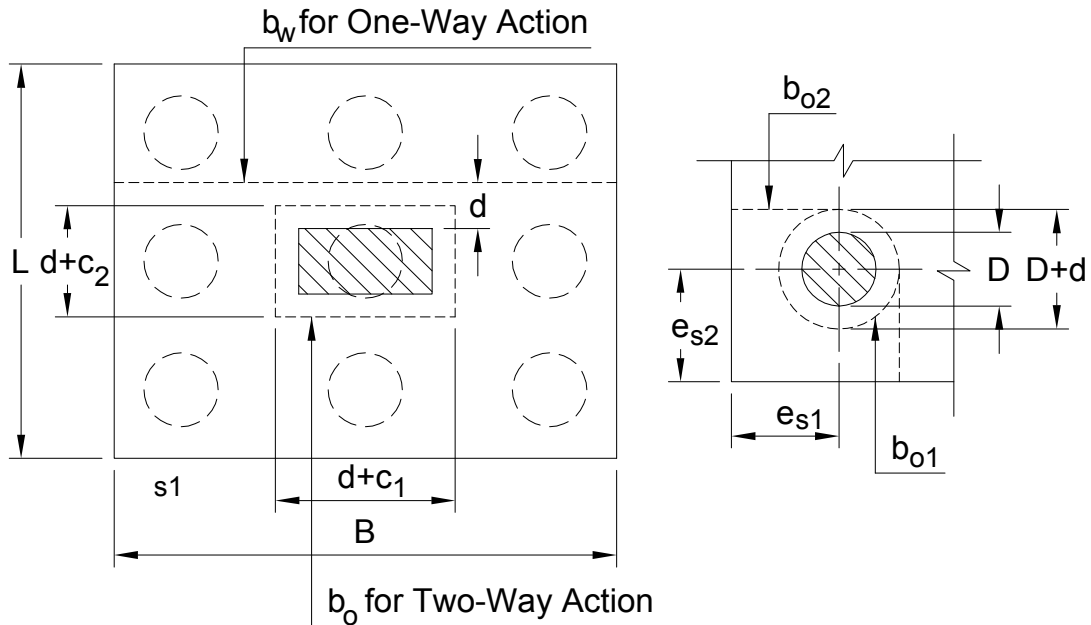
$$\text{Width of Footing, } B = B = 13 \text{ ft}$$

$$\text{Length of Footing, } L = L = 13 \text{ ft}$$

$$\text{Thickness of Footing, } t = t = 33 \text{ in}$$



Design Depth for Pile Cap as per ACI 318-11 Chapter 11



System

Width of Column, c_1 =	16.0 in
Length of Column, c_2 =	16.0 in
Pile Diameter, D =	12.0 in
Edge Distance for Corner Pile, e_{s1} =	15 in
Edge Distance for Corner Pile, e_{s2} =	15 in
Width of Pile Cap, B =	8.5 ft
Length of Pile Cap, L =	8.5 ft
Concrete Cover, c_o =	7.0 in

Load

Pile Service Dead Load, P_D =	20 kips
Pile Service Live Load, P_L =	10 kips
Ultimate Pile Load, $P_u = 1.2 * P_D + 1.6 * P_L$	= 40 kips

Material Properties

Concrete Strength, f'_c =	4000 psi
Shear Strength Reduction Factor (According to Cl.9.3.2 of ACI318), Φ =	0.75
Modification Factor for Lightweight Concrete, λ =	1.00



Calculation of Required Thickness due to One-Way Shear

Assume that Thickness of Pile Cap, t=		22 in
Depth of Pile Cap, d=	t - c _o	= 15 in
Width of Critical Section for One-Way Shear, b _w =	MIN(B ; L)	= 8.5 ft
Number of Piles fall within Critical Section for One-Way Action, n _{r1} =		3
Ultimate Shear force at Critical Area Section, V _{u1} =	P _u * n _{r1}	= 120 kips
Nominal Concrete Shear Strength, ΦV _c =	Φ * 2 * λ * √f _c * $\frac{b_w * 12 * d}{1000}$	= 145 kips
Check Validation =	IF(ΦV _c > V _{u1} ; "O.K."; "Increase Depth")	= O.K.

Calculation of Required Thickness due to Two-Way Shear for Group Piles

Perimeter of Critical Section for Two-Way Shear, b ₀ =	2*(c ₁ +d) + 2*(c ₂ +d)	= 124.0 in
Number of Piles fall within Critical Section for Two-Way Action, n _{r2} =		8
Ultimate Shear force at Critical Area Section, V _{u2} =	P _u * n _{r2}	= 320 kips
Column Type=	SEL("ACI/Alfa S";Type;)	= Interior
Alfa Constant, α _s =	TAB("ACI/AlfaS"; Alfa; Type=Type)	= 40.00
Ratio of Long to Short Column Dimensions, β=	MAX(c ₁ ;c ₂)/MIN(c ₁ ;c ₂)	= 1.00
Concrete Shear Strength (According to Eq. 11-31 of ACI318),		
V _{c1} =	$\left(2 + \frac{4}{\beta}\right) * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000}$	= 706 kips
Concrete Shear Strength (According to Eq. 11-32 of ACI318),		
V _{c2} =	$\left(\alpha_s * \frac{d}{b_0} + 2\right) * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000}$	= 804 kips
Concrete Shear Strength (According to Eq. 11-33 of ACI318),		
V _{c3} =	$4 * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000}$	= 471 kips
Nominal Concrete Shear Strength, ΦV _c =	Φ * MIN(V _{c1} ; V _{c2} ; V _{c3})	= 353 kips
Check Validation =	IF(ΦV _c > V _{u2} ; "O.K."; "Increase Depth")	= O.K.



Calculation of Required Thickness due to Two-Way Shear for Single Corner Pile

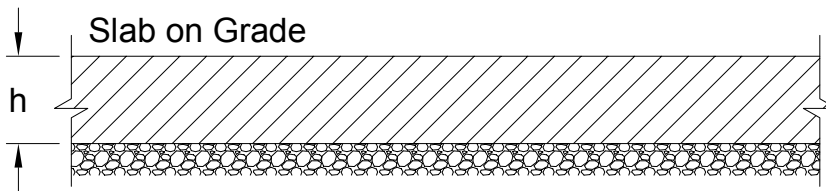
Perimeter of Critical Section for Two-Way Shear, $b_{01} = \pi * (D + d)$	=	84.8 in
Perimeter of Critical Section for Two-Way Shear, $b_{02} = \pi * (D+d)/4 + e_{s1} + e_{s2}$	=	51.2 in
Perimeter of Critical Section for Two-Way Shear, $b_0 = \text{MIN}(b_{01}; b_{02})$	=	51.2 in
Perimeter Ultimate Shear force at Critical Section, $V_{u3} = P_u * 1.0$	=	40 kips
Column Type=	SEL("ACI/Alfa S";Type;)	= Corner
Alfa Constant, $\alpha_s =$	TAB("ACI/AlfaS"; Alfa; Type=Type)	= 20.00
Ratio of Long to Short Column Dimensions, $\beta = \text{MAX}(c_1;c_2)/\text{MIN}(c_1;c_2)$	=	1.00
Concrete Shear Strength (According to Eq. 11-31 of ACI318), $V_{c1} = \left(2 + \frac{4}{\beta}\right) * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000}$	=	291 kips
Concrete Shear Strength (According to Eq. 11-32 of ACI318), $V_{c2} = \left(\alpha_s * \frac{d}{b_0} + 2\right) * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000}$	=	382 kips
Concrete Shear Strength (According to Eq. 11-33 of ACI318), $V_{c3} = 4 * \lambda * \sqrt{f_c} * \frac{b_0 * d}{1000}$	=	194 kips
Nominal Concrete Shear Strength, $\Phi V_c = \Phi * \text{MIN}(V_{c1}; V_{c2}; V_{c3})$	=	146 kips
Check Validation =	IF($\Phi V_c > V_{u3}$; "O.K."; "Increase Depth")	= O.K.

Calculation Summary

Thickness of Pile Cap, $t = t$	=	22 in
--------------------------------	---	-------



Design of Slab on Grade Due to Wheel Load as per ACI 360-10 Appendix 1



System

Thickness of Slab on Grade, h =	10.0 in
Spacing between Wheels, s =	40.0 in
Contact Area per Wheel, A_c =	50.0 in ²
Effective Contact Area per Wheel (According to Cl.A1.2 of ACI360), A_{c_eff} =	61.5 in ²

Load

Wheel Axle Load, P =	30 kips
------------------------	---------

Material Properties

Concrete Strength, f'_c =	4000 psi
Subgrade Modulus, K =	100 lb/in ³
Safety Factor, FS =	2.00

Checking Slab Thickness

Modulus of Rupture of Concrete, f_r =	$9 * \sqrt{f'_c}$	=	569.2 psi
Concrete Working Stress, f_{t_all} =	f_r / FS	=	284.6 psi
Slab Stress per 1000 lb Axle Load, f_t =	$f_{t_all} / (P/1.0)$	=	9.5 psi
Required Slab Thickness (According to Fig.A1.1 of ACI360), h_{min} =			9.92 in
Check Validation=	IF($h \geq h_{min}$; "Valid"; "Invalid")	=	Valid

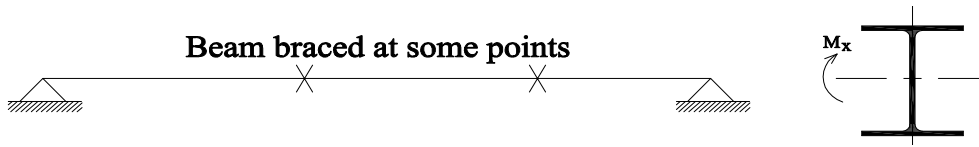
Design Summary

Thickness of Slab on Grade, h =	h	=	10.0 in
-----------------------------------	-----	---	---------



Chapter 3: Steel Design

Design of W-Shapes Subjected to Bending Moment about Strong Axis and Braced at Some Points



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	50 ksi
E =			29000 ksi

Beam Length and C_b

Total length, L =		35.00 ft
Unsupported length, L_b =		17.50 ft
From Table 3-1 (AISC), C_b =		1.50

Design Moments and Uniform Live Load

Ultimate moment, M_U =		200.00 kip*ft
Ultimate moment due to live load case, M_L =		140.00 kip*ft
Ultimate shear, Q_U =		30.00 kips

Section Details

sec.:	SEL("AISC/W"; NAME;)	=	W21X48
depth, d =	TAB("AISC/W"; d ; NAME=sec.)	=	20.60 in
Web th., t_w =	TAB("AISC/W"; t_w ; NAME=sec.)	=	0.35 in
Flange width, b_f =	TAB("AISC/W"; b_f ; NAME=sec.)	=	8.14 in
Flange th., t_f =	TAB("AISC/W"; t_f ; NAME=sec.)	=	0.43 in
Plastic sec. modulus, Z_x =	TAB("AISC/W"; Z_x ; NAME=sec.)	=	107.00 in ³
Elastic sec. modulus, S_x =	TAB("AISC/W"; S_x ; NAME=sec.)	=	93.00 in ³
Inertia about x-axis, I_x =	TAB("AISC/W"; I_x ; NAME=sec.)	=	959.00 in ⁴
r_y =	TAB("AISC/W"; r_y ; NAME=sec.)	=	1.66 in
r_{ts} =	TAB("AISC/W"; r_{ts} ; NAME=sec.)	=	2.05 in

(r_y is radius of gyration about y-axis and r_{ts} : is effective radius of gyration for the L.T.B.)



$$\begin{aligned} \text{Torsional constant, } J &= \text{TAB("AISC/W";J;NAME=sec.)} &= & 0.80 \text{ in}^4 \\ h_o &= \text{TAB("AISC/W";h_o;NAME=sec.)} &= & 20.20 \text{ in} \end{aligned}$$

(h_o : is the distance between C.L. of flanges)

AISC Specification Eqn. (F2-1):

$$\text{Yielding Moment, } M_p = Z_x * F_y * 1/12 = 446 \text{ kip*ft}$$

Element Classification

(1) Web:

$$h/t_w, \lambda_w = \text{TAB("AISC/W";h/t_w;NAME=sec.)} = 53.60$$

According to AISC Specification Table B4.1 Case 9, the limiting width-to-thickness ratio for the web is:

$$\text{Web_Class} = \text{IF}(\lambda_w \leq 3.76 * \sqrt{E/F_y}, \text{"Compact"; "Non-Compact"}) = \text{Compact}$$

(2) Comp. flange:

$$b_f/2t_f, \lambda_f = \text{TAB("AISC/W";b_f/2t_f;NAME=sec.)} = 9.47$$

According to AISC Specification Table B4.1 Case 1, the limiting width-to-thickness ratios for the compression flange are:

$$\lambda_{pf} = 0.38 * \sqrt{E/F_y} = 9$$

$$\lambda_{rf} = 1.00 * \sqrt{E/F_y} = 24$$

$$\text{FI_Class} = \text{IF}(\lambda_f \leq \lambda_{pf}, \text{"Compact"; IF}(\lambda_f > \lambda_{rf}, \text{"Slender"; "Non-Compact"})) = \text{Non-Compact}$$

The available strength provided by AISC Specification Sections F3.1 and F3.2, the nominal flexural moment is calculated as follows, satisfying the condition of compression Flange Local Buckling:

$$M_{n1a} = M_p - 0.7 * F_y * S_x * 1/12 = 175 \text{ kip*ft}$$

$$M_{n1} = \text{IF}(\text{FI_Class} = \text{"Compact"; } M_p; (M_p - M_{n1a} * \frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}})) = 441 \text{ kip*ft}$$

Lateral Torsional Buckling (LTB)

The limiting lengths L_p and L_r are determined according to the AISC Spec. Eqns. F2-5 and F2-6, as follows:

$$L_p = 1.76 * r_y * \sqrt{E/F_y} / 12 = 5.86 \text{ ft}$$

$$L_{r1} = \sqrt{\frac{J * 1.0}{S_x * h_o}} = 0.02$$

$$L_{r2} = \sqrt{1 + \sqrt{6.76 * \left(\frac{0.7 * F_y * S_x * h_o}{E * J * 1.0}\right)^2}} = 2.89$$

$$L_r = 1.95 / 12 * r_{ts} * \frac{E}{0.7 * F_y} * L_{r1} * L_{r2} = 15.95 \text{ ft}$$



Case= $\text{IF}(L_b > L_r, \text{"ELTB"}; \text{IF}(L_b \leq L_p, \text{"No LTB"}; \text{"InLTB"}))$ = ELTB
("ELTB" refers to elastic LTB. and "InLTB" refers to Inelastic LTB.)

According to the AISC Spec. Eqn. F2-2:

$M_1 = \text{MIN}(M_p; C_b * (M_p - (M_p - 0.7 * 1/12 * F_y * S_x) * (L_b - L_p) / (L_r - L_p)))$ = 367 kip*ft

According to the AISC Spec. Eqn. F2-4:

$F_{cr} = C_b * \pi^2 * E / ((L_b + 0.01) * 12 / r_{ts})^2$ = 40.87 ksi

$F_{cr,mod} = \sqrt{(1 + 0.078 * J * 1.0 / (S_x * h_o) * (L_b * 12 / r_{ts})^2)}$ = 1.16 ksi

According to the AISC Spec. Eqns. F2-3:

$M_2 = \text{MIN}(M_p; F_{cr} * S_x / 12 * F_{cr,mod})$ = 367 kip*ft

According to the AISC Spec. Eqn. F2-2:

$M_{n2} = \text{IF}(\text{Case} = \text{"No LTB"}; M_p; \text{IF}(\text{Case} = \text{"InLTB"}; M_1; M_2))$ = 367 kip*ft

Check The Available Flexure Strength

$\Phi M_n = 0.90 * \text{MIN}(M_p; M_{n1}; M_{n2})$ = 330 kip*ft

Safety= $\text{IF}(\Phi M_n \geq M_u, \text{"Safe"}; \text{"Unsafe"})$ = Safe

Moment_ratio= $M_u / \Phi M_n$ = 0.61

Check Shear Strength

$h/t_w, \lambda_w = \text{TAB}(\text{"AISC/W"}; h/t_w; \text{NAME} = \text{sec.})$ = 53.60

$\lambda_{w0} = 2.24 * \sqrt{E/F_y}$ = 54

$\lambda_{w1} = 1.10 * \sqrt{5 * E/F_y}$ = 59

$\lambda_{w2} = 1.37 * \sqrt{5 * E/F_y}$ = 74

Except for very few sections, which are listed in the User Note, AISC Specification Section G2.1(a) is applicable to the I-shaped beams published in the AISC Manual for $F_y \leq 50$ ksi. C_v is calculated exactly according to Eqns. G2-2, G2-3, G2-4, and G2-5

$C_{va} = 1.51 * 5 * E / (F_y * \lambda_w^2)$ = 1.52

$C_v = \text{IF}(\lambda_w \leq \lambda_{w0}; 1; \text{IF}((\lambda_w > \lambda_{w1} \text{ AND } \lambda_w \leq \lambda_{w2}); \lambda_{w1} / I_w; C_{va}))$ = 1.00

From AISC Specification Section G2.1b,

$A_w = d * t_w$ = 7 in²

From AISC Specification Section G2.1, the available shear strength is:

$V_n = 0.6 * F_y * A_w * C_v$ = 210 kips

$\Phi_v = 1.00$

$\Phi_v V_n = \Phi_v * V_n$ = 210 kips

Shear_safety= $\text{IF}(\Phi_v * V_n > Q_u, \text{"Safe"}; \text{"Unsafe"})$ = Safe



Check Deflection

$$\Delta_{all} = 12 * L / 360 = 1.17 \text{ in}$$

$$W_{eq} (LL), W_L = \frac{8 * M_L}{L^2} = 0.91 \text{ kip/ft}$$

$$\Delta_{act} = 12^3 * \frac{5 * W_L * L^4}{384 * E * I_x} = 1.10 \text{ in}$$

Deflection safety (D_s):

$$D_s = IF(\Delta_{all} \geq \Delta_{act}, "Safe", "Unsafe") = \text{Safe}$$

Design Summary

$$\Phi M_n = 0.90 * \text{MIN}(M_p; M_{n1}; M_{n2}) = 330 \text{ kip*ft}$$

$$\text{Safety} = IF(\Phi M_n \geq M_u, "Safe", "Unsafe") = \text{Safe}$$

$$\text{Moment_ratio} = M_u / \Phi M_n = 0.61$$

$$\Phi_v V_n = \Phi_v * V_n = 210 \text{ kips}$$

$$\text{Shear_safety} = IF(\Phi_v * V_n > Q_u, "Safe", "Unsafe") = \text{Safe}$$

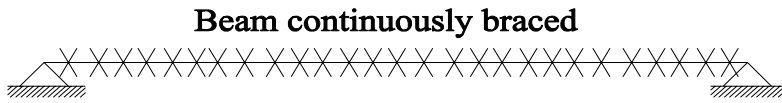
$$\Delta_{all} = 12 * L / 360 = 1.17 \text{ in}$$

$$\Delta_{act} = 12^3 * \frac{5 * W_L * L^4}{384 * E * I_x} = 0.01 \text{ in}$$

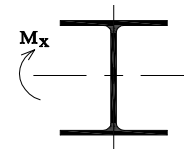
$$D_s = IF(\Delta_{all} \geq \Delta_{act}, "Safe", "Unsafe") = \text{Safe}$$



Design of W-Shapes Subjected to Moment about Strong Axis and Continuously Braced



Beam continuously braced



Materials

Grade:	SEL("Material/ASTM";NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
E=		=	29000 ksi

Beam Length and Cb

Total length, L=	35.00 ft
------------------	----------

Design Moments and Uniform Live Load

Ultimate moment, M_u =	200.00 kip*ft
Ultimate moment due to live load case, M_L =	140.00 kip*ft
Ultimate shear, Q_u =	30.00 kips

Section Details

sec.:	SEL("AISC/W";NAME;)	=	W21X48
depth, d=	TAB("AISC/W";d;NAME=sec.)	=	20.60 in
Web th., t_w =	TAB("AISC/W"; t_w ;NAME=sec.)	=	0.35 in
Flange width, b_f =	TAB("AISC/W"; b_f ;NAME=sec.)	=	8.14 in
Flange th., t_f =	TAB("AISC/W"; t_f ;NAME=sec.)	=	0.43 in
Plastic sec. modulus, Z_x =	TAB("AISC/W"; Z_x ;NAME=sec.)	=	107.00 in ³
Elastic sec. modulus, S_x =	TAB("AISC/W"; S_x ;NAME=sec.)	=	93.00 in ³
Inertia about x-axis, I_x =	TAB("AISC/W"; I_x ;NAME=sec.)	=	959.00 in ⁴
r_y =	TAB("AISC/W"; r_y ;NAME=sec.)	=	1.66 in
r_{ts} =	TAB("AISC/W"; r_{ts} ;NAME=sec.)	=	2.05 in

(r_y is radius of gyration about y-axis and r_{ts} is effective radius of gyration for the L.T.B.)

Torsional constant, J=	TAB("AISC/W";J;NAME=sec.)	=	0.80 in ⁴
h_o =	TAB("AISC/W"; h_o ;NAME=sec.)	=	20.20 in

(h_o is the distance between C.L. of flanges)

AISC Specification Eqn. (F2-1):

Yielding Moment, $M_p = Z_x * F_y * 1/12$	= 446 kip*ft
---	--------------



Element Classification

(1) Web:

$$h/t_w, \lambda_w = \text{TAB}(\text{"AISC/W"; } h/t_w; \text{NAME=sec.}) = 53.60$$

According to AISC Specification Table B4.1 Case 9, the limiting width-to-thickness ratio for the web is:

$$\text{Web_Class} = \text{IF}(\lambda_w \leq 3.76 \sqrt{E/F_y}, \text{"Compact"}, \text{"Non-Compact"}) = \text{Compact}$$

(2) Comp. flange:

$$b_f/2t_f, \lambda_f = \text{TAB}(\text{"AISC/W"; } b_f/2t_f; \text{NAME=sec.}) = 9.47$$

According to AISC Specification Table B4.1 Case 1, the limiting width-to-thickness ratios for the compression flange are:

$$\lambda_{pf} = 0.38 \sqrt{E/F_y} = 9$$

$$\lambda_{rf} = 1.00 \sqrt{E/F_y} = 24$$

$$\text{FI_Class} = \text{IF}(\lambda_f \leq \lambda_{pf}, \text{"Compact"}, \text{IF}(\lambda_f > \lambda_{rf}, \text{"Slender"}, \text{"Non-Compact"})) = \text{Non-Compact}$$

Because the beam is continuously braced, and therefore not subjected to lateral-torsional buckling, the available strength is governed by AISC Specification Sections F3.1 and F3.2. The nominal flexural moment is calculated as follows, satisfying the condition of compression Flange Local Buckling:

$$M_{n1a} = M_p - 0.7 F_y S_x^{1/2} = 174.75 \text{ kip*ft}$$

$$M_{n1} = \text{IF}(\text{FI_Class} = \text{"Compact"}, M_p; (M_p - (M_{n1a})^{\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}})) = 441 \text{ kip*ft}$$

Check The Available Flexure Strength

$$\Phi M_n = 0.90 \cdot \text{MIN}(M_p; M_{n1}) = 397 \text{ kip*ft}$$

$$\text{Safety} = \text{IF}(\Phi M_n \geq M_u, \text{"Safe"}, \text{"Unsafe"}) = \text{Safe}$$

$$\text{Moment_ratio} = M_u / \Phi M_n = 0.50$$

Check Shear Strength

$$h/t_w, \lambda_w = \text{TAB}(\text{"AISC/W"; } h/t_w; \text{NAME=sec.}) = 53.6$$

$$\lambda_{w0} = 2.24 \sqrt{E/F_y} = 53.9$$

$$\lambda_{w1} = 1.10 \sqrt{5 \cdot E/F_y} = 59.2$$

$$\lambda_{w2} = 1.37 \sqrt{5 \cdot E/F_y} = 73.8$$

Except for very few sections, which are listed in the User Note, AISC Specification Section G2.1(a) is applicable to the I-shaped beams published in the AISC Manual for $F_y = 50$ ksi. C_v is calculated exactly according to Eqns. G2-2, G2-3, G2-4, and G2-5

$$C_v = \text{IF}(\lambda_w \leq \lambda_{w0}; 1; \text{IF}((\lambda_w > \lambda_{w1} \text{ AND } \lambda_w \leq \lambda_{w2}); \lambda_{w1}/\lambda_w; 1.51 \cdot 5 \cdot E / (F_y \cdot \lambda_w^2))) = 1.00$$



Chapter 3: Steel Design

W-Shape in Strong Axis Bending, Continuously Braced

From AISC Specification Section G2.1b,

$$A_w = d \cdot t_w = 7 \text{ in}^2$$

From AISC Specification Section G2.1, the available shear strength is:

$$V_n = 0.6 \cdot F_y \cdot A_w \cdot C_v = 210 \text{ kips}$$

$$\Phi_v = 1.00$$

$$\Phi_v V_n = \Phi_v \cdot V_n = 210 \text{ kips}$$

$$\text{Shear_safety} = \text{IF}(\Phi_v \cdot V_n > Q_u, \text{"Safe"}, \text{"Unsafe"}) = \text{Safe}$$

Check Deflection

$$\Delta_{\text{all}} = 12 \cdot L / 360 = 1.17 \text{ in}$$

$$W_{\text{eq}} (\text{LL}), W_L = \frac{8 \cdot M_L}{L^2} = 0.91 \text{ kip/ft}$$

$$\Delta_{\text{act}} = 12^3 \cdot \frac{5 \cdot W_L \cdot L^4}{384 \cdot E \cdot I_x} = 1.10 \text{ in}$$

Deflection safety (D_s):

$$D_s = \text{IF}(\Delta_{\text{all}} \geq \Delta_{\text{act}}, \text{"Safe"}, \text{"Unsafe, increase section"}) = \text{Safe}$$

Design Summary

$$\Phi M_n = 0.90 \cdot \text{MIN}(M_p; M_{n1}) = 397 \text{ kip}\cdot\text{ft}$$

$$\text{Safety} = \text{IF}(\Phi M_n \geq M_u, \text{"Safe"}, \text{"Unsafe"}) = \text{Safe}$$

$$\text{Moment_ratio} = M_u / \Phi M_n = 0.50$$

$$\Delta_{\text{all}} = 12 \cdot L / 360 = 1.17 \text{ in}$$

$$\Delta_{\text{act}} = 12^3 \cdot \frac{5 \cdot W_L \cdot L^4}{384 \cdot E \cdot I_x} = 0.01 \text{ in}$$

$$D_s = \text{IF}(\Delta_{\text{all}} \geq \Delta_{\text{act}}, \text{"Safe"}, \text{"Unsafe, increase section"}) = \text{Safe}$$



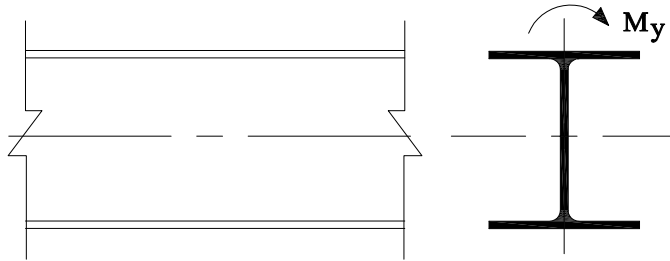
Chapter 3: Steel Design

W-Shape in Minor Axis Bending

AISC

Page: 109

Design of W-shapes Subjected to Moment about Minor Axis



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	50 ksi
E=			29000 ksi

Beam Length

Total length, L=			35.00 ft
------------------	--	--	----------

Design Moments and Uniform Live Load

Ultimate moment in minor-axis, M_{yu} =			266.00 kip*ft
Ultimate shear force, Q_{xu} =			20.00 kips

Section Details

sec.:	SEL("AISC/W"; NAME;)	=	W24X131
depth, d=	TAB("AISC/W"; d; NAME=sec.)	=	24.50 in
Web th., t_w =	TAB("AISC/W"; t_w ; NAME=sec.)	=	0.60 in
Flange width, b_f =	TAB("AISC/W"; b_f ; NAME=sec.)	=	12.90 in
Flange th., t_f =	TAB("AISC/W"; t_f ; NAME=sec.)	=	0.96 in
Plastic sec. modulus, Z_y =	TAB("AISC/W"; Z_y ; NAME=sec.)	=	81.50 in ³
Elastic sec. modulus, S_y =	TAB("AISC/W"; S_y ; NAME=sec.)	=	53.00 in ³
AISC Specification Eqn. (F6-1):			
Yielding Moment, M_p =	MIN ($Z_y * F_y * 1/12$; $1.6/12 * S_y * F_y$)	=	340 kip*ft



Element Classification

Flanges:

$$b_f/2t_f, \lambda_f = \text{TAB}(\text{"AISC/W"; } b_f/2t_f; \text{NAME=sec.}) = 6.7$$

According to AISC Specification Table B4.1 Case 1, the limiting width-to-thickness ratios for the compression flange are:

$$\lambda_{pf} = 0.38 \sqrt{E/F_y} = 9.2$$

$$\lambda_{rf} = 1.0 \sqrt{E/F_y} = 24.1$$

$$FI_Class = \text{IF}(\lambda_f \leq \lambda_{pf}, \text{"Compact"; "Non-Compact"}) = \text{Compact}$$

Because the beam bent about the minor-axis, the available strength is governed by AISC Specification Sections F6.1 and F6.2. The nominal flexural moment is calculated as follows, satisfying the condition of compression Flange Local Buckling:

$$M_{n1} = \text{IF}(FI_Class = \text{"Compact"}; M_p; (M_p - (M_p - 0.7 F_y S_y * 1/12) * (\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}))) = 340 \text{ kip*ft}$$

Check The Available Flexure Strength

$$\Phi M_n = 0.90 * \text{MIN}(M_p; M_{n1}) = 306 \text{ kip*ft}$$

$$\text{Safety} = \text{IF}(\Phi M_n \geq M_{yu}, \text{"Safe"; "Unsafe"}) = \text{Safe}$$

$$\text{Moment ratio} = M_{yu} / \Phi M_n = 0.87$$

Check Shear Strength Section G (AISC Spec.)

Calculate A_w . (Multiply by 2 for both shear resisting elements.)

$$A_w = 2 * b_f * t_f = 24.77 \text{ in}^2$$

Calculate C_v : (Eqns. G2-2, G2-3, G2-4 and G2-5)

$$b_f/2t_f, \lambda_f = \text{TAB}(\text{"AISC/W"; } b_f/2t_f; \text{NAME=sec.}) = 6.70$$

$$k_v = 1.20$$

$$\psi_{f1} = 1.1 \sqrt{k_v * E / F_y} = 29.0$$

$$\psi_{f2} = 1.37 \sqrt{k_v * E / F_y} = 36.1$$

$$C_v = \text{IF}(\lambda_f \leq \psi_{f1}; 1; \text{IF}(\lambda_f > \psi_{f1} \text{ AND } \lambda_f \leq \psi_{f2}; \psi_{f1} / \lambda_f; 1.51 * k_v * E / (F_y * \lambda_f^2))) = 1.0$$

From AISC Specification Section G2.1, the available shear strength is:

$$\Phi_v = 0.90$$

$$\text{Nominal shear strength, } V_n = 0.6 * F_y * A_w * C_v = 743 \text{ kips}$$

$$\text{Design shear, } \Phi V_n = \Phi_v * V_n = 669 \text{ kips}$$

$$\text{Shear_safety} = \text{IF}(V_n > Q_{xu}; \text{"Safe"; "Unsafe"}) = \text{Safe}$$



Chapter 3: Steel Design

W-Shape in Minor Axis Bending

AISC

Page: 111

Design Summary

$\Phi M_n =$	$0.90 * \text{MIN}(M_p; M_{n1})$	=	306 kip*ft
Safety=	$\text{IF}(\Phi M_n \geq M_{yu}; \text{"Safe"}; \text{"Unsafe"})$	=	Safe
Moment ratio=	$M_{yu} / \Phi M_n$	=	0.87
Design shear, $\Phi V_n =$	$\Phi_v * V_n$	=	669 kips
Shear_safety=	$\text{IF}(V_n > Q_{xu}; \text{"Safe"}; \text{"Unsafe"})$	=	Safe



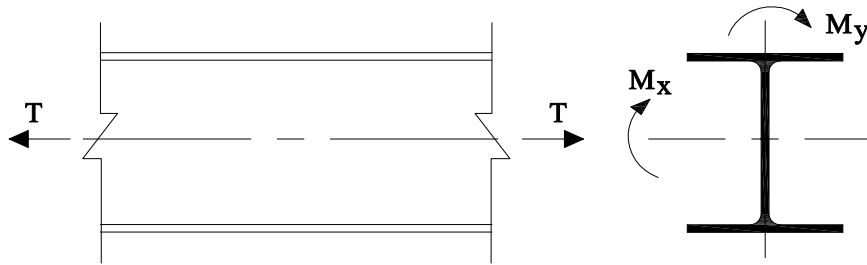
Chapter 3: Steel Design

W-Shape Subjected to Tension Force and Bending Moments

AISC

Page: 112

Design of W-Shapes Subjected to Tension Force and Bending Moments



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	50 ksi
E=			29000 ksi

Beam Length

Unsupported length, L_b =		30.00 ft	
kL_{in} =		14.00 ft	
kL_{out} =		30.00 ft	
<i>(kL_{in} and kL_{out} are the strong and weak/torsional unbraced lengths, respectively)</i>			
From Table 3-1 (AISC), C_{b1} =		1.14	

Given Straining Actions

Dead Load:		
T_D =		29.0 kips
M_{xD} =		32.0 kip*ft
M_{yD} =		11.3 kip*ft
Live Load:		
T_L =		87.0 kips
M_{xL} =		96.0 kip*ft
M_{yL} =		33.8 kip*ft

Ultimate Tension Force and Bending Moments

T_u =	$1.2*T_D + 1.6*T_L$	=	174.0 kips
M_{ux} =	$1.2*M_{xD} + 1.6*M_{xL}$	=	192.0 kip*ft
M_{uy} =	$1.2*M_{yD} + 1.6*M_{yL}$	=	67.6 kip*ft



Section Details

sec.:	SEL("AISC/W";NAME;)	= W14X82
depth, d=	TAB("AISC/W";d;NAME=sec.)	= 14.30 in
Web th., t_w =	TAB("AISC/W"; t_w ;NAME=sec.)	= 0.51 in
Flange width, b_f =	TAB("AISC/W"; b_f ;NAME=sec.)	= 10.10 in
Flange th., t_f =	TAB("AISC/W"; t_f ;NAME=sec.)	= 0.85 in
Gross Area, A=	TAB("AISC/W";A;NAME=sec.)	= 24.00 in ²
I_x =	TAB("AISC/W"; I_x ;NAME=sec.)	= 881.00 in ⁴
I_y =	TAB("AISC/W"; I_y ;NAME=sec.)	= 148.00 in ⁴
<i>(I_x and I_y are the moment of inertia about x-and y-axes, respectively)</i>		
Plastic sec. modulus, Z_x =	TAB("AISC/W"; Z_x ;NAME=sec.)	= 139.00 in ³
Elastic sec. modulus, S_x =	TAB("AISC/W"; S_x ;NAME=sec.)	= 123.00 in ³
Plastic sec. modulus, Z_y =	TAB("AISC/W"; Z_y ;NAME=sec.)	= 44.80 in ³
Elastic sec. modulus, S_y =	TAB("AISC/W"; S_y ;NAME=sec.)	= 29.30 in ³
r_x =	TAB("AISC/W"; r_x ;NAME=sec.)	= 6.05 in
r_y =	TAB("AISC/W"; r_y ;NAME=sec.)	= 2.48 in
<i>(r_x and r_y are the radius of gyration about x- and y-axis, respectively)</i>		
Torsional constant, J=	TAB("AISC/W";J;NAME=sec.)	= 5.07 in ⁴
r_{ts} =	TAB("AISC/W"; r_{ts} ;NAME=sec.)	= 2.85 in
h_o =	TAB("AISC/W"; h_o ;NAME=sec.)	= 13.40 in
<i>(r_{ts} is the Effective radius of gyration for the L.T.B. and h_o is distance between C.L. of flanges)</i>		
AISC Specification Eqn. (F6-1), the yielding moment in minor axis (M_{py}):		
M_{py} =	MIN ($Z_y * F_y * 1/12$; $1.6/12 * S_y * F_y$)	= 187 kip*ft

Slenderness Check (According to section E2)

For members designed on the basis of compression, the slenderness ratio KL/r should not exceed 300.

λ_x =	$\frac{kL_{in}}{r_x} * 12$	= 27.8
λ_y =	$\frac{kL_{out}}{r_y} * 12$	= 145.2

Then, the governed slenderness (λ_{max}):

λ_{max} =	MAX(λ_x ; λ_y)	= 145.2
Slenderness_check=	IF($\lambda_{max} \leq 300$; "Safe"; "Unsafe")	= Safe



Chapter 3: Steel Design

W-Shape Subjected to Tension Force and Bending Moments

AISC

Page: 114

Nominal Tensile Strength

From AISC Specification Section D2(a), the nominal tensile strength due to tensile yielding on the gross section is:

$$T_n = F_y * A = 1200.0 \text{ kips}$$

Nominal Flexural Strength about x-x Axis

Yielding: from AISC specification section F2.1, the nominal flexural strength due to yielding (plastic moment) is:

$$M_{px} = Z_x * F_y = 579 \text{ kip*ft}$$

Lateral torsional buckling (LTB): the limiting lengths L_p and L_r are determined according to the AISC spec. eqns. F2-5 and F2-6, as follows:

$$L_p = 1.76 * r_y * \sqrt{E/F_y} = 8.76 \text{ ft}$$

$$L_{r1} = \sqrt{\frac{J * 1.0}{S_x * h_o}} = 0.06$$

$$L_{r2} = \sqrt{1 + \sqrt{6.76 * \left(\frac{0.7 * F_y * S_x * h_o}{E * J * 1.0}\right)^2}} = 1.42$$

$$L_r = 1.95 / 12 * r_{ts} * \frac{E}{0.7 * F_y} * L_{r1} * L_{r2} = 32.69 \text{ ft}$$

$$\text{Case} = \text{IF}(L_b > L_r, \text{"ELTB"}; \text{IF}(L_b \leq L_p, \text{"No LTB"}; \text{"InLTB"})) = \text{InLTB}$$

("ELTB" refers to elastic lateral torsional buckling and "InLTB" refers to inelastic lateral torsional buckling).

The lateral torsional buckling modification factor, C_b :

$$T_{ey} = \frac{\pi^2 * E * I_y}{(L_b * 12)^2} = 326.9 \text{ kips}$$

$$C_b = C_{b1} * \sqrt{1 + \frac{T_u}{T_{ey}}} = 1.41$$

According to the AISC Spec. Eqn. F2-2:

$$M_{1a} = M_{px} - 0.7 * 1/12 * F_y * S_x = 220 \text{ kip*ft}$$

$$M_1 = \text{MIN}(M_{px}; C_b * (M_{px} - M_{1a} * (L_b - L_p) / (L_r - L_p))) = 541 \text{ kip*ft}$$



Chapter 3: Steel Design

W-Shape Subjected to Tension Force and Bending Moments

AISC

Page: 115

According to the AISC Spec. Eqn. F2-4:

$$F_{cr} = \frac{C_b \cdot \pi^2 \cdot E}{\left(\frac{(L_b + 0.01) \cdot 12}{r_{ts}} \right)^2} = 25.28 \text{ ksi}$$

$$F_{cr,mod} = \sqrt{1 + \frac{0.078 \cdot J \cdot 1.0}{S_x \cdot h_o} \cdot \left(\frac{L_b \cdot 12}{r_{ts}} \right)^2} = 2.20 \text{ ksi}$$

According to the AISC Spec. Eqns. F2-3:

$$M_2 = \text{MIN}(M_{px}; F_{cr} \cdot S_x / 12 \cdot F_{cr,mod}) = 570 \text{ kip}\cdot\text{ft}$$

According to the AISC Spec. Eqn. F2-2:

$$M_{nx2} = \text{IF}(\text{Case} = \text{"No LTB"}; M_{px}; \text{IF}(\text{Case} = \text{"In LTB"}; M_1; M_2)) = 541 \text{ kip}\cdot\text{ft}$$

Element Classification

(1) Web:

$$h/t_w, \lambda_w = \text{TAB}(\text{"AISC/W"}; h/t_w; \text{NAME} = \text{sec.}) = 22.40$$

According to AISC Specification Table B4.1 Case 9, the limiting width-to-thickness ratio for the web is:

$$\text{Web_Class} = \text{IF}(\lambda_w \leq 3.76 \cdot \sqrt{E/F_y}; \text{"Compact"}; \text{"Non-Compact"}) = \text{Compact}$$

(2) Comp. flange:

$$b_f/2t_f, \lambda_f = \text{TAB}(\text{"AISC/W"}; b_f/2t_f; \text{NAME} = \text{sec.}) = 5.92$$

According to AISC Specification Table B4.1 Case 1, the limiting width-to-thickness ratios for the compression flange are:

$$\lambda_{pf} = 0.38 \cdot \sqrt{E/F_y} = 9$$

$$\lambda_{rf} = 1.00 \cdot \sqrt{E/F_y} = 24$$

$$\text{FI_Class} = \text{IF}(\lambda_f \leq \lambda_{pf}; \text{"Compact"}; \text{IF}(\lambda_f > \lambda_{rf}; \text{"Slender"}; \text{"Non-Compact"})) = \text{Compact}$$

The available strength provided by AISC Specification Sections F3.1, F3.2, F6.1 and F6.2, the nominal flexural moments in strong/weak axes are calculated as follows, satisfying the condition of compression

Flange Local Buckling:

$$M_{nx1a} = M_{px} - 0.7 \cdot F_y \cdot S_x \cdot 1/12 = 220 \text{ kip}\cdot\text{ft}$$

$$M_{nx1} = \text{IF}(\text{FI_Class} = \text{"Compact"}; M_{px}; M_{px} - M_{nx1a} \cdot \left(\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}} \right)) = 579 \text{ kip}\cdot\text{ft}$$

$$M_{ny1a} = M_{py} - 0.7 \cdot F_y \cdot S_y \cdot 1/12 = 102 \text{ kip}\cdot\text{ft}$$

$$M_{ny1} = \text{IF}(\text{FI_Class} = \text{"Compact"}; M_{py}; M_{py} - M_{ny1a} \cdot \left(\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}} \right)) = 187 \text{ kip}\cdot\text{ft}$$



Chapter 3: Steel Design

W-Shape Subjected to Tension Force and Bending Moments

AISC

Page: 116

Design Flexure Moment in Major/Minor Axes

$$M_{nx} = \text{MIN}(M_{px}; M_{nx1}; M_{nx2}) = 541 \text{ kip}\cdot\text{ft}$$

$$M_{ny} = \text{MIN}(M_{py}; M_{ny1}) = 187 \text{ kip}\cdot\text{ft}$$

Calculate The Available Flexural and Axial Strengths

$$\Phi_b = 0.90$$

$$\Phi_t = 0.90$$

$$T_c = \Phi_t * T_n = 1080 \text{ kips}$$

$$M_{cx} = \Phi_b * M_{nx} = 487 \text{ kip}\cdot\text{ft}$$

$$M_{cy} = \Phi_b * M_{ny} = 168 \text{ kip}\cdot\text{ft}$$

Interaction of Tension and Flexure

Check limit for AISC Specification Equation H1-1a.

$$\text{Tension_ratio, } t = \frac{T_u}{T_c} = 0.16$$

$$\text{Moment_ratio, } m = \frac{M_{ux}}{M_{cx}} + \frac{M_{uy}}{M_{cy}} = 0.80$$

$$\text{Safety_ratio, } r = \text{IF}(t \geq 0.2; t + 8/9 * m; t/2 + m) = 0.88$$

$$\text{Safety} = \text{IF}(r \leq 1; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Design Summary

$$T_u = 1.2 * T_D + 1.6 * T_L = 174.0 \text{ kips}$$

$$M_{ux} = 1.2 * M_{xD} + 1.6 * M_{xL} = 192.0 \text{ kip}\cdot\text{ft}$$

$$M_{uy} = 1.2 * M_{yD} + 1.6 * M_{yL} = 67.6 \text{ kip}\cdot\text{ft}$$

$$T_c = \Phi_t * T_n = 1080 \text{ kips}$$

$$M_{cx} = \Phi_b * M_{nx} = 487 \text{ kip}\cdot\text{ft}$$

$$M_{cy} = \Phi_b * M_{ny} = 168 \text{ kip}\cdot\text{ft}$$

$$\text{Slenderness_check} = \text{IF}(\lambda_{\max} \leq 300; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\text{Safety_ratio, } r = \text{IF}(t \geq 0.2; t + 8/9 * m; t/2 + m) = 0.88$$

$$\text{Safety} = \text{IF}(r \leq 1; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



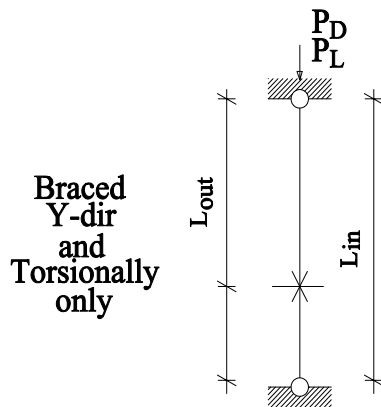
Chapter 3: Steel Design

W-Shapes in Axial Compression

AISC

Page: 117

Design of W-Shapes Subjected to Axial Compression



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	50.00
E =			29000 ksi

Buckling Lengths

kL_{in} =		30.00 ft
kL_{out} =		15.00 ft

(kL_{in} and kL_{out} are unbraced lengths for the strong- and weak-axes)

Axial Loads

Dead load, P_D =		140 kips
Live load, P_L =		420 kips
From Chapter 2 of ASCE/SEI 7, the required compressive strength is:		
Ultimate load, P_u =	$1.2 \cdot P_D + 1.6 \cdot P_L$	= 840 kips

Section Details

sec.:	SEL("AISC/W"; NAME;)	=	W14X90
depth, d =	TAB("AISC/W"; d ; NAME=sec.)	=	14.00 in
Web th., t_w =	TAB("AISC/W"; t_w ; NAME=sec.)	=	0.44 in
Flange width, b_f =	TAB("AISC/W"; b_f ; NAME=sec.)	=	14.50 in
Flange th., t_f =	TAB("AISC/W"; t_f ; NAME=sec.)	=	0.71 in
Area, A =	TAB("AISC/W"; A ; NAME=sec.)	=	26.50 in ²
r_x =	TAB("AISC/W"; r_x ; NAME=sec.)	=	6.14 in
r_y =	TAB("AISC/W"; r_y ; NAME=sec.)	=	3.70 in

(r_x and r_y are the radius of gyration about x- and y-axes, respectively)



Element Classification (According to Table B4-1)

(1) Web:

$$h/t_w, \lambda_w = \text{TAB}(\text{"AISC/W"; } h/t_w; \text{NAME=sec.}) = 25.90$$

According to AISC Specification Table B4.1 Case 10, the limiting width-to-thickness ratio for non-compact web is:

$$\text{Web_Class} = \text{IF}(\lambda_w \leq 1.49 \sqrt{E/F_y}; \text{"Non-Compact"; "Slender"}) = \text{Non-Compact}$$

(2) Flanges:

$$b_f/2t_f, \lambda_f = \text{TAB}(\text{"AISC/W"; } b_f/2t_f; \text{NAME=sec.}) = 10.20$$

According to AISC Specification Table B4.1 Case 4, the limiting width-to-thickness ratio for non-compact flange is:

$$k_c = \text{MIN}(\text{MAX}(4/\sqrt{\lambda_w}; 0.35); 0.76) = 0.76$$

$$\lambda_{rf} = 0.64 \sqrt{k_c E/F_y} = 13$$

$$\text{Fl_Class} = \text{IF}(\lambda_f \leq \lambda_{rf}; \text{"Non-Compact"; "Slender"}) = \text{Non-Compact}$$

Slenderness Check (According to Section E2)

For members designed on the basis of compression, the slenderness ratio KL/r preferably should not exceed 200.

$$\lambda_x = \frac{kL_{in}}{r_x} * 12 = 58.6$$

$$\lambda_y = \frac{kL_{out}}{r_y} * 12 = 48.6$$

Then, the governed slenderness (λ_{max}):

$$\lambda_{max} = \text{MAX}(\lambda_x; \lambda_y) = 58.6$$

Critical Stresses

The available critical stresses may be interpolated from AISC Manual Table 4-22 or calculated directly as follows:

-Calculate the elastic critical buckling stress, F_e :

$$F_e = \frac{\pi^2 * E}{\lambda_{max}^2} = 83.3 \text{ ksi}$$

-Calculate the flexural buckling stress, F_{cr} (Eqns. E3-2 and E3-3):

$$\lambda_1 = 4.71 \sqrt{E/F_y} = 113$$

$$F_{cr} = \text{IF}(\lambda_{max} \leq \lambda_1; 0.658^{(F_y/F_e)} * F_y; 0.877 * F_e) = 38.9 \text{ ksi}$$



Chapter 3: Steel Design

W-Shapes in Axial Compression

AISC

Page: 119

Nominal Compressive Strength (Eqn. E3-1)

$$P_n = F_{cr} * A = 1031 \text{ kips}$$

$$\Phi_v = 0.90$$

$$\Phi_v P_n = \Phi_v * P_n = 928 \text{ kips}$$

Compressive stress_safety (S_s):

$$S_s = \text{IF}(\Phi_v * P_n > P_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\text{Stress_ratio} = P_u / (\Phi_v * P_n) = 0.91$$

Design Summary

$$\text{Ultimate load, } P_u = 1.2 * P_D + 1.6 * P_L = 840 \text{ kips}$$

$$\text{Design load, } \Phi_v P_n = \Phi_v * P_n = 928 \text{ kips}$$

$$\text{Stress_ratio} = P_u / (\Phi_v * P_n) = 0.91$$

$$S_s = \text{IF}(\Phi_v * P_n > P_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



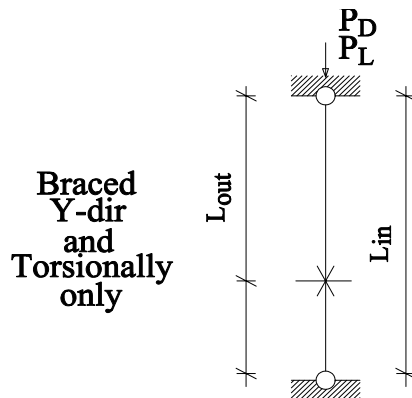
Chapter 3: Steel Design

WT-Shapes in Axial Compression

AISC

Page: 120

Design of WT-Shapes Subjected to Compression Axial Force



Materials

Grade:	SEL("Material/ASTM";NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
E =			29000 ksi
G =			11200 ksi

Buckling Lengths

kL_{in} =			20.00 ft
kL_{out} =			20.00 ft
k_2L =			20.00 ft

(kL_{in} and kL_{out} are unbraced lengths for the strong- and weak- axes, respectively; k_2L is the torsional unbraced length)

Axial Loads

Axial dead load, P_D =			6 kips
Axial Live load, P_L =			18 kips

From Chapter 2 of ASCE/SEI 7, the required compressive strength is:

Ultimate load, P_u =	$1.2 \cdot P_D + 1.6 \cdot P_L$	=	36.0 kips
------------------------	---------------------------------	---	-----------

Section Details

sec.:	SEL("AISC/WT"; NAME;)	=	WT7X15
Depth, d =	TAB("AISC/WT"; d ;NAME=sec.)	=	6.92 in
Stem thickness, t_w =	TAB("AISC/WT"; t_w ;NAME=sec.)	=	0.270 in
Flange width, b_f =	TAB("AISC/WT"; b_f ;NAME=sec.)	=	6.73 in
Flange thickness, t_f =	TAB("AISC/WT"; t_f ;NAME=sec.)	=	0.385 in
Gross area, A =	TAB("AISC/WT"; A ;NAME=sec.)	=	4.4 in ²



Chapter 3: Steel Design

WT-Shapes in Axial Compression

AISC

Page: 121

$I_x =$	TAB("AISC/WT"; I_x ;NAME=sec.)	=	19 in ⁴
$I_y =$	TAB("AISC/WT"; I_y ;NAME=sec.)	=	10 in ⁴
<i>(I_x and I_y are the moment of inertia about x-and y-axes, respectively)</i>			
$r_x =$	TAB("AISC/WT"; r_x ;NAME=sec.)	=	2.07 in
$r_y =$	TAB("AISC/WT"; r_y ;NAME=sec.)	=	1.49 in
<i>(r_x and r_y are the radius of gyration about x- and y-axis, respectively)</i>			
Torsion constant, J=	TAB("AISC/WT";J;NAME=sec.)	=	0.19 in ⁴
$Q_s =$	TAB("AISC/WT"; Q_s ;NAME=sec.)	=	0.61
$y =$	TAB("AISC/WT"; y ;NAME=sec.)	=	1.58 in
<i>(Q_s is a reduction factor for unstiffened elements and y is the distance to the N.A.)</i>			

Element Classification

(1) Flanges:

$$b_f/2t_f, \lambda_{rf} = b_f/(2*t_f) = 8.74$$

Determine the flange limiting slenderness ratio, λ_{rf} , from AISC Specification Table B4.1a case 2:

$$\lambda_{rf} = 0.56*\sqrt{(E/F_y)} = 13.5$$

$$FI_Class = IF(\lambda_{rf} \leq \lambda_{rf}, "Non-Compact"; "Slender") = Non-Compact$$

(2) Web:

$$d/t_w, \lambda_w = d/t_w = 25.6$$

Determine the slender web limit from AISC Specification Table B4.1a case 4:

$$\lambda_{rw} = 0.75*\sqrt{(E/F_y)} = 18.06$$

$$Web_Class = IF(\lambda_w \leq \lambda_{rw}, "Non-compact"; "Slender") = Slender$$

$$Q = Q_s = 0.610$$

Slenderness check:

For members designed on the basis of compression, the slenderness ratio KL/r preferably should not exceed 200.

$$\lambda_x = \frac{kL_{in}}{r_x} * 12 = 115.9$$

$$\lambda_y = \frac{kL_{out}}{r_y} * 12 = 161.1$$

$$\lambda_{max} = MAX(\lambda_x, \lambda_y) = 161.1$$



Chapter 3: Steel Design

WT-Shapes in Axial Compression

AISC

Page: 122

X-X Axis Critical Elastic Flexural Buckling Stress:

$$F_{ex} = \frac{\pi^2 * E}{\lambda_x^2} = 21.3 \text{ ksi}$$

Critical Elastic Torsional and Flexural-Torsional Buckling Stress:

$$F_{ey} = \frac{\pi^2 * E}{\lambda_y^2} = 11.0 \text{ ksi}$$

Torsional Parameters

The shear center for a T-shaped section is located on the axis of symmetry at the mid-depth of the flange.

$$x_o = 0.0 \text{ in}$$

$$y_o = y - t_f / 2 = 1.39 \text{ in}$$

According to the AISC Specification Eqn. E4-11:

$$r_o = \sqrt{(x_o^2 + y_o^2 + \frac{I_x + I_y}{A})} = 2.92 \text{ in}$$

According to the AISC Specification Eqn. E4-10:

$$H = \frac{x_o^2 + y_o^2}{r_o^2} = 0.77 \text{ in}$$

According to the AISC Specification Eqn. E4-9:

$$F_{ez} = \left(\frac{\pi^2 * E * C_w}{(k_z * L)^2} + GJ \right) \frac{1}{A * r_o^2}$$

Omit term with C_w per User Note at end of AISC Specification Section E4.

$$F_{ez} = \frac{G * J}{A * r_o^2} = 56.72 \text{ ksi}$$

According to the AISC Specification Eqn. E4-5:

$$F_{e2} = \frac{F_{ey} + F_{ez}}{2 * H} * \left(1 - \sqrt{1 - \frac{4 * F_{ey} * F_{ez} * H}{(F_{ey} + F_{ez})^2}} \right) = 10.5 \text{ ksi}$$

Governed Critical Elastic Buckling Stress

$$F_e = \text{MIN} (F_{ex}; F_{ey}; F_{e2}) = 10.5 \text{ ksi}$$



Chapter 3: Steel Design

WT-Shapes in Axial Compression

AISC

Page: 123

Buckling Stress for The Section

Determine whether AISC Specification Equation E7-2 or E7-3 applies.

$$F_{er} = 0.44 * Q * F_y = 13.4 \text{ ksi}$$

$$F_{cr} = \text{IF}(F_e \geq F_{er}; Q * 0.658^{(F_y * Q / F_e)} * F_y; 0.877 * F_e) = 9.2 \text{ ksi}$$

Nominal Compressive Strength

$$P_n = F_{cr} * A = 40.5 \text{ kips}$$

$$\Phi_v = 0.90$$

$$\Phi_v P_n = \Phi_v * P_n = 36.5 \text{ kips}$$

Compressive stress safety (S_s):

$$S_s = \text{IF}(\Phi_v * P_n > P_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\text{Stress_ratio} = \frac{P_u}{\Phi_v * P_n} = 0.99$$

Design Summary

$$\text{Ultimate load, } P_u = 1.2 * P_D + 1.6 * P_L = 36.0 \text{ kips}$$

$$\text{Design load, } \Phi_v P_n = \Phi_v * P_n = 36.5 \text{ kips}$$

$$\text{Stress_ratio} = \frac{P_u}{\Phi_v * P_n} = 0.99$$

$$S_s = \text{IF}(\Phi_v * P_n > P_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



Chapter 3: Steel Design

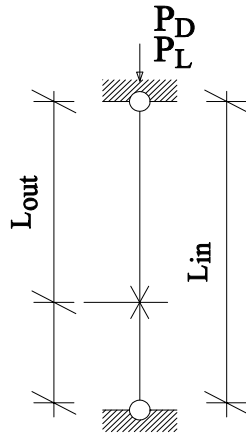
Built-Up W-Shapes with Slender Elements

AISC

Page: 124

Design of Built-Up W-Shapes with Slender Elements Subjected to Compression Axial Force

**Braced
Y-dir
and
Torsionally
only**



Materials

Grade:	SEL("Material/ASTM";NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
E=			29000 ksi
G=			11200 ksi

Buckling Lengths

kL_{in} =		30.00 ft
kL_{out} =		15.00 ft
k_2L =		15.00 ft

(kL_{in} and kL_{out} are unbraced lengths for the strong- and weak- axes, respectively; k_2L is the torsional unbraced length)

Axial Loads

Dead load, P_D =		140 kips
Live load, P_L =		200 kips
From Chapter 2 of ASCE/SEI 7, the required compressive strength is:		
Ultimate load, $P_u=1.2*P_D+1.6*P_L$	=	488 kips

Section Details

Web height, h =		15.0 in
Web th., t_w =		0.25 in
Flange width, b_f =		8.00 in
Flange th., t_f =		1.00 in



Built-Up Section Properties (ignoring fillet welds):

$$\text{Area, } A = h \cdot t_w + 2 \cdot b_f \cdot t_f = 19.75 \text{ in}^2$$

$$I_x = 2 \cdot (b_f \cdot t_f) \cdot (t_f/2 + h/2)^2 + \frac{t_w \cdot h^3}{12} + \frac{b_f \cdot (t_f)^3 \cdot 2}{12} = 1096 \text{ in}^4$$

$$I_y = \frac{2 \cdot b_f^3 \cdot t_f}{12} + \frac{h \cdot t_w^3}{12} = 85.35 \text{ in}^4$$

$$r_x = \sqrt{\frac{I_x}{A}} = 7.45 \text{ in}$$

$$r_y = \sqrt{\frac{I_y}{A}} = 2.08 \text{ in}$$

Slenderness Check

For members designed on the basis of compression, the slenderness ratio KL/r preferably should not exceed 200.

$$\lambda_x = \frac{kL_{in}}{r_x} \cdot 12 = 48.3$$

$$\lambda_y = \frac{kL_{out}}{r_y} \cdot 12 = 86.5$$

Then, the governed slenderness (λ_{max}):

$$\lambda_{max} = \text{MAX}(\lambda_x; \lambda_y) = 86.5$$

Elastic Flexural Buckling Stress

The available critical stresses may be interpolated from AISC Manual Table 4-22 or calculated directly. As follows:

$$F_{e1} = \frac{\pi^2 \cdot E}{\lambda_{max}^2} = 38.3 \text{ ksi}$$

Elastic Critical Torsional Buckling Stress

From the User Note in AISC *Specification* Section E4,

$$h_o = h + t_f = 16 \text{ in}$$

$$C_w = \frac{I_y \cdot h_o^2}{4} = 5462 \text{ in}^6$$

From AISC Design Guide 9, Equation 3.4,

$$J = \frac{2 \cdot b_f^3 \cdot t_f^3 + h \cdot t_w^3}{3} = 5.41 \text{ in}^4$$



According to AISC Specification (Eqn. E4-4),

$$F_{e2} = \frac{\pi^2 * E * C_w}{(kzL * 12)^2} + G * J \cdot \frac{1}{I_x + I_y} = 92.1 \text{ ksi}$$

Elastic Governed Stress

$$F_e = \text{MIN}(F_{e1}; F_{e2}) = 38.3 \text{ ksi}$$

Element Classification

(1) Flanges: Check for slender flanges using AISC *Specification* Table B4.1a, then determine Q_s , the unstiffened element (flange) reduction factor using AISC *Specification* Section E7.1.

Calculate k_c using AISC *Specification* Table B4.1b note [a].

$$k_c = \text{MIN}(\text{MAX}(4/\sqrt{h/t_w}); 0.35); 0.76) = 0.52$$

$$b_f/2t_f, \lambda_f = b_f/(2 * t_f) = 4.00$$

Determine the flange limiting slenderness ratio, λ_{rf} , from AISC *Specification* Table B4.1a case 2

$$\lambda_{rf} = 0.64 * \sqrt{(k_c * E / F_y)} = 11.11$$

$$FI_Class = \text{IF}(\lambda_f \leq \lambda_{rf}, \text{"Non-Compact"}, \text{"Slender"}) = \text{Non-Compact}$$

Calculate Q_s , according to the AISC *Specification* Eqns. E7-4, E7-5 and E7-6

$$\lambda_{rf1} = 1.17 * \sqrt{(k_c * E / F_y)} = 20.32$$

$$Q_{s1} = 0.9 * E * k_c / (F_y * \lambda_f^2) = 16.97$$

$$Q_{s2} = 1.415 - 0.65 * \lambda_f * \sqrt{(F_y / (E * k_c))} = 1.27$$

$$Q_s = \text{IF}(\lambda_f \leq \lambda_{rf}; 1; \text{IF}(\lambda_f > \lambda_{rf1}; Q_{s1}; Q_{s2})) = 1.00$$

Web: Check for a slender web, then determine Q_a , the stiffened element (web) reduction factor using AISC *Specification*, Section E7.2.

$$h/t_w, \lambda_w = h/t_w = 60.00$$

Determine the slender web limit from AISC *Specification* Table B4.1a case 5

$$\lambda_{rw} = 1.49 * \sqrt{(E / F_y)} = 35.88$$

$$Web_Class = \text{IF}(\lambda_w \leq \lambda_{rw}, \text{"Non-compact"}, \text{"Slender"}) = \text{Slender}$$

$$Q_a = \frac{A_e}{A_g}$$

where A_e is the effective area based on the reduced effective width (b_e). For AISC *Specification* Equation E7-17, take f as F_{cr} with F_{cr} calculated based on $Q = 1.0$. Select between AISC *Specification* Equations E7-2 and E7-3 based on KL/r_y .

$$\lambda_1 = 4.71 * \sqrt{\frac{E}{F_y}} = 113$$



Calculate the flexural buckling stress, F_{cr} :

$$F_{cr1} = \text{IF}(\lambda_{\max} \leq \lambda_1; 0.658^{(F_y/F_e)} * F_y; 0.877 * F_e) = 29.0 \text{ ksi}$$

$$b_e = \text{MIN}(1.92 * t_w * \sqrt{\frac{E}{F_{cr1}}} * (1 - \frac{0.34}{\lambda_w} * \sqrt{\frac{E}{F_{cr1}}}); h) = 12.5 \text{ in}$$

(Note that b_e should be less than the web height)

$$A_e = b_e * t_w + 2 * b_f * t_f = 19.1 \text{ in}^2$$

$$Q_a = \frac{A_e}{A} = 0.967$$

$$Q = Q_s * Q_a = 0.967$$

Flexural Buckling Strength

Determine another time whether AISC *Specification* Equation E7-2 or E7-3 applies.

$$\lambda_2 = 4.71 * \sqrt{(E / (Q * F_y))} = 115$$

$$F_{cr2} = \text{IF}(\lambda_{\max} \leq \lambda_1; Q * 0.658^{(F_y * Q / F_e)} * F_y; 0.877 * F_e) = 28.5 \text{ ksi}$$

Nominal Compressive Strength

$$P_n = F_{cr2} * A = 563 \text{ kips}$$

$$\Phi_v = 0.90$$

$$\Phi_v P_n = \Phi_v * P_n = 507 \text{ kips}$$

Compressive stress safety (S_s):

$$S_s = \text{IF}(\Phi_v * P_n > P_u, \text{"Safe"}, \text{"Unsafe"}) = \text{Safe}$$

$$\text{Stress_ratio} = \frac{P_u}{\Phi_v * P_n} = 0.96$$

Design Summary

$$\text{Ultimate load, } P_u = 1.2 * P_D + 1.6 * P_L = 488 \text{ kips}$$

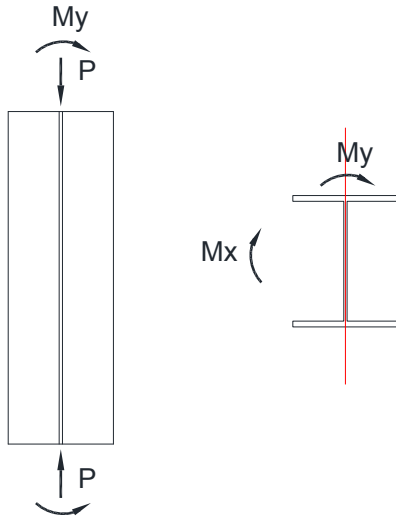
$$\Phi_v P_n = \Phi_v * P_n = 507 \text{ kips}$$

$$\text{Stress_ratio} = \frac{P_u}{\Phi_v * P_n} = 0.96$$

$$S_s = \text{IF}(\Phi_v * P_n > P_u, \text{"Safe"}, \text{"Unsafe"}) = \text{Safe}$$



Design of W-Shapes Subjected to Compression Force and Bending Moment



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
Fy=	TAB("Material/ASTM";F _y ;NAME=Grade)	=	50 ksi
E=			29000 ksi

Beam Length and C_b

Unsupported length, L _b =	14.00 ft
kL _{in} =	14.00 ft
kL _{out} =	14.00 ft
(kL _{in} and kL _{out} are strong- and weak/torsional- axes unbraced length, respectively)	
From Table 3-1 (AISC), C _b =	1.00

Ultimate Compression Force and Bending Moments

(obtained from a second-order analysis that includes P- δ effects)

P _u =	200.0 kips
M _{ux} =	50.0 kip*ft
M _{uy} =	50.0 kip*ft



Chapter 3: Steel Design

W-Shapes Subjected to Compression and Bending

Section Details

sec.:	SEL("AISC/W";NAME;)	=	W14X68
depth, d=	TAB("AISC/W";d;NAME=sec.)	=	14.00 in
Web th., t_w =	TAB("AISC/W"; t_w ;NAME=sec.)	=	0.41 in
Flange width, b_f =	TAB("AISC/W"; b_f ;NAME=sec.)	=	10.00 in
Flange th., t_f =	TAB("AISC/W"; t_f ;NAME=sec.)	=	0.72 in
Gross Area, A=	TAB("AISC/W";A;NAME=sec.)	=	20.00 in ²
I_x =	TAB("AISC/W"; I_x ;NAME=sec.)	=	722.00 in ⁴
I_y =	TAB("AISC/W"; I_y ;NAME=sec.)	=	121.00 in ⁴
<i>(I_x and I_y are the moment of inertia about x-and y-axes, respectively)</i>			
Plastic sec. modulus, Z_x =	TAB("AISC/W"; Z_x ;NAME=sec.)	=	115.00 in ³
Elastic sec. modulus, S_x =	TAB("AISC/W"; S_x ;NAME=sec.)	=	103.00 in ³
Plastic sec. modulus, Z_y =	TAB("AISC/W"; Z_y ;NAME=sec.)	=	36.90 in ³
Elastic sec. modulus, S_y =	TAB("AISC/W"; S_y ;NAME=sec.)	=	24.20 in ³
Radius of gyration about x-axis, r_x =	TAB("AISC/W"; r_x ;NAME=sec.)	=	6.01 in
Radius of gyration about y-axis, r_y =	TAB("AISC/W"; r_y ;NAME=sec.)	=	2.46 in
Torsional constant, J=	TAB("AISC/W";J;NAME=sec.)	=	3.01 in ⁴
r_{ts} =	TAB("AISC/W"; r_{ts} ;NAME=sec.)	=	2.80 in
h_o =	TAB("AISC/W"; h_o ;NAME=sec.)	=	13.30 in
<i>(r_{ts} is the Effective radius of gyration for the L.T.B. and h_o is distance between C.L. of flanges)</i>			
AISC Specification Eqn. (F2-1):			
Yielding Moment in major axis, M_{px} =	$Z_x * F_y * 1/12$	=	479 kip*ft
AISC Specification Eqn. (F6-1):			
Yielding Moment in minor axis, M_{py} =	MIN ($Z_y * F_y * 1/12$; $1.6/12 * S_y * F_y$)	=	154 kip*ft

Element Classification

(1) Web:

h/tw, λ_w =	TAB("AISC/W";h/ t_w ;NAME=sec.)	=	27.50
---------------------	-----------------------------------	---	-------

According to AISC Specification Table B4.1 Case 9, the limiting width-to-thickness ratio for the web is:

Web_Class=	IF($\lambda_w \leq 3.76 * \sqrt{E/F_y}$;"Compact"; "Non-Compact")	=	Compact
------------	---	---	---------

(2) Comp. flange:

$b_f/2t_f$, λ_f =	TAB("AISC/W"; $b_f/2t_f$;NAME=sec.)	=	6.97
----------------------------	--------------------------------------	---	------



According to AISC Specification Table B4.1 Case 1, the limiting width-to-thickness ratios for the compression flange are:

$$\lambda_{pf} = 0.38 * \sqrt{\frac{E}{F_y}} = 9$$

$$\lambda_{rf} = 1.00 * \sqrt{\frac{E}{F_y}} = 24$$

$$FI_Class = IF(\lambda_f \leq \lambda_{pf}, "Compact"; IF(\lambda_f > \lambda_{rf}, "Slender"; "Non-Compact")) = Compact$$

The available strength provided by AISC Specification Sections F3.1, F3.2, F6.1 and F6.2, the nominal flexural moments in strong/weak axes are calculated as follows, satisfying the condition of compression Flange Local Buckling:

$$M_{px1} = M_{px} - 0.7 * F_y * S_x * 1/12 = 179 \text{ kip*ft}$$

$$M_{nx1} = IF(FI_Class = "Compact"; M_{px}; (M_{px} - (M_{px1}) * (\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}))) = 479 \text{ kip*ft}$$

$$M_{py1} = M_{py} - 0.7 * F_y * S_y * 1/12 = 83 \text{ kip*ft}$$

$$M_{ny1} = IF(FI_Class = "Compact"; M_{py}; (M_{py} - (M_{py1}) * (\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}))) = 154 \text{ kip*ft}$$

Slenderness Check: (According to Section E2)

For members designed on the basis of compression, the slenderness ratio KL/r preferably should not exceed 200.

$$\lambda_x = \frac{KL_{in}}{r_x} * 12 = 28.0$$

$$\lambda_y = \frac{KL_{out}}{r_y} * 12 = 68.3$$

Then, the governed slenderness (λ_{max}):

$$\lambda_{max} = MAX(\lambda_x; \lambda_y) = 68.3$$

Critical Stresses

The available critical stresses may be interpolated from AISC Manual Table 4-22 or calculated directly as follows:

-Calculate the elastic critical buckling stress, F_e :

$$F_e = \frac{\pi^2 * E}{\lambda_{max}^2} = 61.4 \text{ ksi}$$



-Calculate the flexural buckling stress, F_{cr} (Eqns. E3-2 and E3-3):

$$\lambda_1 = 4.71 * \sqrt{\frac{E}{F_y}} = 113$$

$$F_{cr} = \begin{cases} F_y & \text{if } (\lambda_{\max} \leq \lambda_1; 0.658^{(F_y / F_e)}) * F_y; 0.877 * F_e \end{cases} = 35.6 \text{ ksi}$$

Design Compressive Strength

(Eqn. E3-1)

$$P_n = F_{cr} * A = 712.0 \text{ kips}$$

$$\Phi_c = 0.90$$

$$\Phi_c P_n = \Phi_c * P_n = 640.8 \text{ kips}$$

Lateral Torsional Buckling (LTB)

The limiting lengths L_p and L_r are determined according to the AISC Spec. Eqns. F2-5 and F2-6, as follows:

$$L_p = 1.76 * r_y * \sqrt{\frac{E}{F_y}} / 12 = 8.69 \text{ ft}$$

$$L_{r1} = \sqrt{\frac{J * 1.0}{S_x * h_o}} = 0.05$$

$$L_{r2} = \sqrt{1 + \sqrt{6.76 * \left(\frac{0.7 * F_y * S_x * h_o}{E * J * 1.0} \right)^2}} = 1.56$$

$$L_r = 1.95 / 12 * r_{ts} * \frac{E}{0.7 * F_y} * L_{r1} * L_{r2} = 29.41 \text{ ft}$$

$$\text{Case} = \begin{cases} \text{"ELTB"} & \text{if } (L_b > L_r); \\ \text{"No LTB"}; \text{"InLTB"} & \text{if } (L_b \leq L_p); \end{cases} = \text{InLTB}$$

(*"ELTB" refers to elastic LTB. and "InLTB" refers to Inelastic LTB.*)

According to the AISC Spec. Eqn. F2-2:

$$M_1 = \text{MIN}(M_{px}; C_b * (M_{px} - (M_{px} - 0.7 * 1 / 12 * F_y * S_x) * (L_b - L_p) / (L_r - L_p))) = 433 \text{ kip*ft}$$

According to the AISC Spec. Eqn. F2-4:

$$F_{cr} = C_b * \pi^2 * \frac{E}{((L_b + 0.01) * 12 / r_{ts})^2} = 79.4 \text{ ksi}$$

$$F_{cr,mod} = \sqrt{1 + 0.078 * J * \frac{1.0}{S_x * h_o} * \left(L_b * \frac{12}{r_{ts}} \right)^2} = 1.3 \text{ ksi}$$

According to the AISC Spec. Eqns. F2-3:

$$M_2 = \text{MIN}(M_{px}; F_{cr} * S_x / 12 * F_{cr,mod}) = 479 \text{ kip*ft}$$



According to the AISC Spec. Eqn. F2-2:

$$M_{nx2} = \text{IF}(\text{Case}="No L.T.B."; M_{px}; \text{IF}(\text{Case}="InLTB"; M_1; M_2)) = 433 \text{ kip}\cdot\text{ft}$$

Design Flexure Moments in Major/Minor Axes

$$\Phi_b = 0.90$$

$$M_{nx} = \text{MIN}(M_{px}; M_{nx1}; M_{nx2}) = 433 \text{ kip}\cdot\text{ft}$$

$$M_{ny} = \text{MIN}(M_{py}; M_{ny1}) = 154 \text{ kip}\cdot\text{ft}$$

Calculate the Available Flexural and Axial Strengths

$$F_{ca} = \frac{\Phi_c \cdot P_n}{A} = 32.04 \text{ ksi}$$

$$F_{bcx} = 12 \cdot \frac{\Phi_b \cdot M_{nx}}{S_x} = 45.40 \text{ ksi}$$

$$F_{bcy} = 12 \cdot \frac{\Phi_b \cdot M_{ny}}{S_y} = 68.73 \text{ ksi}$$

Calculate the Actual Flexural and Axial Stresses

$$f_{ra} = \frac{P_u}{A} = 10.00 \text{ ksi}$$

$$f_{rbx} = 12 \cdot \frac{M_{ux}}{S_x} = 5.83 \text{ ksi}$$

$$f_{rby} = 12 \cdot \frac{M_{uy}}{S_y} = 24.79 \text{ ksi}$$

Check the Combined Stress Ratio

(AISC Specification Section H2)

$$\text{Stress_ratio} = \frac{f_{ra}}{F_{ca}} + \frac{f_{rbx}}{F_{bcx}} + \frac{f_{rby}}{F_{bcy}} = 0.80$$

$$\text{Safety} = \text{IF}(\text{Stress_ratio} \leq 1; "Safe"; "Unsafe") = \text{Safe}$$



Design Summary

$f_{ra} =$	$\frac{P_u}{A}$	=	10.0 ksi
$F_{ca} =$	$\frac{\Phi_c * P_n}{A}$	=	32.0 ksi
$f_{rbx} =$	$12 * \frac{M_{ux}}{S_x}$	=	5.8 ksi
$F_{bcx} =$	$12 * \frac{\Phi_b * M_{nx}}{S_x}$	=	45.4 ksi
$f_{rby} =$	$12 * \frac{M_{uy}}{S_y}$	=	24.8 ksi
$F_{bcy} =$	$12 * \frac{\Phi_b * M_{ny}}{S_y}$	=	68.7 ksi
Stress_ratio =	$\frac{f_{ra}}{F_{ca}} + \frac{f_{rbx}}{F_{bcx}} + \frac{f_{rby}}{F_{bcy}}$	=	0.80
Safety =	IF(Stress_ratio ≤ 1; "Safe"; "Unsafe")	=	Safe



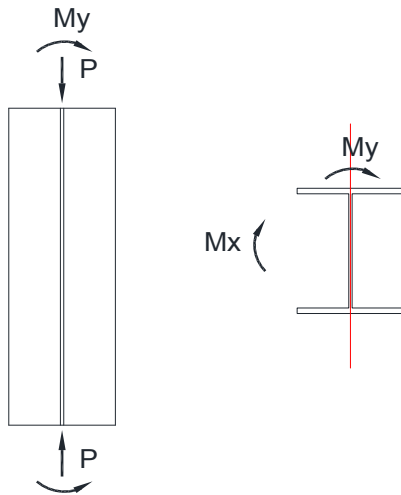
Chapter 3: Steel Design

W-Shape Subjected to P and M including the Second Order Effect

AISC

Page: 134

Design of W-Shapes Subjected to Axial Compression and Moments including the Second Order Effect



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
E=			29000 ksi

Beam Length and C_b (The member is not subjected to sidesway)

Unsupported length, L_b =		14.00 ft
Strong axis unbraced length, kL_{in} =		14.00 ft
Weak axis and torsional unbraced length, kL_{out} =		14.00 ft
From Table 3-1 (AISC), C_b =		1.14

Given Straining Actions (Not including second-order effects)

P_D =		5.0 kips
P_L =		15.0 kips
M_{xD} =		15.0 kip*ft
M_{xL} =		45.0 kip*ft
M_{yD} =		2.0 kip*ft
M_{yL} =		6.0 kip*ft

From Chapter 2 of ASCE/SEI 7, the required strength (not considering second-order effects) is:

P_u =	$1.2*P_D+1.6*P_L$	=	30.0 kips
M_{ux1} =	$1.2*M_{xD}+1.6*M_{xL}$	=	90.0 kip*ft
M_{uy1} =	$1.2*M_{yD}+1.6*M_{yL}$	=	12.0 kip*ft



Chapter 3: Steel Design

W-Shape Subjected to P and M including the Second Order Effect

AISC

Page: 135

Section Details

sec.:	SEL("AISC/W";NAME;)	=	W10X33
depth, d=	TAB("AISC/W";d;NAME=sec.)	=	9.73 in
Web th., t_w =	TAB("AISC/W"; t_w ;NAME=sec.)	=	0.29 in
Flange width, b_f =	TAB("AISC/W"; b_f ;NAME=sec.)	=	7.96 in
Flange th., t_f =	TAB("AISC/W"; t_f ;NAME=sec.)	=	0.44 in
Gross Area, A=	TAB("AISC/W";A;NAME=sec.)	=	9.71 in ²
I_x =	TAB("AISC/W"; I_x ;NAME=sec.)	=	171.00 in ⁴
I_y =	TAB("AISC/W"; I_y ;NAME=sec.)	=	36.60 in ⁴
<i>(I_x and I_y are the moment of inertia about x-and y-axes, respectively)</i>			
Plastic sec. modulus, Z_x =	TAB("AISC/W"; Z_x ;NAME=sec.)	=	38.80 in ³
Elastic sec. modulus, S_x =	TAB("AISC/W"; S_x ;NAME=sec.)	=	35.00 in ³
Plastic sec. modulus, Z_y =	TAB("AISC/W"; Z_y ;NAME=sec.)	=	14.00 in ³
Elastic sec. modulus, S_y =	TAB("AISC/W"; S_y ;NAME=sec.)	=	9.20 in ³
r_x =	TAB("AISC/W"; r_x ;NAME=sec.)	=	4.19 in
r_y =	TAB("AISC/W"; r_y ;NAME=sec.)	=	1.94 in
<i>(r_x and r_y are the radius of gyration about x- and y- axis, respectively)</i>			
Torsional constant, J=	TAB("AISC/W";J;NAME=sec.)	=	0.58 in ⁴
r_{ts} =	TAB("AISC/W"; r_{ts} ;NAME=sec.)	=	2.20 in
h_o =	TAB("AISC/W"; h_o ;NAME=sec.)	=	9.30 in
<i>(r_{ts} is the Effective radius of gyration for the L.T.B. and h_o is distance between C.L. of flanges)</i>			
AISC Specification Eqn. (F2-1), yielding Moment in major axis (M_{px}):			
M_{px} =	$Z_x * F_y * 1/12$	=	162 kip*ft
AISC Specification Eqn. (F6-1), yielding Moment in minor axis (M_{py}):			
M_{py} =	$\text{MIN}(Z_y * F_y * 1/12; 1.6/12 * S_y * F_y)$	=	58 kip*ft



Chapter 3: Steel Design

W-Shape Subjected to P and M including the Second Order Effect

AISC

Page: 136

Required Flexural Strength (including second-order amplification)

Use the approximate method of second-order analysis procedure from AISC Specification Appendix 8.

Because the member is not subject to sidesway, only P-δ amplifiers need to be added.

$$B_1 = \frac{C_m}{1 - \alpha * P_r / P_{e1}} \geq 1 \quad (\text{Spec. Eq. A-8-3})$$

The x-x axis flexural magnifier is,

$$C_{mx} = 1.00$$

$$P_{e1} = \frac{\pi^2 * E * I_x}{(kL_{in} * 12)^2} = 1734 \text{ kips}$$

$$\alpha = 1.00$$

$$B_{1x} = \frac{C_{mx}}{1 - \alpha * P_u / P_{e1}} = 1.02$$

$$M_{ux} = B_{1x} * M_{ux1} = 91.8 \text{ kip*ft}$$

The Y-Y axis flexural magnifier is,

$$P_{e2} = \frac{\pi^2 * E * I_y}{(kL_{out} * 12)^2} = 371.2 \text{ kips}$$

$$C_{my} = 1.00$$

$$B_{1y} = \frac{C_{my}}{1 - \alpha * P_u / P_{e2}} = 1.09$$

$$M_{uy} = B_{1y} * M_{uy1} = 13.1 \text{ kip*ft}$$

Element Classification

(1) Web:

$$h/t_w, \lambda_w = \text{TAB}(\text{"AISC/W"; } h/t_w; \text{NAME=sec.}) = 27.10$$

According to AISC Specification Table B4.1 Case 9, the limiting width-to-thickness ratio for the web is:

$$\text{Web_Class} = \text{IF}(\lambda_w \leq 3.76 * \sqrt{E/F_y}, \text{"Compact"; "Non-Compact"}) = \text{Compact}$$

(2) Comp. flange:

$$b_f/2t_f, \lambda_f = \text{TAB}(\text{"AISC/W"; } b_f/2t_f; \text{NAME=sec.}) = 9.15$$

According to AISC Specification Table B4.1 Case 1, the limiting width-to-thickness ratios for the compression flange are:

$$\lambda_{pf} = 0.38 * \sqrt{E/F_y} = 9$$

$$\lambda_{rf} = 1.00 * \sqrt{E/F_y} = 24$$

$$\text{Fl_Class} = \text{IF}(\lambda_f \leq \lambda_{pf}, \text{"Compact"; IF}(\lambda_f > \lambda_{rf}, \text{"Slender"; "Non-Compact"})) = \text{Non-Compact}$$



Chapter 3: Steel Design

W-Shape Subjected to P and M including the Second Order Effect

AISC

Page: 137

The available strength provided by AISC Specification Sections F3.1, F3.2, F6.1 and F6.2, the nominal flexural moments in strong/weak axes are calculated as follows, satisfying the condition of compression Flange Local Buckling:

$$M_{nx1a} = M_{px} - 0.7 * F_y * S_x * 1/12 = 60 \text{ kip*ft}$$

$$M_{nx1} = \text{IF}(\text{FI_Class} = \text{"Compact"}; M_{px}; (M_{px} - M_{nx1a} * (\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}))) = 161 \text{ kip*ft}$$

$$M_{ny1a} = M_{py} - 0.7 * F_y * S_y * 1/12 = 31 \text{ kip*ft}$$

$$M_{ny1} = \text{IF}(\text{FI_Class} = \text{"Compact"}; M_{py}; (M_{py} - M_{ny1a} * (\frac{\lambda_f - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}))) = 58 \text{ kip*ft}$$

Slenderness Check (According to section E2)

For members designed on the basis of compression, the slenderness ratio KL/r preferably should not exceed 200.

$$\lambda_x = \frac{KL_{in}}{r_x} * 12 = 40.1$$

$$\lambda_y = \frac{KL_{out}}{r_y} * 12 = 86.6$$

Then, the governed slenderness (λ_{max}):

$$\lambda_{max} = \text{MAX}(\lambda_x; \lambda_y) = 86.6$$

Critical Stresses

The available critical stresses may be interpolated from AISC Manual Table 4-22 or calculated directly as follows:

-Calculate the elastic critical buckling stress, F_e :

$$F_e = \frac{\pi^2 * E}{\lambda_{max}^2} = 38.2 \text{ ksi}$$

-Calculate the flexural buckling stress, F_{cr} (Eqns. E3-2 and E3-3):

$$\lambda_1 = 4.71 * \sqrt{E/F_y} = 113$$

$$F_{cr} = \text{IF}(\lambda_{max} \leq \lambda_1; (0.658)^{\left(\frac{F_y}{F_e}\right)} * F_y; 0.877 * F_e) = 28.9 \text{ ksi}$$



Chapter 3: Steel Design

W-Shape Subjected to P and M including the Second Order Effect

AISC

Page: 138

Design Compressive Strength (Eqn. E3-1)

$$P_n = F_{cr} * A = 281 \text{ kips}$$

$$\Phi_c = 0.90$$

$$\Phi_c P_n = 253 \text{ kips}$$

Lateral Torsional Buckling (LTB)

The limiting lengths L_p and L_r are determined according to the AISC Spec. Eqns. F2-5 and F2-6, as follows:

$$L_p = 1.76 * r_y * \sqrt{(E/F_y)/12} = 6.85 \text{ ft}$$

$$L_{r1} = \sqrt{\frac{J * 1.0}{S_x * h_o}} = 0.04$$

$$L_{r2} = \sqrt{1 + \sqrt{6.76 * \left(\frac{0.7 * F_y * S_x * h_o}{E * J * 1.0}\right)^2}} = 1.66$$

$$L_r = 1.95/12 * r_{ts} * \frac{E}{0.7 * F_y} * L_{r1} * L_{r2} = 19.67 \text{ ft}$$

$$\text{Case} = \text{IF}(L_b > L_r, \text{"ELTB"}; \text{IF}(L_b \leq L_p, \text{"No LTB"}; \text{"InLTB"})) = \text{InLTB}$$

("ELTB" refers to elastic LTB and "InLTB" refers to inelastic LTB)

According to the AISC Spec. Eqn. F2-2:

$$M_{1a} = M_{px} - 0.7 * 1/12 * F_y * S_x = 59.9 \text{ kip*ft}$$

$$M_1 = \text{MIN}(M_{px}; C_b * (M_{px} - M_{1a} * (L_b - L_p) / (L_r - L_p))) = 147 \text{ kip*ft}$$

According to the AISC Spec. Eqn. F2-4:

$$F_{cr} = C_b * \pi^2 * E / ((L_b + 0.01) * 12 / r_{ts})^2 = 55.87 \text{ ksi}$$

$$F_{cr,mod} = \sqrt{(1 + 0.078 * J * 1.0 / (S_x * h_o) * (L_b * 12 / r_{ts})^2)} = 1.35$$

According to the AISC Spec. Eqns. F2-3:

$$M_2 = \text{MIN}(M_{px}; F_{cr} * S_x / 12 * F_{cr,mod}) = 162 \text{ kip*ft}$$

According to the AISC Spec. Eqn. F2-2:

$$M_{nx2} = \text{IF}(\text{Case} = \text{"No LTB"}; M_{px}; \text{IF}(\text{Case} = \text{"InLTB"}; M_1; M_2)) = 147.0 \text{ kip*ft}$$

Design Flexure Moment in Major/Minor Axes

$$\Phi_b = 0.90$$

$$M_{nx} = \text{MIN}(M_{px}; M_{nx1}; M_{nx2}) = 147.0 \text{ kip*ft}$$

$$M_{ny} = \text{MIN}(M_{py}; M_{ny1}) = 58.0 \text{ kip*ft}$$



Chapter 3: Steel Design

W-Shape Subjected to P and M including the Second Order Effect

AISC

Page: 139

Calculate The Available Flexural and Axial Strengths

$$\begin{aligned} P_c &= \Phi_c * P_n &= & 252.90 \text{ kips} \\ M_{cx} &= \Phi_b * M_{nx} &= & 132.3 \text{ kip*ft} \\ M_{cy} &= \Phi_b * M_{ny} &= & 52.20 \text{ kip*ft} \end{aligned}$$

Check The Combined Stress Ratio (AISC Specification Section H1-1a and H1-1b)

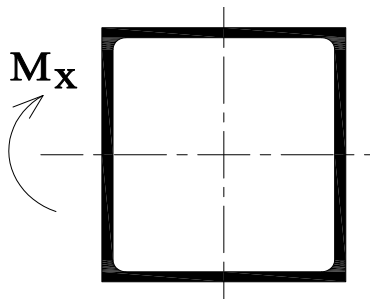
$$\begin{aligned} \text{Axial ratio, } p &= \frac{P_u}{P_c} &= & 0.12 \\ \text{Moments ratio, } m &= \frac{M_{ux}}{M_{cx}} + \frac{M_{uy}}{M_{cy}} &= & 0.94 \\ \text{Stress_ratio} &= \text{IF}(p \geq 0.2; (p + 8/9 * m); (p/2 + m)) &= & 1.00 \text{ in} \\ \text{Safety} &= \text{IF}(\text{Stress_ratio} \leq 1; \text{"Safe"}; \text{"Unsafe"}) &= & \text{Safe} \end{aligned}$$

Design Summary

$$\begin{aligned} P_c &= \Phi_c * P_n &= & 252.9 \text{ kips} \\ M_{cx} &= \Phi_b * M_{nx} &= & 132.3 \text{ kip*ft} \\ M_{cy} &= \Phi_b * M_{ny} &= & 52.2 \text{ kip*ft} \\ \text{Stress_ratio} &= \text{IF}(p \geq 0.2; (p + 8/9 * m); (p/2 + m)) &= & 1.00 \\ \text{Safety} &= \text{IF}(\text{Stress_ratio} \leq 1; \text{"Safe"}; \text{"Unsafe"}) &= & \text{Safe} \end{aligned}$$



Design of HSS-Shapes Subjected to Moment about Strong Axis



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A500
F _y =	TAB("Material/ASTM";F _y ;NAME=Grade)	=	46 ksi
E=			29000 ksi

Beam Length and C_b

Total length, L=			50.00 ft
------------------	--	--	----------

Design Moments and Uniform Live Load

Ultimate moment, M _u =			150.00 kip*ft
Ultimate moment due to live load case, M _L =			80.00 kip*ft
Ultimate Shear force, Q _u =			66 kips

Section Details

sec.:	SEL("AISC/HSS";NAME;)	=	HSS18X6X3/8
depth, H _t =	TAB("AISC/HSS";H _t ;NAME=sec.)	=	18.00 in
HSS th., t _{des} =	TAB("AISC/HSS";t _{des} ;NAME=sec.)	=	0.349 in
HSS width, b=	TAB("AISC/HSS";B;NAME=sec.)	=	6.00 in
Plastic sec. modulus, Z _x =	TAB("AISC/HSS";Z _x ;NAME=sec.)	=	86.40 in ³
Elastic sec. modulus, S _x =	TAB("AISC/HSS";S _x ;NAME=sec.)	=	66.90 in ³
Inertia about x-axis, I _x =	TAB("AISC/HSS";I _x ;NAME=sec.)	=	602.00 in ⁴
Yielding Moment, M _p =	Z _x *F _y *1/12	=	331 kip*ft



Chapter 3: Steel Design

HSS-Shape in Strong Axis Bending

AISC

Page: 141

Element Classification

(1) Web:

$$h/t_{des}, \lambda_w = \text{TAB}(\text{"AISC/HSS"; } h/t_{des}; \text{NAME=sec.}) = 48.70$$

Determine the limiting ratio for a compact HSS web in flexure from AISC Specification Table B4.1b Case 19.

$$\lambda_{wr} = 2.42 * \sqrt{(E/F_y)} = 60.8$$

$$\text{Web_Class} = \text{IF}(\lambda_w \leq \lambda_{wr}, \text{"Compact"; "Non-Compact"}) = \text{Compact}$$

(2) Comp. flange:

$$b/t_{des}, \lambda_f = \text{TAB}(\text{"AISC/HSS"; } b/t_{des}; \text{NAME=sec.}) = 14.20$$

Determine the limiting ratio for a slender HSS flange in flexure from AISC Specification Table B4.1b Case 17.

$$\lambda_{fr} = 1.12 * \sqrt{(E/F_y)} = 28.1$$

$$\text{Fl_Class} = \text{IF}(\lambda_f \leq \lambda_{fr}, \text{"Compact"; "Non-Compact"}) = \text{Compact}$$

$$M_{n1a} = M_p - F_y * S_x * 1/12 = 74.55 \text{ kip*ft}$$

$$\lambda_{fa} = 3.57 * \lambda_f * \sqrt{\frac{F_y}{E} - 4} = -1.98$$

$$M_{n1b} = \text{MIN}(M_p; M_p - M_{n1a} * \lambda_{fa}) = 331.0 \text{ kip*ft}$$

$$M_{n1} = \text{IF}(\text{Fl_Class} = \text{"Compact"; } M_p; M_{n1b}) = 331.0 \text{ kip*ft}$$

(Note that For HSS with noncompact flanges and compact webs, AISC Specification Section F7.2(b) applies)

Check The Available Flexure Strength

$$\Phi M_n = 0.90 * \text{MIN}(M_p; M_{n1}) = 298 \text{ kip*ft}$$

$$\text{Safety} = \text{IF}(\Phi M_n \geq M_u, \text{"Safe"; "Unsafe"}) = \text{Safe}$$

$$\text{Moment ratio} = M_u / \Phi M_n = 0.50$$

Check Shear Strength

From AISC Specification Section G5, if the exact radius is unknown, h shall be taken as the corresponding outside dimension minus three times the design thickness.

$$h = H_t - 3 * t_{des} = 17 \text{ in}$$

$$\lambda_w = \text{TAB}(\text{"AISC/HSS"; } h/t_{des}; \text{NAME=sec.}) = 48.70$$



Chapter 3: Steel Design

HSS-Shape in Strong Axis Bending

For rectangular HSS in shear, use AISC Specification Section G2.1 with $A_w = 2ht$ (per AISC Specification Section G5) and $k_v = 5$.

$k_v =$			5
$\lambda_{w1} =$	$1.1 \cdot \sqrt{(k_v \cdot E / F_y)}$	=	62
$\lambda_{w2} =$	$1.37 \cdot \sqrt{(k_v \cdot E / F_y)}$	=	77
$C_{va} =$	$1.51 \cdot 5 \cdot E / (F_y \cdot \lambda_w^2)$	=	2.0
$C_v =$	$\text{IF}(\lambda_w \leq \lambda_{w1}; 1; \text{IF}((\lambda_w > \lambda_{w1} \text{ AND } \lambda_w \leq \lambda_{w2}); \lambda_{w1} / \lambda_w; C_{va}))$	=	1
$A_w =$	$2 \cdot h \cdot t_{des}$	=	12 in ²
Nominal shear strength (V_n):			
$V_n =$	$0.6 \cdot F_y \cdot A_w \cdot C_v$	=	331.20 kips
From AISC Specification Section G1, the available shear strength is:			
$\Phi_v =$			0.90
$\Phi_v V_n =$	$\Phi_v \cdot V_n$	=	298.08 kips
Shear_safety =	$\text{IF}(\Phi_v \cdot V_n > Q_u; \text{"Safe"}; \text{"Unsafe"})$	=	Safe

Check Deflection

$\Delta_{all} =$	$L / 240$	=	0.21 ft
$W_{eq} (LL), W_L =$	$\frac{8 \cdot M_L}{L^2}$	=	0.26 kip/ft
$\Delta_{act} =$	$12^2 \cdot \frac{5 \cdot W_L \cdot L^4}{384 \cdot E \cdot I_x}$	=	0.175 ft
Deflection safety, $D_s =$	$\text{IF}(\Delta_{all} \geq \Delta_{act}; \text{"Safe"}; \text{"Increase section"})$	=	Safe

Design Summary

$\Phi M_n =$	$0.90 \cdot \text{MIN}(M_p; M_{n1})$	=	298 kip*ft
Safety =	$\text{IF}(\Phi M_n \geq M_u; \text{"Safe"}; \text{"Unsafe"})$	=	Safe
Moment ratio =	$M_u / \Phi M_n$	=	0.50
$\Phi_v V_n =$	$\Phi_v \cdot V_n$	=	298 kips
Shear_safety =	$\text{IF}(\Phi_v \cdot V_n > Q_u; \text{"Safe"}; \text{"Unsafe"})$	=	Safe
$\Delta_{act} =$	$\frac{5 \cdot W_L \cdot L^4}{384 \cdot E \cdot I_x}$	=	0.00 ft
$\Delta_{all} =$	$L / 240$	=	0.21 ft
Deflection safety, $D_s =$	$\text{IF}(\Delta_{all} \geq \Delta_{act}; \text{"Safe"}; \text{"Increase section"})$	=	Safe



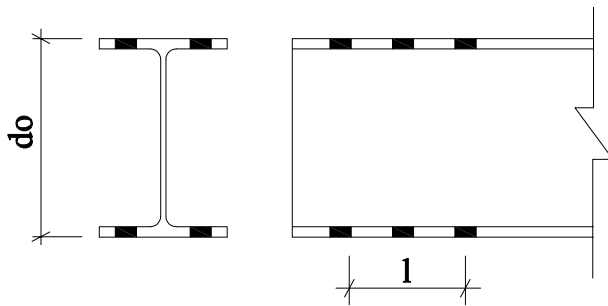
Chapter 3: Steel Design

W-Shape Subjected to Tension Force in a Bolted Connection

AISC

Page: 143

Design of W-Shapes Subjected to Tension Force in a Bolted Connection



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
F_u =	TAB("Material/ASTM"; F_u ;NAME=Grade)	=	65 ksi

Buckling Lengths

Member length, L=			25.00 ft
-------------------	--	--	----------

Axial Loads

Axial dead load, P_D =			30 kips
--------------------------	--	--	---------

Axial Live load, P_L =			90 kips
--------------------------	--	--	---------

From Chapter 2 of ASCE/SEI 7, the required compressive strength is:

Ultimate load, P_u =	$1.2 \cdot P_D + 1.6 \cdot P_L$	=	180 kips
------------------------	---------------------------------	---	----------

Section and Connection Details

sec.:	SEL("AISC/W";NAME;)	=	W12X106
depth, d_o =	TAB("AISC/W";d;NAME=sec.)	=	12.90 in
Web th., t_w =	TAB("AISC/W"; t_w ;NAME=sec.)	=	0.61 in
Flange width, b_f =	TAB("AISC/W"; b_f ;NAME=sec.)	=	12.20 in
Flange th., t_f =	TAB("AISC/W"; t_f ;NAME=sec.)	=	0.99 in
Gross Area, A_g =	TAB("AISC/W";A;NAME=sec.)	=	31.20 in ²
r_x =	TAB("AISC/W"; r_x ;NAME=sec.)	=	5.47 in
r_y =	TAB("AISC/W"; r_y ;NAME=sec.)	=	3.11 in

(r_x and r_y are the radius of gyration about x- and y- axis)



Chapter 3: Steel Design

W-Shape Subjected to Tension Force in a Bolted Connection

AISC

Page: 144

Rounded depth, d_{WT} =	TAB("AISC/W"; d_{WT} ;NAME=sec.)	=	13.00 in
WT=	TAB("AISC/WT";NAME; $d_{ro}=d_{WT}/2$)	=	WT6X53
y =	TAB("AISC/WT"; y;NAME=WT)	=	1.190 in
Bolt_diameter:	SEL("AISC/Bolt";Size;)	=	d3/4
d_b =	TAB("AISC/Bolt";dia;Size=Bolt_diameter)	=	0.750 in
hole diameter, d_h =	$d_b+1/16$	=	0.813 in
Connection length, l =			9.00 in

Check Tensile Yielding

From AISC Manual Table 5-1, the tensile yielding strength is:

Φ_{t1} =		=	0.90
P_{n1} =	$\Phi_{t1} * F_y * A_g$	=	1404.0 kips
Yield_safety=	IF($P_u \leq P_{n1}$;"Safe";"Unsafe")	=	Safe

Check Tensile Rupture

Calculate the shear lag factor, U, as the larger of the values from AISC specification section D3, Table D3.1 case 2 and case 7. From AISC Specification Section D3, for open cross sections, U need not be less than the ratio of the gross area of the connected element(s) to the member gross area.

$$U_1 = \frac{2 * b_f * t_f}{A_g} = 0.774$$

Case 2: Check as two WT-shapes per AISC Specification Commentary Figure C-D3.1

$$U_2 = 1 - \frac{y}{l} = 0.868$$

Case 7:

$$U_3 = \text{IF}(b_f \geq 2/3 * d_o; 0.90; 0.85) = 0.900$$

$$U = \text{MAX}(U_1; U_2; U_3) = 0.900$$

Effective Net Area

Calculate A_n using AISC Specification Section B4.3.

$$A_n = A_g - 4 * (d_h + 1/16) * t_f = 27.73 \text{ in}^2$$

Calculate A_e using AISC Specification Section D3

$$A_e = A_n * U = 24.96 \text{ in}^2$$



Chapter 3: Steel Design

W-Shape Subjected to Tension Force in a Bolted Connection

AISC

Page: 145

Available Tensile Rupture Strength

$$\begin{aligned} P_2 &= F_u * A_e &= 1622.4 \text{ kips} \\ \Phi_{t2} & &= 0.75 \\ P_{n2} &= P_2 * \Phi_{t2} &= 1216.8 \text{ kips} \\ \text{Rupture_safety} &= \text{IF}(P_u \leq P_{n1}, \text{"Safe"}, \text{"Unsafe"}) &= \text{Safe} \end{aligned}$$

Slenderness Check (According to section D1)

For members designed on the basis of compression, the slenderness ratio KL/r should not exceed 300.

$$\begin{aligned} \lambda_{\max} &= \frac{L}{r_y} * 12 &= 96.5 \\ \text{Slenderness_limit} &= \text{IF}(\lambda_{\max} \leq 300, \text{"Safe"}, \text{"Unsafe"}) &= \text{Safe} \end{aligned}$$

Design Summary

$$\begin{aligned} \text{Ultimate load, } P_u &= 1.2 * P_D + 1.6 * P_L &= 180.0 \text{ kips} \\ P_{n1} &= \Phi_{t1} * F_y * A_g &= 1404.0 \text{ kips} \\ \text{Yield_safety} &= \text{IF}(P_u \leq P_{n1}, \text{"Safe"}, \text{"Unsafe"}) &= \text{Safe} \\ P_{n2} &= P_2 * \Phi_{t2} &= 1216.8 \text{ kips} \\ \text{Rupture_safety} &= \text{IF}(P_u \leq P_{n1}, \text{"Safe"}, \text{"Unsafe"}) &= \text{Safe} \\ \text{Slenderness_limit} &= \text{IF}(\lambda_{\max} \leq 300, \text{"Safe"}, \text{"Unsafe"}) &= \text{Safe} \end{aligned}$$



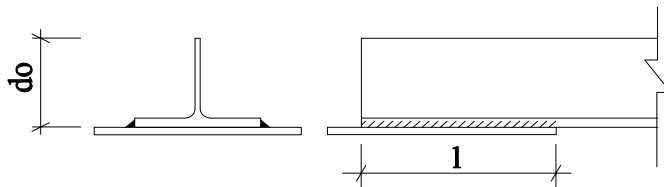
Chapter 3: Steel Design

WT-Shape Subjected to Tension Force in Welded Connections

AISC

Page: 146

Design of WT-Shapes Subjected to Tension Force in Welded Connections



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	50 ksi
F_u =	TAB("Material/ASTM"; F_u ; NAME=Grade)	=	65 ksi

Buckling Length

Member length, L=			30.00 ft
-------------------	--	--	----------

Axial Loads

Axial dead load, P_D =			40 kips
Axial Live load, P_L =			120 kips
From Chapter 2 of ASCE/SEI 7, the required compressive strength is:			
Ultimate load, P_u =	$1.2 \cdot P_D + 1.6 \cdot P_L$	=	240 kips

Section and Connection Details

sec.:	SEL("AISC/WT"; NAME;)	=	WT6X20
depth, d_o =	TAB("AISC/WT"; d; NAME=sec.)	=	5.97 in
Web th., t_w =	TAB("AISC/WT"; t_w ; NAME=sec.)	=	0.29 in
Flange width, b_f =	TAB("AISC/WT"; b_f ; NAME=sec.)	=	8.01 in
Flange th., t_f =	TAB("AISC/WT"; t_f ; NAME=sec.)	=	0.515 in
Gross Area, A_g =	TAB("AISC/WT"; A; NAME=sec.)	=	5.84 in ²
r_x =	TAB("AISC/WT"; r_x ; NAME=sec.)	=	1.57 in
r_y =	TAB("AISC/WT"; r_y ; NAME=sec.)	=	1.94 in
(r_x and r_y are the radius of gyration about x- and y- axis)			
Distance to centroid, y =	TAB("AISC/WT"; y; NAME=sec.)	=	1.09 in
Connection length, l =			16.00 in



Chapter 3: Steel Design

WT-Shape Subjected to Tension Force in Welded Connections

AISC

Page: 147

Check Tensile Yielding

From AISC *Manual* Table 5-1, the tensile yielding strength is:

$$\begin{aligned}\Phi_{t1} &= && 0.90 \\ P_{n1} &= \Phi_{t1} * F_y * A_g &= & 262.8 \text{ kips} \\ \text{Yield_safety} &= \text{IF}(P_u \leq P_{n1}; \text{"Safe"}; \text{"Unsafe"}) &= & \text{Safe}\end{aligned}$$

Check Tensile Rupture

Calculate the shear lag factor, U , as the larger of the values from AISC Specification Section D3, Table D3.1 case 2 and case 7. From AISC Specification Section D3, for open cross sections, U need not be less than the ratio of the gross area of the connected element(s) to the member gross area.

$$U_1 = \frac{b_f * t_f}{A_g} = 0.706$$

Case 2: Check as two WT-shapes per AISC Specification Commentary Figure C-D3.1

$$U_2 = 1 - \frac{y}{l} = 0.932$$

Case 7:

$$U_3 = \text{IF}(b_f \geq 2/3 * d_o; 0.90; 0.85) = 0.900$$

$$U = \text{MAX}(U_1; U_2; U_3) = 0.932$$

Effective Net Area

Calculate A_n using AISC Specification Section B4.3.

$$A_n = A_g = 5.8 \text{ in}^2$$

Calculate A_e using AISC Specification Section D3

$$A_e = A_n * U = 5.4 \text{ in}^2$$

Available Tensile Rupture Strength

$$P_2 = F_u * A_e = 351.0 \text{ kips}$$

$$\Phi_{t2} = 0.75$$

$$P_{n2} = P_2 * \Phi_{t2} = 263.3 \text{ kips}$$

$$\text{Rupture_safety} = \text{IF}(P_u \leq P_{n1}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



Chapter 3: Steel Design

WT-Shape Subjected to Tension Force in Welded Connections

AISC

Page: 148

Slenderness Check (According to section D1)

For members designed on the basis of compression, the slenderness ratio KL/r should not exceed 300.

$$r_{\min} = \text{MIN}(r_x; r_y) = 1.57 \text{ in}$$

$$\lambda_{\max} = \frac{L}{r_{\min}} * 12 = 229.3$$

$$\text{Slenderness_limit} = \text{IF}(\lambda_{\max} \leq 300; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Design Summary

$$\text{Ultimate load, } P_u = 1.2 * P_D + 1.6 * P_L = 240.0 \text{ kips}$$

$$P_{n1} = \Phi_{t1} * F_y * A_g = 262.8 \text{ kips}$$

$$\text{Yield_safety} = \text{IF}(P_u \leq P_{n1}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

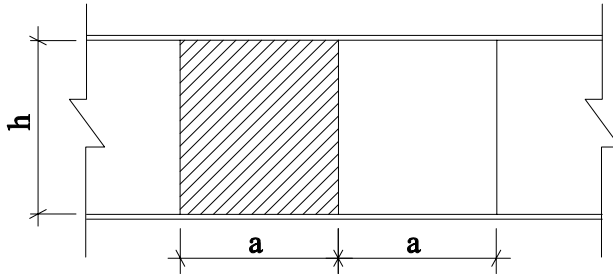
$$P_{n2} = P_2 * \Phi_{t2} = 263.3 \text{ kips}$$

$$\text{Rupture_safety} = \text{IF}(P_u \leq P_{n1}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\text{Slenderness_limit} = \text{IF}(\lambda_{\max} \leq 300; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



Design of Interior Panel of Built-Up Girder with Transverse Stiffeners Subjected to Shear Force



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A36
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	36 ksi
E =			29000 ksi

Loads

The required shear strength at the start of this panel from the end , V_u :

V_u =			120 kips
---------	--	--	----------

Section Details

Depth, d =			36 in
Web thickness, t_w =			0.3125 in
Clear distance between stiffeners, a =			99 in
Upper flange width, b_{fc} =			12 in
Upper flange thickness, t_{fc} =			1.50 in
Lower flange width, b_{ft} =			12.00 in
Lower flange thickness, t_{ft} =			1.50 in

Shear Strength for this Panel

h =	$d - t_{fc} - t_{ft}$	=	33.00 in
ψ =	a/h	=	3.00
k_{v1} =	$5 + (5/\psi^2)$	=	5.56

Based on AISC Specification Section G2.1, $k_v=5$ when $a/h > 3$ or $a/h > [260/(h/t_w)]^2$

λ_w =	h/t_w	=	106
ψ_1 =	$(260/\lambda_w)^2$	=	6.02
Use k_v =	IF($\psi > 3$ AND $\psi > \psi_1; 5; k_{v1}$)	=	5.56
λ_{w1} =	$1.10 \cdot \sqrt{(k_v \cdot E/F_y)}$	=	74
λ_{w2} =	$1.37 \cdot \sqrt{(k_v \cdot E/F_y)}$	=	92



Calculate C_v according to Eqns. G2-2, G2-3, G2-4 and G2-5:

$$C_{v1} = \text{IF}(\lambda_w \leq \lambda_{w1}; 1; \text{IF}(\lambda_w > \lambda_{w1} \text{ AND } \lambda_w \leq \lambda_{w2}; \lambda_{w1}/\lambda_w; 1.51 * k_v * E / (F_y * \lambda_w^2))) = 0.60$$

Check the additional limits from AISC Specification Section G3.1 for the use of tension field action:

$$A_w = d * t_w = 11.3 \text{ in}^2$$

$$\eta = \frac{A_w * 2}{b_{fc} * t_{fc} + b_{ft} * t_{ft}} = 0.63$$

$$v_{fc} = \frac{h}{b_{fc}} = 2.75$$

$$v_{ft} = \frac{h}{b_{ft}} = 2.75$$

$$\text{Check_TF} = \text{IF}(\psi > \text{MIN}(3; \psi_1) \text{ AND } \eta > 2.5 \text{ AND } v_{fc} > 6 \text{ AND } v_{ft} > 6; "1"; "2") = 2$$

$$\text{Case} = \text{IF}(\text{Check_TF} = "1"; "NP"; "P") = P$$

"P": permitted and "NP": not permitted

Calculate C_v and V_n , according to Section G3-2a and b:

$$C_{v2} = \text{IF}(\lambda_w \leq \lambda_{w1}; 1; (C_{v1} + \frac{1 - C_{v1}}{1.15 * \sqrt{1 + (\frac{a}{h})^2}})) = 0.71$$

Nominal shear strength:

$$V_n = \text{IF}(\text{Case} = \text{"PERMITTED"}; 0.6 * F_y * A_w * C_{v2}; 0.6 * F_y * A_w * C_{v1}) = 146 \text{ kips}$$

$$\Phi_v = 0.90$$

$$\Phi_v V_n = \Phi_v * V_n = 131 \text{ kips}$$

$$\text{Shear_safety} = \text{IF}(\Phi_v * V_n > V_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\text{Force_ratio} = V_u / \Phi_v V_n = 0.92$$

Design Summary

$$V_u = 120 \text{ kips}$$

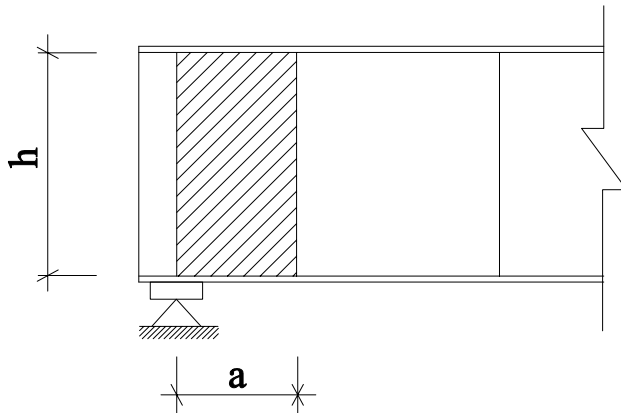
$$\Phi_v V_n = \Phi_v * V_n = 131 \text{ kips}$$

$$\text{Force_ratio} = V_u / \Phi_v V_n = 0.92$$

$$\text{Shear_safety} = \text{IF}(\Phi_v * V_n > V_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



Design of End Panel of Built-Up Girder with Transverse Stiffeners Subjected to Shear Force



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A36
F_y =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	36 ksi
E =			29000 ksi

Loads

Reaction at support, R_v =			154.0 kips
------------------------------	--	--	------------

Section Details

depth, d =			36 in
Web thickness, t_w =			0.3125 in
clear distance between stiffeners, a =			60.00 in
Upper flange width, b_{fc} =			12 in
Upper flange thickness, t_{fc} =			1.50 in
Lower flange width, b_{ft} =			12.00 in
Lower flange thickness, t_{ft} =			1.50 in

Shear Strength for End Panel

h =	$d - t_{fc} - t_{ft}$	=	33.00 in
ψ =	a/h	=	1.82
k_{v1} =	$5 + (5/\psi^2)$	=	6.51
Based on AISC Specification Section G2.1, $k_v=5$ when $a/h > 3$ or $a/h > [260/(h/t_w)]^2$			
λ_w =	h/t_w	=	106
ψ_1 =	$(260/\lambda_w)^2$	=	6.02
Therefore, use k_v =	IF($\psi > 3$ AND $\psi > \psi_1$; 5; k_{v1})	=	6.51



Tension field action is not allowed because the panel is an end panel.

$$\lambda_{w1} = 1.10 \sqrt{(k_v * E / F_y)} = 80$$

$$\lambda_{w2} = 1.37 \sqrt{(k_v * E / F_y)} = 99$$

Calculate C_v according to Eqns. G2-2, G2-3, G2-4 and G2-5:

$$C_v = \text{IF}(\lambda_w \leq \lambda_{w1}; 1; \text{IF}(\lambda_w > \lambda_{w1} \text{ AND } \lambda_w \leq \lambda_{w2}; \lambda_{w1} / \lambda_w; 1.51 * k_v * E / (F_y * \lambda_w^2))) = 0.705$$

$$A_w = d * t_w = 11.3 \text{ in}^2$$

Calculate V_n using Eqn. G2-1:

$$\text{Nominal shear strength, } V_n = 0.6 * F_y * A_w * C_v = 172 \text{ kips}$$

$$\Phi_v = 0.90$$

$$\Phi_v V_n = \Phi_v * V_n = 155 \text{ kips}$$

$$\text{Shear_safety} = \text{IF}(\Phi_v * V_n > R_v; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\text{Force_ratio} = R_v / \Phi_v V_n = 0.99$$

Design Summary

$$\text{Reaction at support, } R_v = 154.0 \text{ kips}$$

$$\Phi_v V_n = \Phi_v * V_n = 154.8 \text{ kips}$$

$$\text{Force_ratio} = R_v / \Phi_v V_n = 0.99$$



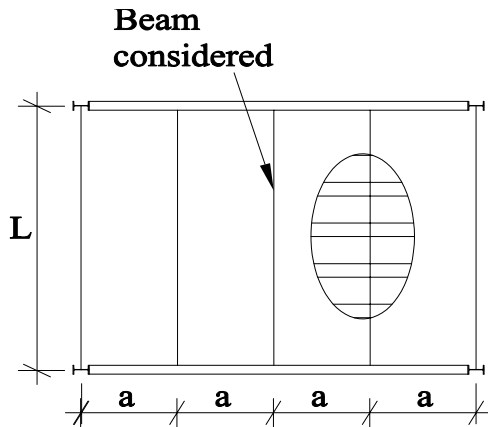
Chapter 3: Steel Design

Composite Beam Subjected to Bending

AISC

Page: 153

Design of Composite Beam Subjected to Bending about its Major Axis



Materials

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
F_u =	TAB("Material/ASTM"; F_u ;NAME=Grade)	=	65 ksi
E_s =			29000 ksi

Beam Length

Total length, L =			45.00 ft
Beam spacing, a =			10.0 ft

Concrete Details

f'_c =			4.0 ksi
Total thickness, t_s =			7.5 in
concrete weight, γ_c =			145.0 lb/ft ³

Loads

Superimposed (HVAC, ceiling, floor covering, etc.), w_{sd} =			10.0 lb/ft ²
Live load for construction (temporary loads during concrete placement), w_{LC} =			25.0 lb/ft ²
Live load non-reducible, w_{LL} =			100.0 lb/ft ²

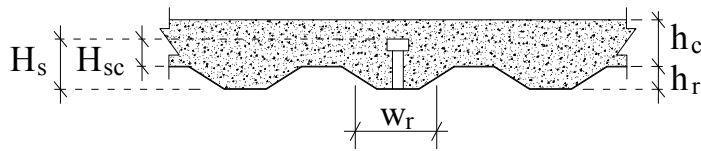
Section Details

sec.:	SEL("AISC/W";NAME;)	=	W21X50
Weight, w_{sec} =	TAB("AISC/W";W;NAME=sec.)	=	50.00 lb/ft
depth, d =	TAB("AISC/W";d;NAME=sec.)	=	20.80 in
Web th., t_w =	TAB("AISC/W"; t_w ;NAME=sec.)	=	0.38 in
Flange width, b_f =	TAB("AISC/W"; b_f ;NAME=sec.)	=	6.53 in



Flange th., t_f =	TAB("AISC/W"; t_f ;NAME=sec.)	=	0.54 in
Gross area, A_s =	TAB("AISC/W";A;NAME=sec.)	=	14.70 in ²
Plastic sec. modulus, Z_x =	TAB("AISC/W"; Z_x ;NAME=sec.)	=	110.00 in ³
Inertia about x-axis, I_x =	TAB("AISC/W"; I_x ;NAME=sec.)	=	984.00 in ⁴
AISC Specification Eqn. (F2-1):			
Yielding Moment, M_p =	$Z_x * F_y * 1/12$	=	458 kip*ft

Metal Deck and Stud Connector Details (in accordance with metal deck manufacturer's data)



Rib height, h_r =			3.0 in
Average rib width, w_r =			6.0 in
weight of slab, w_s =			75.0 lb/ft ²
Diameter of stud, d_{sa} =			0.750 in
Height of stud (minimum is $4d_{sa}$), H_s =			4.50 in
Extension of the stud above the deck (minimum is 1.5 in), H_{sc} =			1.50 in

Composite Deck and Anchor Requirements

Check composite deck and anchor requirements stipulated in AISC Specification Sections I1.3, I3.2c and I8.

- Conc_strength_check =	IF(($f'_c \leq 10$ AND $f'_c \geq 3$) ; "o.k." ; "change f'_c ")	=	o.k.
- h_r _check=	IF($h_r \leq 3$; "o.k." ; "decrease h_r ")	=	o.k.
- w_r _check=	IF($w_r \geq 2$; "o.k." ; "increase w_r ")	=	o.k.
- d_{sa} _check=	IF($d_{sa} \leq 0.75$; "o.k." ; "decrease d_{sa} ")	=	o.k.
- t_f _check=	IF($t_f \geq d_{sa}/2.5$; "o.k." ; "decrease d_{sa} ")	=	o.k.
- H_{sc} _check=	IF(($H_s \geq (h_r + 1.5)$ AND $H_s < t_s - 0.5$); "o.k." ; "unsafe")	=	o.k.
- H_s _check=	IF($H_s \geq 4 * d_{sa}$; "o.k." ; "increase H_s ")	=	o.k.
- h_c _check=	IF(($t_s - h_r$) ≥ 2 ; "o.k." ; "increase h_c ")	=	o.k.



Chapter 3: Steel Design

Composite Beam Subjected to Bending

AISC

Page: 155

Design for Pre-Composite Condition

- Construction Pre-composite Loads:

$$w_{D1} = 0.001 * (w_s * a + w_{sec}) = 0.80 \text{ kip/ft}$$

$$w_{L1} = 0.001 * (w_{LC} * a) = 0.25 \text{ kip/ft}$$

- Construction Pre-composite flexural strength, from Chapter 2 of ASCE/SEI 7, the required flexural strength is:

$$w_{u1} = 1.2 * w_{D1} + 1.6 * w_{L1} = 1.36 \text{ kip/ft}$$

$$M_{u1} = \frac{w_{u1} * L^2}{8} = 344 \text{ kip*ft}$$

Assume that attachment of the deck perpendicular to the beam provides adequate bracing to the compression flange during construction, thus the beam can develop its full plastic moment capacity. The design flexural strength is determined as follows, from AISC Specification Equation F2-1:

$$\Phi_b = 0.90$$

$$M_{n1} = \Phi_b * M_p = 412 \text{ kip*ft}$$

$$\text{Flexural_safety1} = \text{IF}(M_{n1} \geq M_{u1}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

- Pre-composite deflection:

$$\Delta_{nc} = \frac{5 * \frac{w_{D1}}{12} * (L * 12)^4}{384 * E_s * I_x} = 2.59 \text{ in}$$

$$\Delta_{recom} = \frac{L * 12}{360} = 1.50 \text{ in}$$

If pre-composite deflection exceeds the recommended limit. One possible solution is to increase the member size. A second solution is to induce camber into the member. So, the user in this step has to determine a solution in case of exceeding the recommended limit.

$$\text{Camber} = 2.00 \text{ in}$$

$$\text{deflection_check} = \text{IF}((\Delta_{nc} - \text{Camber}) < \Delta_{recom}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Design for Composite Condition

- Required Flexural Strength:

$$w_{D2} = 0.001 * ((w_s + w_{sd}) * a + w_{sec}) = 0.90 \text{ kip/ft}$$

$$w_{L2} = 0.001 * (w_{LL} * a) = 1.00 \text{ kip/ft}$$

From Chapter 2 of ASCE/SEI 7, the required flexural strength is:

$$w_{u2} = 1.2 * w_{D2} + 1.6 * w_{L2} = 2.68 \text{ kip/ft}$$

$$M_{u2} = \frac{w_{u2} * L^2}{8} = 678 \text{ kip*ft}$$



Determine The Effective Slab Width, b_e

The effective width of the concrete slab is the sum of the effective widths to each side of the beam centerline as determined by the minimum value of the three widths set forth in AISC Specification Section I3.1a:

$$b_{e1} = \frac{L}{8} * 2 = 11.25 \text{ ft}$$

$$b_{e2} = \frac{a}{2} * 2 = 10.00 \text{ ft}$$

$$b_e = \text{MIN}(b_{e1}; b_{e2}) = 10.00 \text{ ft}$$

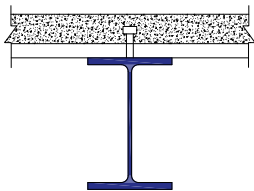
Available Flexural Strength

According to AISC Specification Section I3.2a, the nominal flexural strength shall be determined from the plastic stress distribution on the composite section when $h / t_w \leq \sqrt{(3.76 E / F_y)}$

$$\lambda_w = \frac{d}{t_w} = 54.74$$

$$\text{Web_Class} = \text{IF}(\lambda_w \leq 3.76 * \sqrt{(E_s / F_y)}; \text{"Compact"}; \text{"Non-Compact"}) = \text{Compact}$$

According to AISC Specification Commentary Section I3.2a, the number and strength of steel headed stud anchors will govern the compressive force, C, for a partially composite beam. The composite percentage is based on the minimum of the limit states of concrete crushing and steel yielding as follows:



- Concrete crushing:

A_c = Area of concrete slab within effective width. Assume that the deck profile is 50% void and 50% concrete fill.

$$A_c = (b_e * 12) * (t_s - h_r) + 0.5 * (b_e * 12 * h_r) = 720.00 \text{ in}^2$$

$$C_c = 0.85 * f'_c * A_c = 2448 \text{ kips}$$

- Steel yielding:

$$C_s = A_s * F_y = 735 \text{ kips}$$

- Shear transfer:

60% is used as a trial percentage of composite action as follows:

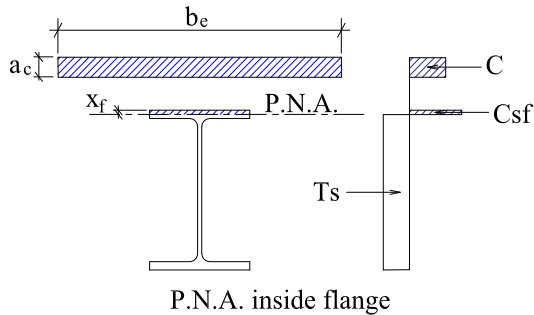
$$C_1 = \Sigma Q_n$$

$$C_1 = 0.6 * \text{MIN}(C_c; C_s) = 441 \text{ kips}$$



Location of The Plastic Neutral Axis

The plastic neutral axis (PNA) is located by determining the axis above and below which the sum of horizontal forces is equal. This concept assumes the trial PNA location is within the top flange of the beam.



$$\Sigma F_{\text{above PNA}} = \Sigma F_{\text{below PNA}}$$

$$C_1 + C_{sf1} = T_{s1} * F_y$$

$$C_{sf1} = x_{f1} * b_f * F_y$$

$$T_{s1} = (A_s - x_{f1} * b_f) * F_y$$

$$x_{f1} = \frac{A_s * F_y - C_1}{2 * b_f * F_y} = 0.45 \text{ in}$$

$$x_f = \text{IF}(x_{f1} \leq t_f; x_{f1}; t_f) = 0.45 \text{ in}$$

$$C_{sf} = x_f * b_f * F_y = 147 \text{ kips}$$

$$T_s = (A_s - x_f * b_f) * F_y = 588 \text{ kips}$$

$$C = T_s - C_{sf} = 441 \text{ kips}$$

Check the percentage of partial composite action:

$$\alpha = C / \text{MIN}(C_c; C_s) = 0.60$$

$$\text{Check_case} = \text{IF}(\alpha < 0.50; \text{"Conservative"}; \text{"o.k."}) = \text{o.k.}$$

Determine the nominal moment resistance of the composite section following the procedure in Specification Commentary Section I3.2a: (calculating the sum. of moments about the P.N.A.)

$$M_2 = \Sigma F * Y$$

$$a_c = \frac{C}{0.85 * f'_c * b_e * 12} = 1.08 \text{ in}$$

$$M_{n2} = 1/12 * (C * (t_s + x_f - a_c/2) + C_{sf} * (x_f/2) + T_s * (d/2 - x_f)) = 763 \text{ kip*ft}$$

$$\text{Flexural_safety2} = \text{IF}(M_{n2} \geq M_{u2}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



Composite deflection: (AISC specs. I3.1 and Eqn. C-13-1)

$$Y_{ENA} = \frac{(A_s * d/2 + (C/F_y) * (d + (t_s - a_c/2)))}{(A_s + C/F_y)} = 16.91 \text{ in}$$

$$I_{Lb} = I_x + A_s * (Y_{ENA} - d/2)^2 + (C/F_y) * (d + (t_s - a_c) - Y_{ENA})^2 = 2545 \text{ in}^3$$

$$\Delta_c = \frac{5 * \frac{W_{L2}}{12} * (L * 12)^4}{384 * E_s * I_{Lb}} = 1.25 \text{ in}$$

$$\Delta_{recom} = \frac{L * 12}{360} = 1.50 \text{ in}$$

$$\text{Deflection_check2} = \text{IF}(\Delta_c < \Delta_{recom}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Summary

Pre-composite condition:

$$M_{u1} = \frac{W_{u1} * L^2}{8} = 344 \text{ kip*ft}$$

$$M_{n1} = \Phi_b * M_p = 412 \text{ kip*ft}$$

$$\text{Flexural_safety1} = \text{IF}(M_{n1} \geq M_{u1}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

$$\Delta_{nc} = \frac{5 * \frac{W_{D1}}{12} * (L * 12)^4}{384 * E_s * I_x} = 2.59 \text{ in}$$

$$\Delta_{recom} = \frac{L * 12}{360} = 1.50 \text{ in}$$

$$\text{Deflection_check} = \text{IF}((\Delta_{nc} - \text{Camber}) < \Delta_{recom}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Composite condition:

$$M_{u2} = \frac{W_{u2} * L^2}{8} = 678 \text{ kip*ft}$$

$$M_{n2} = 1/12 * (C * (t_s + x_f - a_c/2) + C_{sf} * (x_f/2) + T_s * (d/2 - x_f)) = 763 \text{ kip*ft}$$

$$\text{Flexural_safety2} = \text{IF}(M_{n2} \geq M_{u2}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

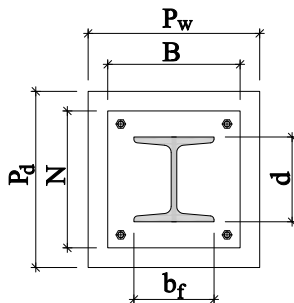
$$\Delta_{nc} = \frac{5 * \frac{W_{D1}}{12} * (L * 12)^4}{384 * E_s * I_x} = 2.59 \text{ in}$$

$$\text{Deflection_check} = \text{IF}((\Delta_{nc} - \text{Camber}) < \Delta_{recom}; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$



Chapter 4: Connection Design

Design of Base Plate Bearing on Concrete Subjected to Concentric Loading



Loads

Dead Load, P_D =		115.0 kips
Live Load, P_L =		345.0 kips

Material Properties

Grade:	SEL("Material/ASTM"; NAME;)	=	A36
Yield stress, f_{yp} =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	36 ksi

Column and Pedestal Data

Concrete strength for pedestal (f'_c):

f'_c =			3 ksi
Sec.:	SEL("AISC/W"; NAME;)	=	W12X96
Pedestal depth, P_d =			24 in
Pedestal width, P_w =			24 in
Depth of column, d =	TAB("AISC/W"; d ; NAME=Sec.)	=	12.7 in
Flange of column, b_f =	TAB("AISC/W"; b_f ; NAME=Sec.)	=	12.2 in

The Required Strength

(Chapter 2 of ASCE/SEI 7)

P_u =	$1.2 \cdot P_D + 1.6 \cdot P_L$	=	690 kips
---------	---------------------------------	---	----------

Preliminary Base Plate Dimensions

Φ_c =			0.65
A_{1req} =	$\frac{P_u}{\Phi_c \cdot 0.85 \cdot f'_c}$	=	416 in ²
$N1$ =	$d + 2 \cdot 3$	=	18.7 in
N =	$MAX(N1; \sqrt{A_{1req}} + 0.5 \cdot (0.95 \cdot d - 0.8 \cdot b_f))$	=	22 in



Chapter 4: Connection Design

Base Plate Subjected to Concentric Loading

AISC

Page: 160

$$B1 = b_f + 2 \cdot 3 = 18.2 \text{ in}$$

$$B = \text{IF}((d - b_f) < 1; \text{MAX}(B1; A_{1\text{req}}/N; N); \text{MAX}(B1; A_{1\text{req}}/N)) = 22 \text{ in}$$

Concrete Bearing Strength

$$\text{Pedestal area, } A_2 = P_d \cdot P_w = 576 \text{ in}^2$$

$$\text{Base plate area, } A_1 = N \cdot B = 484 \text{ in}^2$$

$$\text{Check plate area} = \text{IF}(A_1 > A_{1\text{req}}; \text{"o.k."}; \text{"Unsafe"}) = \text{o.k.}$$

$$P_b = \text{MIN}(0.85 \cdot f_c \cdot A_1 \cdot \sqrt{A_2/A_1}; 1.7 \cdot f_c \cdot A_1) = 1346 \text{ kips}$$

Concrete bearing strength ($\Phi_c P_p$):

$$\Phi_c P_p = \Phi_c \cdot P_b = 875 \text{ kips}$$

$$\text{Check safety, check} = \text{IF}(\Phi_c P_p > P_u; \text{"o.k."}; \text{"Unsafe"}) = \text{o.k.}$$

Base Plate Thickness

$$m = \frac{N - 0.95 \cdot d}{2} = 4.97 \text{ in}$$

$$n = \frac{B - 0.8 \cdot b_f}{2} = 6.12 \text{ in}$$

$$n' = \frac{\sqrt{d \cdot b_f}}{4} = 3.11 \text{ in}$$

$$X = \left(4 \cdot d \cdot \frac{b_f}{(d + b_f)^2} \right) \cdot \left(\frac{P_u}{\Phi_c \cdot P_b} \right) = 0.79$$

$$\lambda = \text{MIN}(2 \cdot \sqrt{X} / (1 + \sqrt{1 - X}); 1.00) = 1.00$$

$$l = \text{MAX}(m; n; \lambda \cdot n') = 6.12 \text{ in}$$

$$f_{pu} = \frac{P_u}{N \cdot B} = 1.43 \text{ ksi}$$

$$t_{\text{min}} = l \cdot \sqrt{\frac{2 \cdot f_{pu}}{0.9 \cdot f_{yp}}} = 1.82 \text{ in}$$

$$t = \text{TAB}(\text{"Material/plate_th"}; t_{fr}; t_{in} > t_{\text{min}}) = 2.00 \text{ in}$$

Summary: Use Plate with The Following Dimensions

$$\text{Plate length} = N = 22 \text{ in}$$

$$\text{Plate width} = B = 22 \text{ in}$$

$$\text{Plate thickness} = t = 2.00 \text{ in}$$



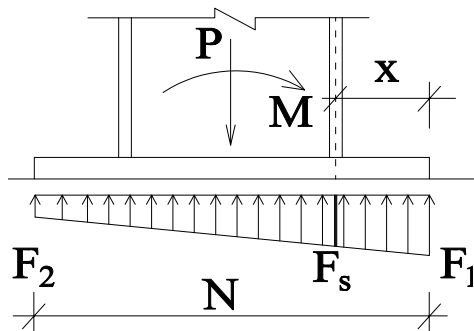
Chapter 4: Connection Design

Base Plate Subjected to Small Eccentricity

AISC

Page: 161

Design of Base Plate Bearing on Concrete Subjected to Small Eccentricity, $e \leq N/6$



Loads

Dead Load, P_D =	50 kips
Live Load, P_L =	90 kips
Moment from D.L., M_D =	100 kip*in
Moment from L.L., M_L =	180 kip*in

Base Plate Material Properties

Grade:	SEL("Material/ASTM"; NAME;)	=	A36
Yield stress, f_{yp} =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	36 ksi

Column, Base Plate and Pedestal Dimensions

Concrete strength for pedestal (f'_c):

f'_c =		=	3 ksi
Sec.:	SEL("AISC/W"; NAME;)	=	W10X112
Pedestal depth, P_d =		=	17 in
Pedestal width, P_w =		=	14 in
Base plate depth, N =		=	17 in
Base plate width, B =		=	14 in
Depth of column, d =	TAB("AISC/W"; d ; NAME=Sec.)	=	11.4 in
Flange of column, b_f =	TAB("AISC/W"; b_f ; NAME=Sec.)	=	10.4 in

Check Eccentricity Size

M_t =	$M_D + M_L$	=	280 kip*in
P_t =	$P_D + P_L$	=	140 kips
e =	M_t / P_t	=	2.00 in
Check_e=	IF($e \leq N/6$; "O.K."; "not O.K.")	=	O.K.

(Note that: if this check was not O.K., this template will give a wrong solution)



Chapter 4: Connection Design

Base Plate Subjected to Small Eccentricity

AISC

Page: 162

The Ultimate Load and Moment

(Chapter 2 of ASCE/SEI 7)

$$P_u = 1.2 \cdot P_D + 1.6 \cdot P_L = 204 \text{ kips}$$

$$M_u = 1.2 \cdot M_D + 1.6 \cdot M_L = 408 \text{ kip}\cdot\text{in}$$

The Maximum Bearing Stress, F_b

$$\Phi_c = 0.60$$

$$A_1 = N \cdot B = 238.00 \text{ in}^2$$

$$A_2 = P_d \cdot P_w = 238.00 \text{ in}^2$$

$$F_{b1} = 0.85 \cdot \Phi_c \cdot f_c \cdot \sqrt{A_2/A_1} = 1.53 \text{ ksi}$$

$$F_{b2} = 1.7 \cdot f_c = 5.10 \text{ ksi}$$

$$F_b = \text{MIN}(F_{b1}; F_{b2}) = 1.53 \text{ ksi}$$

$$F_1 = \text{IF}(\text{Check_e} = \text{"O.K."}; \frac{P_u}{A_1} + \frac{M_u \cdot N/2}{(B \cdot N^3)/12}; \text{" "}) = 1.46 \text{ ksi}$$

$$F_2 = \frac{P_u}{A_1} - \frac{M_u \cdot \frac{N}{2}}{B \cdot N^3 \cdot 12} = 0.25 \text{ ksi}$$

$$\text{Check_F} = \text{IF}(F_1 < F_b; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Base Plate Thickness:

The critical section is at distance (x) from the plate edge, where:

$$x = \frac{N - 0.95 \cdot d}{2} = 3.09 \text{ in}$$

The distance from the base center to this section (x_1) and the stress at this section (F_s) can be calculated as:

$$x_1 = \frac{N}{2} - x = 5.41 \text{ in}$$

$$F_s = \text{IF}(\text{Check_e} = \text{"O.K."}; \frac{P_u}{A_1} + \frac{M_u \cdot x_1}{(B \cdot N^3)/12}; \text{" "}) = 1.24 \text{ ksi}$$



Chapter 4: Connection Design

Base Plate Subjected to Small Eccentricity

AISC

Page: 163

The factored moment for a 1-in strip at this section (M_s) can be calculated as follows:

$$M_s = \frac{F_s * x^2}{2} + (F_1 - F_s) * \frac{x^2 * 0.67}{2} = 6.62 \text{ kip*in}$$

$$t_{p,\min} = \sqrt{\frac{4 * M_s}{0.9 * f_{yp}}} = 0.90 \text{ in}$$

Summary: Use Plate with The Following Minimum Dimensions

Plate length=	N	=	17 in
Plate width=	B	=	14 in
Plate thickness=	$t_{p,\min}$	=	0.90 in



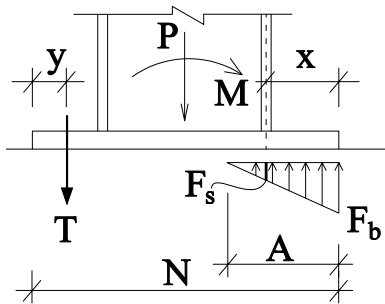
Chapter 4: Connection Design

Base Plate Subjected to Large Eccentricity

AISC

Page: 164

Design of Base Plate Bearing on Concrete Subjected to Large Eccentricity, $e > N/2$



Loads

Dead Load, P_D =		21 kips
Live Load, P_L =		39 kips
Moment from D.L., M_D =		171 kip*in
Moment from L.L., M_L =		309 kip*in

Base Plate Material Properties

Grade:	SEL("Material/ASTM"; NAME;)	=	A36
Yield stress, f_{yp} =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	36 ksi

Column, Base Plate and Pedestal Dimensions

Concrete strength for pedestal (f'_c):

f'_c =		3 ksi
Sec.:	SEL("AISC/W"; NAME;)	= W8X35
Pedestal depth, P_d =		28 in
Pedestal width, P_w =		28 in
Base plate depth, N =		14 in
Base plate width, B =		14 in
Distance to bolt, y =		1.50 in
Depth of column, d =	TAB("AISC/W"; d ; NAME=Sec.)	= 8.1 in
Flange of column, b_f =	TAB("AISC/W"; b_f ; NAME=Sec.)	= 8.0 in

Check Eccentricity Size

M_t =	$M_D + M_L$	=	480 kip*in
P_t =	$P_D + P_L$	=	60 kips
e =	M_t / P_t	=	8.00 in
Check_e=	IF($e > N/2$; "O.K."; "not O.K.")	=	O.K.

(Note that: if this check was not O.K., this template will give a wrong solution)



Chapter 4: Connection Design

Base Plate Subjected to Large Eccentricity

AISC

Page: 165

The Ultimate Load and Moment

(Chapter 2 of ASCE/SEI 7)

$$P_u = 1.2 * P_D + 1.6 * P_L = 88 \text{ kips}$$

$$M_u = 1.2 * M_D + 1.6 * M_L = 700 \text{ kip*in}$$

The Maximum Bearing Stress, F_b

$$\Phi_c = 0.60$$

$$A_1 = N * B = 196.00 \text{ in}^2$$

$$A_2 = P_d * P_w = 784.00 \text{ in}^2$$

$$F_{b1} = 0.85 * \Phi_c * f_c * \sqrt{A_2 / A_1} = 3.06 \text{ ksi}$$

$$F_{b2} = 1.7 * f_c = 5.10 \text{ ksi}$$

$$F_b = \text{MIN}(F_{b1}; F_{b2}) = 3.06 \text{ ksi}$$

$$N' = N - y = 12.50 \text{ in}$$

$$F' = \frac{F_b * B * N'}{2} = 267.8 \text{ ksi}$$

Distance from the base to bolt centers (A') is:

$$A' = \frac{N}{2} - y = 5.50 \text{ in}$$

$$M_1 = P_u * A' + M_u = 1184 \text{ kip*in}$$

$$A_1 = \frac{F' + \sqrt{(F')^2 - 4 * \frac{F_b * B}{6} * M_1}}{\frac{F_b * B}{3}} = 32.4 \text{ in}$$

$$A_2 = \frac{F' - \sqrt{(F')^2 - 4 * \frac{F_b * B}{6} * M_1}}{\frac{F_b * B}{3}} = 5.1 \text{ in}$$

$$A = \text{MIN}(A_1; A_2) = 5.1 \text{ in}$$

$$\text{Check_A} = \text{IF}(A < N'; \text{"O.K."}; \text{"not O.K."}) = \text{O.K.}$$

(If this check was not O.K., increase plate dimensions to find a solution or check inputs)

Tension in Bolts

$$T = \frac{F_b * A * B}{2} - P_u = 21.2 \text{ kips}$$



Base Plate Thickness

The critical section is at distance (x) from the plate edge, where:

$$x = \frac{N - 0.95 \cdot d}{2} = 3.15 \text{ in}$$

The distance from the zero stress point to this section (x_1) and the stress at this section (F_s) can be calculated as:

$$x_1 = A - x = 1.95 \text{ in}$$

$$F_s = x_1 / A \cdot F_b = 1.17 \text{ ksi}$$

The factored moment for a 1-in strip at this section (M_{s1}) can be determined from the bearing stress distribution as follows:

$$M_{s1} = \frac{F_s \cdot x^2}{2} + (F_b - F_s) \cdot \frac{x^2 \cdot 0.67}{2} = 12.09 \text{ kip}\cdot\text{in}$$

Also, The moment based on the critical section on the anchor bolt side is determined as follows (it is assumed that the critical plate width is based on the load spreading out at 45 degrees:

$$M_{s2} = T/2 \cdot (x-y) / (2 \cdot (x-y)) = 5.30 \text{ kip}\cdot\text{in}$$

So, the critical moment is the maximum from M_{s1} and M_{s2} as follows:

$$M_s = \text{MAX}(M_{s1}; M_{s2}) = 12.09 \text{ kip}\cdot\text{in}$$

$$t_{p,\min} = \sqrt{\frac{4 \cdot M_s}{0.9 \cdot f_{yp}}} = 1.22 \text{ in}$$

Summary: Use Plate with The following Minimum Dimensions

$$\text{Plate length} = N = 14 \text{ in}$$

$$\text{Plate width} = B = 14 \text{ in}$$

$$\text{Plate thickness} = t_{p,\min} = 1.22 \text{ in}$$



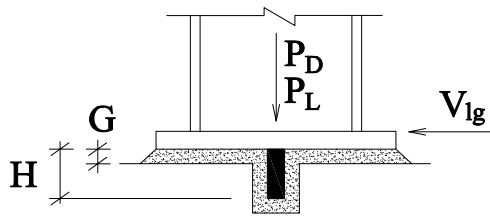
Chapter 4: Connection Design

Shear Lug

AISC

Page: 167

Design of a Shear Lug for Base Plates Subjected to Axial and Shear Loads



Loads

Dead Load, P_D =	120 kips
Live Load, P_L =	150 kips
Shear Load, V_w =	55 kips

Base Plate Material Properties

Grade:	SEL("Material/ASTM"; NAME;)	=	A36
Yield stress, f_{yp} =	TAB("Material/ASTM"; F_y ; NAME=Grade)	=	36 ksi

Column, Base Plate and Pedestal Dimensions

Concrete strength for pedestal (f'_c):

f'_c =	3 ksi
Base plate depth, N =	14 in
Base plate width, B =	14 in
The coefficient of friction, μ =	0.55
Shear lug width, W =	8 in
Grout depth, G =	1.0 in

The Portion of The Shear which can be Transferred by Friction Equal to μ :

$$V_{lgu} = 1.3 * V_w - \mu * (0.9 * P_D) = 12.1 \text{ kips}$$

The Required Bearing Area

$$\Phi_c = 0.60$$

$$A_{lgu} = \frac{V_{lgu}}{0.85 * \Phi_c * f'_c} = 7.9 \text{ in}^2$$

The Height of The Bearing Portion

$$H = \frac{A_{lgu}}{W} = 0.99 \text{ in}$$



Chapter 4: Connection Design

Shear Lug

AISC

Page: 168

Base Plate Thickness

$$M_{Igu} = \frac{V_{Igu}}{W} * \frac{H+G}{2} = 1.5 \text{ kip*in}$$

$$t_{lg} = \sqrt{\frac{4 * M_{Igu}}{0.9 * f_{yp}}} = 0.43 \text{ in}$$

Summary: Use Shear Lug with the Following Minimum Dimensions

$$\text{Depth} = H+G = 2 \text{ in}$$

$$\text{Width} = W = 8 \text{ in}$$

$$\text{Thickness} = t_{lg} = 0.43 \text{ in}$$



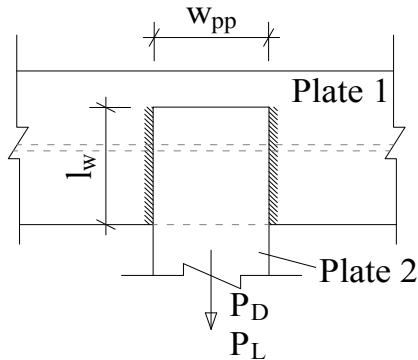
Chapter 4: Connection Design

Fillet Weld Subjected to Longitudinal Shear Force

AISC

Page: 169

Design of Fillet Weld Subjected to Longitudinal Shear Force



Details of The Connected Plates

Grade:	SEL("Material/ASTM"; NAME;)	=	A992
F_y =	TAB("Material/ASTM"; F_y ;NAME=Grade)	=	50 ksi
Thickness of the first plate, t_{p1} =			0.2500 in
Thickness of the second plate, t_{p2} =			0.3750 in
Width of the perpendicular part, w_{pp} =			18.0 in

Loads

Force:	SEL ("AISC/force"; type;)	=	Tension
Dead load, P_D =			33.0 kips
Live load, P_L =			100.0 kips
From Chapter 2 of ASCE/SEI 7, the required strength is:			
P_u =	$1.2 \cdot P_D + 1.6 \cdot P_L$	=	199.6 kips

Preliminary Welding Details

Electrode classification number, F_{EXX} =			70 ksi
Length of weld on each side, l_w =			27.00 in
Thickness of weld, t_w =			0.1875 in



Chapter 4: Connection Design

Fillet Weld Subjected to Longitudinal Shear Force

AISC

Page: 170

Design of Weld

- Check the maximum and minimum Weld Size (AISC Specification Section J2.2b)

Minimum thickness of the connected parts (t_{pmin}):

$$t_{pmin} = \text{MIN}(t_{p1}; t_{p2}) = 0.2500 \text{ in}$$

$$t_{w,max} = \text{IF}(t_{pmin} < 1/4; t_{pmin}; (t_{pmin} - 1/16)) = 0.1875 \text{ in}$$

$$t_{w,min1} = \text{IF}(t_{pmin} \leq 1/4; 1/8; \text{IF}((t_{pmin} > 1/4 \text{ AND } t_{pmin} \leq 1/2); 3/16; 0)) = 0.1250 \text{ in}$$

$$t_{w,min2} = \text{IF}((t_{pmin} > 1/2 \text{ AND } t_{pmin} \leq 3/4); 1/4; 5/16) = 0.3125 \text{ in}$$

$$t_{w,min} = \text{IF}(t_{w,min1} = 0; t_{w,min2}; \text{MIN}(t_{w,min1}; t_{w,min2})) = 0.1250 \text{ in}$$

$$\text{Check_1} = \text{IF}((t_w \geq t_{w,min} \text{ AND } t_w \leq t_{w,max}); \text{"O.K."}; \text{"Increase } t_w\text{"}) = \text{O.K.}$$

- Minimum required length:

$$l_{w,min} = \frac{P_u}{0.60 * F_{EXX} * t_w / \sqrt{2} * 0.75 * 2} = 23.9 \text{ in}$$

- Check length for perpendicular plate width:

$$\text{Check1} = \text{IF}(F = \text{"C"}; \text{"O.K."}; \text{IF}(l_{w,min} \geq w_{pp}; \text{"O.K."}; \text{"increase } l_w\text{"})) = \text{O.K.}$$

- Calculate the effective weld length:

$$\lambda_w = l_w / t_w = 144.0 \text{ in}$$

$$\beta_w = \text{MIN}(1.2 - 0.002 * \lambda_w; 1) = 0.91 \text{ in}$$

$$l_{w,eff} = \beta_w * l_w = 24.57 \text{ in}$$

- Recheck the weld at its reduced strength:

$$\Phi R_n = 0.75 * 2 * l_{w,eff} * t_w / \sqrt{2} * 0.6 * F_{EXX} = 205.2 \text{ kips}$$

$$\text{Check_2} = \text{IF}(\Phi R_n > P_u; \text{"Safe"}; \text{"Unsafe"}) = \text{Safe}$$

Design Summary

$$\text{Electrode} = F_{EXX} = 70.0 \text{ ksi}$$

$$\text{Size} = t_w = 0.1875 \text{ in}$$

$$\text{length} = l_w = 27.00 \text{ in}$$

$$P_u = 1.2 * P_D + 1.6 * P_L = 199.6 \text{ kips}$$

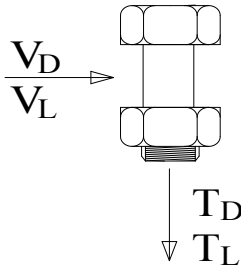
$$\Phi R_n = 0.75 * 2 * l_{w,eff} * t_w / \sqrt{2} * 0.6 * F_{EXX} = 205.2 \text{ kips}$$

$$\text{Check_1} = \text{IF}((t_w \geq t_{w,min} \text{ AND } t_w \leq t_{w,max}); \text{"O.K."}; \text{"Increase } t_w\text{"}) = \text{O.K.}$$

$$\text{Check_2} = \text{IF}(\Phi R_n > P_u; \text{"Safe"}; \text{"Increase weld size/length"}) = \text{Safe}$$



Design of Bolts in Bearing Type Connection Subjected to Combined Tension and Shear Forces



Details of Bolt

Grade:	SEL("AISC/ASTM_bolts"; Name;)	=	A325
F_u =	TAB("AISC/ASTM_bolts"; F_u ; Name=Grade)	=	120 ksi
Bolt:	SEL("AISC/bolt"; Size;)	=	d3/4
Bolt diameter, d_b =	TAB("AISC/bolt"; dia; Size=Bolt)	=	0.7500 in
Area of bolt, A_b =	TAB("AISC/bolt"; Area; Size=Bolt)	=	0.4418 in ⁴

Loads

Dead:			
Tension force, T_D =			3.50 kips
Shear force, V_D =			1.3 kips
Live:			
Tension force, T_L =			12.0 kips
Shear force, V_L =			4.0 kips
From Chapter 2 of ASCE/SEI 7, the required strength is:			
T_u =	$1.2 \cdot T_D + 1.6 \cdot T_L$	=	23.4 kips
V_u =	$1.2 \cdot V_D + 1.6 \cdot V_L$	=	8.0 kips

Check for Shear

Φ =			0.75
From AISC Specification Table J3.2,			
The available shear strength (F_{nv}):			
F_{nv} =	$0.40 \cdot F_u$	=	48.0 ksi
The available shear stress (f_{rv}):			
f_{rv} =	V_u / A_b	=	18.1 ksi
Check_Shear=	IF($\Phi \cdot F_{nv} \geq f_{rv}$; "Safe"; "Increase d_b ")	=	Safe



Check for Tension Accompanied by Shear

From AISC Specification Table J3.2,

The available tensile strength (F_{nt}):

$$F_{nt} = 0.75 * F_u = 90.0 \text{ ksi}$$

The available tensile strength of a bolt subject to combined tension and shear is as follows, from AISC Spec. Eqn. J3.3a,

$$F_{nt}' = 1.30 * F_{nt} - \frac{F_{nt}}{\phi * F_{nv}} * f_{rv} = 71.8 \text{ ksi}$$

The available tension force (R_n):

$$R_n = A_b * \text{MIN}(F_{nt}', F_{nt}) = 31.7 \text{ kips}$$

$$\text{Check_Tension} = \text{IF}(\phi * R_n \geq T_u, \text{"Safe"}, \text{"Increase } d_b \text{"}) = \text{Safe}$$

Design Summary

$$\text{Size} = d_b = 0.7500 \text{ in}$$

$$F_u = \text{TAB}(\text{"AISC/ASTM_bolts"}, F_u, \text{Name=Grade}) = 120 \text{ ksi}$$

$$f_{rv} = V_u / A_b = 18.1 \text{ ksi}$$

$$F_{nv} = 0.40 * F_u = 48.0 \text{ ksi}$$

$$\text{Check_Shear} = \text{IF}(\phi * F_{nv} \geq f_{rv}, \text{"Safe"}, \text{"Increase } d_b \text{"}) = \text{Safe}$$

$$T_u = 1.2 * T_D + 1.6 * T_L = 23.4 \text{ kips}$$

$$R_n = A_b * \text{MIN}(F_{nt}', F_{nt}) = 31.7 \text{ kips}$$

$$\text{Check_Tension} = \text{IF}(\phi * R_n \geq T_u, \text{"Safe"}, \text{"Increase } d_b \text{"}) = \text{Safe}$$



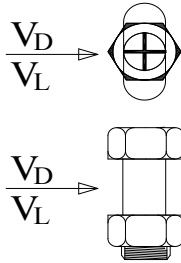
Chapter 4: Connection Design

Slip Critical Connection with Short-Slotted Holes

AISC

Page: 173

Design of Slip Critical Connection with Short-Slotted Holes Subjected to Shear Force



Details of Bolt (short slots transverse to the load)

Grade:	SEL("AISC/ASTM_bolts"; Name;)	=	A325
F_u =	TAB("AISC/ASTM_bolts"; F_u ; Name=Grade)	=	120 ksi
Bolt:	SEL("AISC/J3.1"; Size;)	=	d3/4 A325
Bolt diameter, d_b =	TAB("AISC/J3.1"; dia; Size=Bolt)	=	0.7500 in
Area of bolt, A_b =	TAB("AISC/J3.1"; Area; Size=Bolt)	=	0.4418 in ⁴
Class:	SEL("AISC/Class"; class;)	=	Class_A
T_b =	TAB("AISC/J3.1"; T_b ; Size=Bolt)	=	28 kips
μ =	TAB("AISC/Class2"; mio; cat=Class_sym)	=	0.35
(T_b is the minimum bolt pretension and μ is the mean slip coefficient)			
D_u =			1.13
Number of slip planes, n_s =			2
hole factor, h_f =			1.00

Loads

Shear force due to dead load, V_D =			3.00 kips
Shear force due to live load, V_L =			7.00 kips
From Chapter 2 of ASCE/SEI 7, the required strength is:			
V_u =	$1.2*V_D+1.6*V_L$	=	14.8 kips

Check for Slip Resistance

Φ =			1.00
The design slip resistance, ΦR_n =	$\Phi * \mu * D_u * h_f * T_b * n_s$	=	22.15 kips
Check_slip=	IF($\Phi R_n \geq V_u$; "Safe"; "Unsafe")	=	Safe



Chapter 4: Connection Design

Slip Critical Connection with Short-Slotted Holes

AISC

Page: 174

Check The Limit State of Bolt Shear

$$\Phi_2 = 0.75$$

From AISC Specification Table J3.2,

$$\text{The available shear strength, } F_{nv} = 0.40 * F_u = 48.0 \text{ ksi}$$

$$\text{The actual shear stress, } f_{rv} = V_u / (A_b) = 33.5 \text{ ksi}$$

$$\text{Check_Shear} = \text{IF}(\Phi_2 * F_{nv} \geq f_{rv}, \text{"Safe"}, \text{"Increase } d_b\text{"}) = \text{Safe}$$

Design Summary

$$\text{Size} = d_b = 0.7500 \text{ in}$$

$$F_u = \text{TAB}(\text{"AISC/ASTM_bolts"}, F_u, \text{Name=Grade}) = 120 \text{ ksi}$$

$$V_u = 1.2 * V_D + 1.6 * V_L = 14.8 \text{ kips}$$

$$\text{The design slip resistance, } \Phi R_n = \Phi * \mu * D_u * h_f * T_b * n_s = 22.15 \text{ kips}$$

$$\text{Check_slip} = \text{IF}(\Phi R_n \geq V_u, \text{"Safe"}, \text{"Unsafe"}) = \text{Safe}$$

$$\text{The available shear stress, } f_{rv} = V_u / A_b = 33.5 \text{ ksi}$$

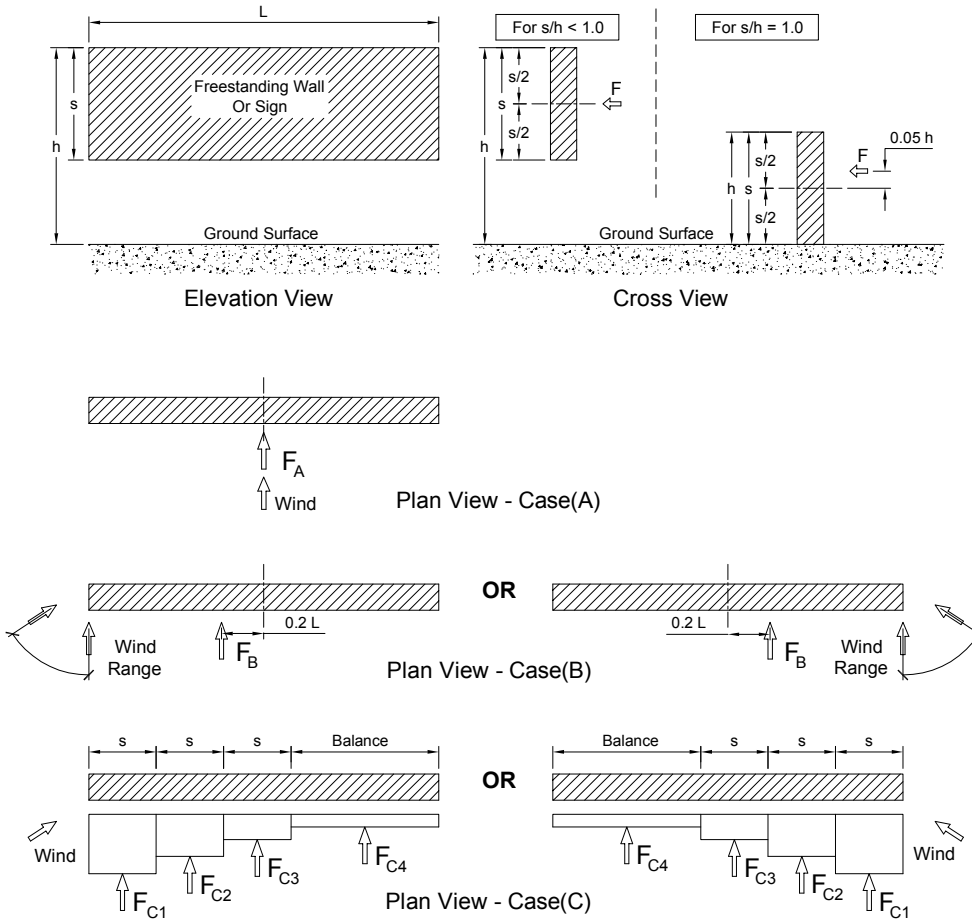
$$\text{The available shear strength, } F_{nv} = 0.40 * F_u = 48.00 \text{ ksi}$$

$$\text{Check_Shear} = \text{IF}(\Phi_2 * F_{nv} \geq f_{rv}, \text{"Safe"}, \text{"Increase } d_b\text{"}) = \text{Safe}$$



Chapter 5: Design Loads

Calculation of Wind load for Solid Freestanding Walls & Signs as per ASCE/SEI 7-10 Chapters 26 & 29



Dimensions of Solid Freestanding Walls or Solid Freestanding Signs

Horizontal Dimension of Wall or Sign, L =	75.0 ft
Mean top height of Wall or Sign, h =	10.0 ft
Vertical Dimension of Wall or Sign, s =	10.0 ft

Wind load Parameters

Basic wind speed, V =	105.00 mph
Wind Directionality Factor (According to Table 26.6-1 of ASCE/SEI 7),	
K_d =	0.85
The Exposure Category (According to Cl. 26.7.3 of ASCE/SEI 7):	
Category: SEL("ASCE/Exp"; Category;)	= B
Gust-Effect Factor (According to Cl. 26.9.1 of ASCE/SEI 7), G =	0.85
Topographic Factor (According to Cl. 26.8.2 of ASCE/SEI 7), K_{zt} =	1.00



Velocity Pressure

According to (Table 26.9-1 of ASCE/SEI 7),

$$\alpha = \text{TAB}(\text{"ASCE/Exp"; Alpha; Category=Category}) = 7.00$$

According to (Table 26.9-1 of ASCE/SEI 7),

$$z_g = \text{TAB}(\text{"ASCE/Exp"; } z_g; \text{Category=Category}) = 1200.00$$

The Velocity Pressure Exposure Coefficient (According to Table 29.3-1 of ASCE/SEI 7):

$$K_h = \text{IF}(h < 15; 2.01 * (15/z_g)^{(2/\alpha)}; 2.01 * (h/z_g)^{(2/\alpha)}) = 0.57$$

Velocity Pressure (According to Cl. 29.3.2 of ASCE/SEI 7),

$$q_h = 0.00256 * K_h * K_{zt} * K_d * V^2 = 13.67 \text{ psf}$$

$$\text{The gross area of the solid freestanding wall or sign, } A_s = L * s = 750 \text{ ft}^2$$

$$\text{Ratio of solid area to gross area, } \epsilon = 1.00$$

$$\text{Reduction Factor for Openings, } RF = 1 - (1 - \epsilon)^{1.5} = 1.00$$

Wind Forces - Case A

$$\text{Force Coefficient (According to Fig. 29.4-1 of ASCE/SEI 7), } C_{fA} = 1.33$$

Design wind force (According to Cl. 29.4.1 of ASCE/SEI 7),

$$F_A = q_h * G * C_{fA} * A_s * RF / 1000 = 11.6 \text{ kips}$$

Wind Forces - Case B

$$\text{Force Coefficient (According to Fig. 29.4-1 of ASCE/SEI 7), } C_{fB} = 1.33$$

Design wind force (According to Cl. 29.4.1 of ASCE/SEI 7),

$$F_B = q_h * G * C_{fB} * A_s * RF / 1000 = 11.6 \text{ kips}$$

Wind Forces - Case C

Region-1 from (0 to s or less)

Force Coefficient for Region-1 (According to Fig. 29.4-1 of ASCE/SEI 7),

$$C_{fC1} = 3.48$$

$$\text{Effective Area for Region-1, } A_{sC1} = \text{IF}(L/s > 1; s*s; L*s;) = 100 \text{ ft}^2$$

Design Wind Force for Region-1 (According to Cl. 29.4.1 of ASCE/SEI 7).

$$F_{C1} = RF/1000 * \text{MAX}(16; q_h * G * C_{fC1} * \text{IF}(s/h > 0.8; (1.8-s/h); 1)) * A_{sC1} = 3.2 \text{ kips}$$

$$\text{Region-2 from (s to 2s) Validation: IF}(L/s > 1; \text{"Valid"; "Invalid";}) = \text{Valid}$$

Force Coefficient for Region-2 (According to Fig. 29.4-1 of ASCE/SEI 7),

$$C_{fC2} = 2.28$$

$$\text{Effective Area for Region-2, } A_{sC2} = \text{IF}(L/s > 2; s*s; \text{IF}(L/s < 1; 0; (L-s)*s);) = 100 \text{ ft}^2$$

Design Wind Force for Region-2 (According to Cl. 29.4.1 of ASCE/SEI 7).

$$F_{C2} = RF/1000 * \text{MAX}(16; q_h * G * C_{fC2} * \text{IF}(s/h > 0.8; (1.8-s/h); 1)) * A_{sC2} = 2.1 \text{ kips}$$



Chapter 5: Design Loads

Wind load for Solid Freestanding Walls & Signs

Region-3 from (2s to 3s)	Validation: IF(L/s>2;"Valid";"Invalid";)	=	Valid
Force Coefficient for Region-3 (According to Fig. 29.4-1 of ASCE/SEI 7),			
C_{fC3} =			1.68
Effective Area for Region-3, A_{sC3} = IF(L/s>3;s*s;IF(L/s<2;0;(L-2*s)*s;);)		=	100 ft ²
Design Wind Force for Region-3 (According to Cl. 29.4.1 of ASCE/SEI 7).			
F_{C3} =	RF/1000*MAX(16;q _h *G*C _{fC3} *IF(s/h>0.8;(1.8-s/h);1))*A _{sC3}	=	1.6 kips
Region-4 from (3s to L)	Validation: IF(L/s>3;"Valid";"Invalid";)	=	Valid
Force Coefficient for Region-4 (According to Fig. 29.4-1 of ASCE/SEI 7),			
C_{fC4} =			1.05
Effective Area for Region-4, A_{sC4} = IF(L/s>3;(L-3*s)*s;0;)		=	450 ft ²
Design Wind Force for Region-4 (According to Cl. 29.4.1 of ASCE/SEI 7).			
F_{C4} =	RF/1000*MAX(16;q _h *G*C _{fC4} *IF(s/h>0.8;(1.8-s/h);1))*A _{sC4}	=	7.2 kips

Calculation Summary

F_A =	F_A	=	11.6 kips
F_B =	F_B	=	11.6 kips
F_{C1} =	F_{C1}	=	3.2 kips
F_{C2} =	F_{C2}	=	2.1 kips
F_{C3} =	F_{C3}	=	1.6 kips
F_{C4} =	F_{C4}	=	7.2 kips



Chapter 5: Design Loads

Snow Loads for Flat Roof

ASCE-7

Page: 178

Calculation of Snow Loads for Flat Roof as per ASCE/SEI 7-10 Chapter 7

Parameters of Snow Load

Ground Snow Loads (According to Table 7-1 of ASCE/SEI 7), p_g =		18.00 psf
Snow Density (According to Eq. 7.7-1 of ASCE/SEI 7), γ =	$\text{MIN}(0.13 * p_g + 14; 30)$	= 16.34 lb/ft ³
Terrain Category (According to Table 7-2 of ASCE/SEI 7), TER_CAT=	$\text{SEL}(\text{"ASCE/Ter_Cat"}; \text{ID};)$	= B
Exposure of Roof (According to Table 7-2 of ASCE/SEI 7), EX_RF=	$\text{SEL}(\text{"ASCE/EX_RF"}; \text{ID};)$	= Fully Exposed
Exposure Factor (According to Table 7-2 of ASCE/SEI 7), C_e =		0.90
Thermal Factor (According to Table 7-3 of ASCE/SEI 7), C_t =	$\text{SEL}(\text{"ASCE/Ct"}; \text{ID};)$	= 1.00
Risk Category (According to Table 1.5-1 of ASCE/SEI 7), RI_CAT=	$\text{SEL}(\text{"ASCE/Risk_Cat"}; \text{ID};)$	= II
Importance Factor (According to Table 1.5-2 of ASCE/SEI 7), I_s =	$\text{TAB}(\text{"ASCE/Is"}; I_s; \text{RI_CAT}=\text{RI_CAT};)$	= 1.00

Snow Load for Flat Roof

Min Snow Load (According to Cl. 7.3.4 of ASCE/SEI 7), p_m =	$\text{IF}(p_g > 20; 20 * I_s; p_g * I_s)$	= 18.00 psf
Flat Roof Snow Load (According to Cl. 7.3 of ASCE/SEI 7), p_f =	$0.7 * C_e * C_t * I_s * p_g$	= 11.34 psf

Calculation Summary

Min Snow Load, p_m =	p_m	= 18.00 psf
Flat Roof Snow Load, p_f =	p_f	= 11.34 psf



Chapter 5: Design Loads

Snow Loads for Sloped Roof

ASCE-7

Page: 179

Calculation of Snow Loads for Sloped Roof as per ASCE/SEI 7-10 Chapter 7

Parameters of Snow Load

Ground Snow Loads (According to Table 7-1 of ASCE/SEI 7), p_g =		40.00 pf
Density of Snow (According to Eq. 7.7-1 of ASCE/SEI 7), γ =	$\text{MIN}(0.13 * p_g + 14; 30)$	= 19.20 lb/ft ³
Terrain Category (According to Table 7-2 of ASCE/SEI 7), TER_CAT=	SEL("ASCE/Ter_Cat"; ID;)	= B
Exposure of Roof (According to Table 7-2 of ASCE/SEI 7), EX_RF=	SEL("ASCE/EX_RF"; ID;)	= Fully Exposed
Exposure Factor (According to Table 7-2 of ASCE/SEI 7), C_e =		0.70
Thermal Factor (According to Table 7-3 of ASCE/SEI 7), C_t =	SEL("ASCE/Ct"; ID;)	= 1.10
Risk Category (According to Table 1.5-1 of ASCE/SEI 7), RI_CAT=	SEL("ASCE/Risk_Cat"; ID;)	= II
Importance Factor (According to Table 1.5-2 of ASCE/SEI 7), I_s =	TAB("ASCE/Is"; Is; RI_CAT=RI_CAT;)	= 1.00

Snow Load for Flat Roof

Min Snow Load (According to Cl. 7.3.4 of ASCE/SEI 7), p_m =	$\text{IF}(p_g > 20; 20 * I_s; p_g * I_s)$	= 20.00 psf
Flat Roof Snow Load (According to Cl. 7.3 of ASCE/SEI 7), p_f =	$0.7 * C_e * C_t * I_s * p_g$	= 21.56 psf

Snow Load for Sloped Roof

α =		20.0 °
Thermal Resistance Value R=		30.0 ° Fh ft ² /Btu
Roof Slope Factor (According to Fig. (7-2b) of ASCE/SEL 7, C_s =		1.00
Sloped Roof Snow Load (According to Cl.7.4 of ASCE/SEL 7), p_s =	$p_f * C_s$	= 21.56 in

Calculation Summary

Min Snow Load, p_m =	p_m	= 20.00 psf
Flat Roof Snow Load, p_f =	p_f	= 21.56 psf
Sloped Roof Snow Load, p_s =	p_s	= 21.56 in



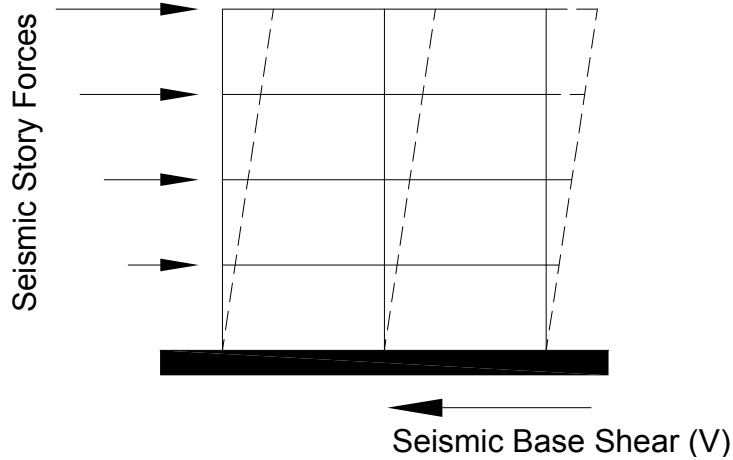
Chapter 5: Design Loads

Seismic Base Shear

ASCE-7

Page: 180

Calculation of Seismic Base Shear as per ASCE/SEI 7-10 Chapter 11



Site Parameters

(According to Cl.11.4.2 of ASCE/SEI 7),

Site Class: SEL("ASCE/Site_Cl"; ID;) = A

Mapped Acceleration Parameters

(According to Cl.11.4.1 of ASCE/SEI 7),

At Short Period, $S_s = 1.50$

At 1 Second Period, $S_1 = 0.50$

Site Coefficient at Short Period, $F_a = 1.00$

Site Coefficient at 1 Second Period, $F_v = 1.30$

Spectral Response Acceleration Parameters

(According to Cl.11.4.3 of ASCE/SEI 7),

Spectral Response Acceleration at Short Period, $S_{MS} = F_a * S_s = 1.50$

Spectral Response Acceleration at 1 Second Period, $S_{M1} = F_v * S_1 = 0.65$

Design Spectral Acceleration Parameters

(According to Cl.11.4.4 of ASCE/SEI 7),

Design Spectral Acceleration Parameter at Short Period, $S_{DS} = 2/3 * S_{MS} = 1.00$

Design Spectral Acceleration Parameter at 1 Second period, $S_{D1} = 2/3 * S_{M1} = 0.43$

Risk Category

Risk Category (According to Table 1.5-1 of ASCE/SEI 7),

RI_CAT= SEL("ASCE/Risk_Cat"; ID;) = I

Importance Factor (According to Table 1.5-12 of ASCE/SEI 7),

$I_e = \text{TAB}(\text{"ASCE/Ie"; Ie; RI_CAT=RI_CAT}) = 1.00$



Chapter 5: Design Loads

Seismic Base Shear

ASCE-7

Page: 181

Fundamental Period:

(According to Cl.12.8.2 of ASCE/SEI 7),

Type of Structure, STR= SEL("ACI/Ct&X";STR;) = All other structural systems

Building Period Parameter, C_t = TAB("_ACI/Ct&X";Ct;STR=STR;) = 0.020

Building Period Parameter, x = TAB("_ACI/Ct&X";X;STR=STR;) = 0.750

Structure Height, h_n = 66.00 ft

Approximate Fundamental Period, T_a = $C_t * h_n^x$ = 0.46 sec

Building fundamental period, T = T_a = 0.46 sec

Long-period transition period, T_L = 2.00

Seismic Response Coefficient

(According to Cl.12.8.1.1 of ASCE/SEI 7)

Response Modification Coefficient (According to Table 12.2-1), R = 3.25

Calculated Seismic Response Coefficient, $C_{s,c}$ = $\frac{S_{DS}}{R/I_e}$ = 0.3077

Maximum Seismic Response Coefficient, $C_{s,max1}$ = $\frac{S_{D1}}{T*(R/I_e)}$ = 0.2876

Maximum Seismic Response Coefficient, $C_{s,max2}$ = $\frac{S_{D1} * T_L}{T^2 * (R/I_e)}$ = 1.2505

Maximum Seismic Response Coefficient, $C_{s,max}$ = IF($T > T_L$; $C_{s,max2}$; $C_{s,max1}$) = 0.2876

Minimum Seismic Response Coefficient, $C_{s,min}$ = $0.044 * S_{DS} * I_e$ = 0.0440

Seismic Response Coefficient C_s = IF($C_{s,c} \geq C_{s,min}$;MIN($C_{s,c}$; $C_{s,max}$); $C_{s,min}$) = 0.2876

Seismic Base Shear

(According to Cl.12.8.1 of ASCE/SEI 7),

Effective Seismic Weight of Structure, W = 1305.00 kips

Seismic Base Shear V = $C_s * W$ = 375.32 kips

Calculation Summary

Seismic Base Shear V = $C_s * W$ = 375.32 kips